

## Flow Characteristics of Gas-Liquid Two Phase Plunging Jet Absorber —Gas Holdup and Bubble Penetration Depth—

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**Abstract**—A gas-liquid two phase plunging jet is formed through a gas sucking type multi-jet ejector nozzle. In this study, the effects of various conditions in the multi-jet ejector nozzle, the column diameter, and the liquid jet length on penetration depth of air bubbles  $l_b$  and gas holdup  $h_G$  in a gas-liquid two phase plunging jet absorber were studied experimentally. Consequently, empirical equations concerning  $l_b$  and  $h_G$  were obtained, respectively. These equations agree with the experimental data with an accuracy of  $\pm 20\%$  for  $l_b$  and  $\pm 25\%$  for  $h_G$ .

Key words : Gas Absorption, Plunging Jet Absorber, Biphasic Jet, Penetration Depth, Gas Holdup

### INTRODUCTION

Various kinds of devices using air bubble dispersion have been widely used as high performance gas-liquid contacting devices in chemical, fermentation, and waste treatment processes. Numerous attempts have been made by many researchers [Bin et al., 1982; Bin, 1993; Burgess et al., 1972, 1973; Funatsu et al., 1988; Ide et al., 1976; Ide et al., 1986; Kusabiraki et al., 1990; Mckeoh et al., 1981; Nishikawa et al., 1976; Ohkawa et al., 1985, 1987; Smigelshi et al., 1977; Suciú et al., 1976; Tojo et al., 1982; Van de sande et al., 1975; Weisweiler et al., 1978] to improve the performance of these devices. Their performance can be markedly improved by dispersing small solute bubbles in liquid phase and simultaneously increasing the turbulence of gas and liquid.

A plunging jet absorber is used as one of such high performance devices. Over the past few decades a considerable number of studies concerning a plunging jet absorber have been made. Some of these studies have been reported on gas entrainment [Bin, 1993; Kusabiraki et al., 1990; Mckeoh et al., 1981; Ohkawa et al., 1985, 1987], gas holdup [Bin, 1993; Funatsu et al., 1988], penetration depth of air bubbles [Bin, 1993; Kusabiraki et al., 1990; Mckeoh et al., 1981; Ohkawa et al., 1987; Smigelshi et al., 1977; Tojo et al., 1982; Van de sande et al., 1975; Suciú et al., 1976; Weisweiler et al., 1978], interfacial area [Bin et al., 1982; Bin, 1993; Burgess et al., 1972, 1973] and liquid-side volumetric mass transfer coefficient [Bin et al., 1982; Bin, 1993; Funatsu et al., 1988; Tojo et al., 1982]. In all cases, most of these studies have been made on a single phase plunging liquid jet absorber, but few studies have been reported on a gas-liquid two-phase plunging jet absorber [Ide et al., 1976, 1986].

In this present work, a new type of absorber using a gas-liquid two phase plunging jet which was formed through multi-

jet ejector nozzle was devised. This absorber has several advantages as follows. It doesn't need an air compressor for gas sucking and dispersion. It is simple in construction and operation, and it can provide intensive gas-liquid mixing through a gas sucking type multi-jet ejector nozzle. As it is a long column type tower, it has large gas holdup and gas-liquid contact area nevertheless with its small column volume.

The purpose of this study is to experimentally make clear the effects of various conditions in the multi-jet ejector nozzle, the column diameter, and the liquid jet length on penetration depth of air bubbles  $l_b$  and gas holdup  $h_G$  in a gas-liquid two phase plunging jet absorber.

### EXPERIMENTAL

A schematic diagram of absorber and plunging jet system is shown in Fig. 1. The transparent acrylic resin column of 1.11 m height was used and the diameter of column was varied from  $5 \times 10^{-2}$  to  $1.2 \times 10^{-1}$  m. The multi-jet ejector nozzle was attached to the top of the column. Fig. 2 shows details of the nozzle. The diameter of the liquid inlet duct to the nozzle  $D_p$  was  $1.8 \times 10^{-2}$  m, and the nozzle diameter  $D$  was varied from  $8 \times 10^{-3}$  to  $1.2 \times 10^{-2}$  m as shown in Table 1. The diameters of the gas inlet holes were constant,  $3 \times 10^{-3}$  m. The vertical length of the tapered section was  $2 \times 10^{-2}$  m, and the length of the nozzle was constant,  $2 \times 10^{-2}$  m. The A perforated plate made of brass was installed in this nozzle, of which hole diameter  $d$  was varied from  $2.57 \times 10^{-3}$  to  $4.78 \times 10^{-3}$  m, and the number of holes  $n$  was varied from 3 to 6. Hole area ratio of the perforated plate  $m_p$  was varied within the range of 0.061 to 0.166.  $m_p$  is determined by the following equation.

$$m_p = nd^2/D_p^2 \quad (1)$$

Liquid jets ejected through the perforated plate flowed into the nozzle. After liquid was mixed with gas in the nozzle, the plunging jet spouted from the nozzle, passing through a gas layer, plunged into a liquid bath through the gas liquid interface

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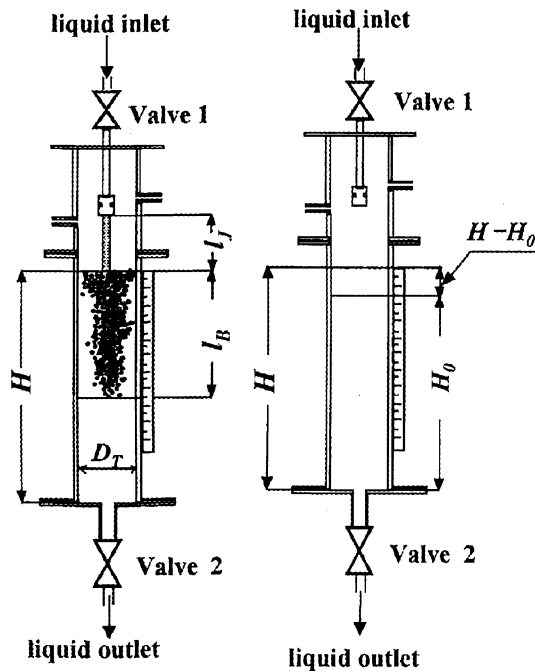


Fig. 1. Schematic diagram of absorber and plunging jet system.

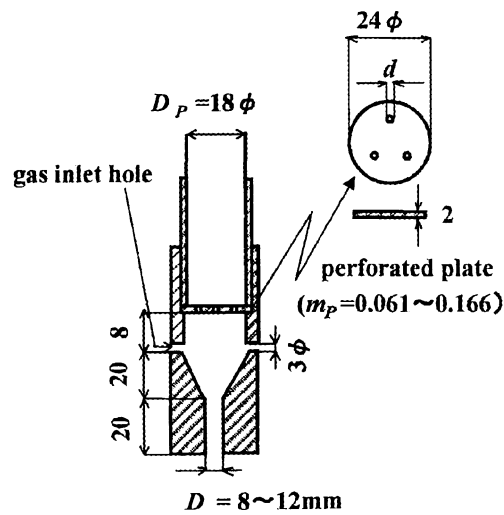


Fig. 2. Details of nozzle.

with a substantial amount of gas entrained and formed a submerged gas-liquid biphasic phase. The liquid jet length  $l_j$ , which was distance, from the nozzle exit to the liquid surface, was varied from 0.2 to 0.3 m. The penetration depth of air bubbles was measured by a scale fitted to the column wall. After the liquid flow was shut off by closing both valve 1 and valve 2 simultaneously, static dispersion height  $H_0$  was measured. Gas holdup is given from

$$h_G = (H - H_0) / l_B \quad (2)$$

where  $H$  represents the dispersion height of air bubbles. All experiments were carried out with air-water system at atmospheric pressure and room temperature. Experimental conditions and corresponding keys used in figures are shown in Table 1.

Table 1. Experimental conditions and corresponding keys

Key	$D_T$ [m]	$m_p$ [-]	$n$	$d$ [mm]	$D$ [m]	$l_j$ [m]
▽	0.05	0.061	3	2.57	0.01	
▼		0.097	6	2.29		
▼		0.166	6	2.99		
◇	0.075	0.061	3	2.57		
◆		0.097	6	2.29		
◆		0.166	6	2.99		
○		0.061	3	2.57	0.008	
●		0.097	6	2.29		
●		0.166	6	2.99		
○	0.1	0.061	3	2.57	0.01	0.2
●		0.073	6	1.99		
●		0.097	6	2.29		
●		0.10	3	3.28		
⊗		0.141	2	4.78		
⊗		0.153	3	4.06		
●		0.166	6	2.99	0.012	
○		0.061	3	2.57		
●		0.097	6	2.29		
●		0.166	6	2.99	0.3	
□		0.061	3	2.57		
△		0.061	3	2.57		
▲	0.12	0.073	6	1.99	0.01	0.2
▲		0.097	6	2.29		
▲		0.10	3	3.28		
▲		0.141	2	4.78		
▲		0.153	3	4.06		
▲		0.166	6	2.99		

## RESULTS AND DISCUSSION

### 1. Penetration Depth of Air Bubbles, $l_B$

Fig. 3 shows the relation between  $l_B$  and  $E_T$  for various  $m_p$  under the condition  $D_T=0.1$  m, and a comparison of  $l_B$  with those for a single phase plunging liquid jet is also shown.  $E_T$  is

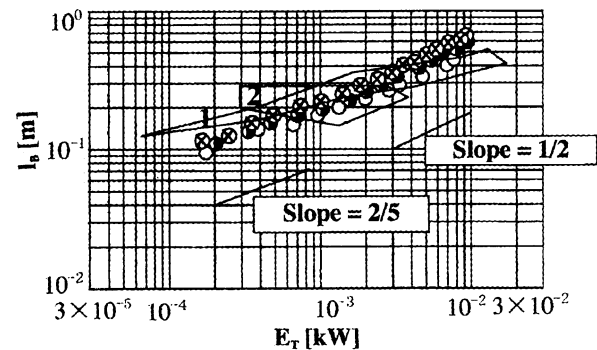


Fig. 3. Relation between  $l_B$  and  $E_T$  for various  $m_p$  ( $D_T=0.1$  m).

	$D$ [m]	$V_N$ [m/s]	Author
1	0.006-0.03	1-10	McKeoh et al., 1981
2	0.045	1-10	Tojo et al., 1982

given by the sum of kinetic energy and potential energy

$$E_T = Q_L (\rho_L u_0^2 / 2 + \rho_L g l_z) \quad (3)$$

where  $\rho_L$  is liquid density,  $u_0$  is liquid velocity based on cross-sectional area of holes for the perforated plate,  $g$  is acceleration of gravity, and  $l_z$  is liquid jet length ( $=l_j + 4.8 \times 10^{-2}$  m). As can be seen from this figure, it is found that  $l_B$  increases with increasing  $E_T$ .  $l_B$  is proportional to  $E_T^{2/5}$ , if  $E_T$  is less than  $1 \times 10^{-3}$  kW. On the other hand,  $l_B$  is proportional to  $E_T^{1/2}$ , if  $E_T$  is greater than this value. This is because the liquid jet under the liquid surface is dragged by downflow of surrounding liquid in the column when  $E_T$  is greater than  $1 \times 10^{-3}$  kW. Regions 1 and 2 surrounded by solid line designate the experimental results of Mckeoh et al.'s [1981] and Tojo et al.'s [1982], respectively. Tojo et al. [1982] reported the relationship between  $l_B$  and the jet kinetic power per unit volume of liquid content as  $l_B \propto (P/V)^{1/3}$ .  $P$  is equivalent to  $E_T$  in this work. The slope of their results was qualitatively similar to that of our study in the small  $E_T$  range. Fig. 4 shows relation between  $l_B$  and  $m_p$  under the condition that  $D_T$  and  $E_T$  are constant. It is found from the results of experimental data in Fig. 4 that  $l_B/D_p$  is proportional to  $m_p^{-1/3}$ .

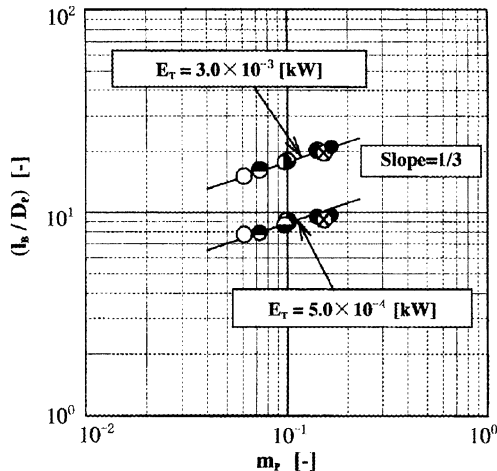


Fig. 4. Relation between  $l_B/D_p$  and  $m_p$  ( $D_T=0.1$  m).

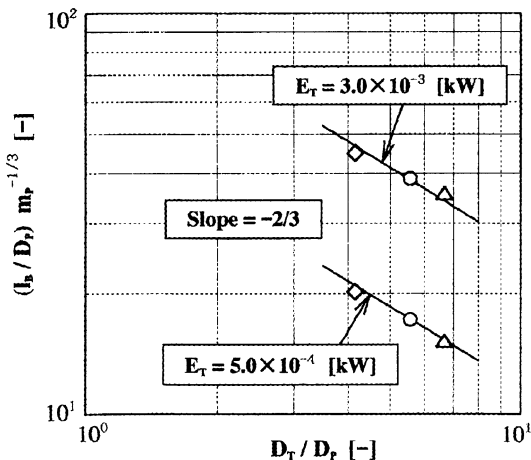


Fig. 5. Relation between  $(l_B/D_p)m_p^{-1/3}$  and  $(D_T/D_p)$ .

In order to clarify the effects of  $D_T$  on the penetration depth,  $(l_B/D_p)m_p^{-1/3}$  was plotted versus  $E_T$  for various  $D_T$ . As a result it was found that  $(l_B/D_p)m_p^{-1/3}$  decreased with  $D_T$  at constant value of  $E_T$ . Consequently,  $(l_B/D_p)m_p^{-1/3}$  was plotted against  $D_T/D_p$  in Fig. 5 under the condition that  $E_T$  are constant. As can be seen from this figure, it was found that  $(l_B/D_p)m_p^{-1/3}$  was proportional to  $D_T^{-2/3}$ . Considering the above results,  $(l_B/D_p)m_p^{-1/3}(D_T/D_p)^{2/3}$  was plotted against  $E_T$  in Fig. 6.

Ultimately, the following equations concerning  $l_B$  were obtained,

$$\text{for } 1.0 \times 10^{-4} \text{ kW} < E_T < 1.0 \times 10^{-3} \text{ kW}$$

$$(l_B/D_p) = 1.1 \times 10^3 m_p^{1/3} (D_T/D_p)^{-2/3} E_T^{2/5} \quad (4)$$

$$\text{for } 1.0 \times 10^{-3} \text{ kW} < E_T < 1.0 \times 10^{-2} \text{ kW}$$

$$(l_B/D_p) = 2.2 \times 10^3 m_p^{1/3} (D_T/D_p)^{-2/3} E_T^{1/2} \quad (5)$$

These equations agree with all experimental data with an accuracy of  $\pm 20\%$ .

## 2. Gas Holdup, $h_G$

$h_G$  was also measured under the experimental condition as shown in Table 1. Fig. 7 shows relation between  $h_G$  and  $E_T$  for various  $m_p$  under the condition,  $D_T=0.12$  m. It is found that  $h_G$

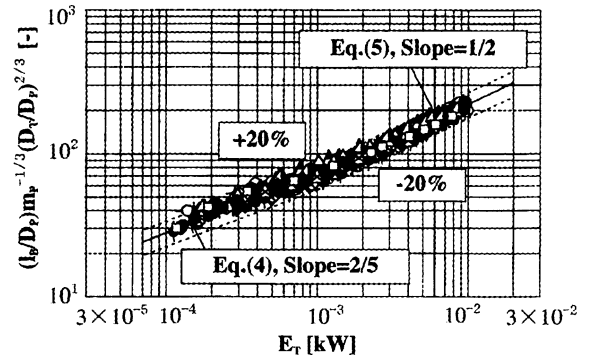


Fig. 6. Relation between  $(l_B/D_p)m_p^{-1/3}(D_T/D_p)^{2/3}$  and  $E_T$ .

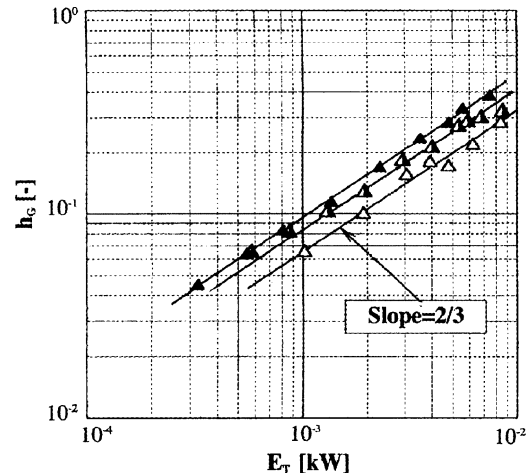
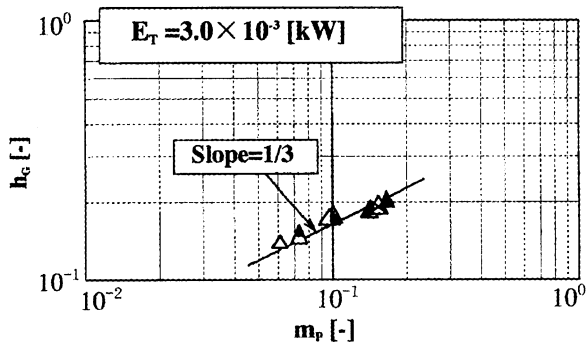
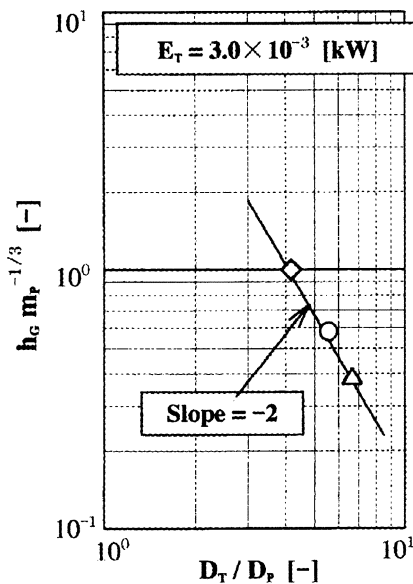


Fig. 7. Relation between  $h_G$  and  $E_T$  for various  $m_p$  ( $D_T=0.12$  m).

Fig. 8. Relation between  $h_G$  and  $m_p$  ( $D_T=0.12$  m).Fig. 9. Relation between  $h_G m_p^{-1/3}$  and  $D_T/D_p$ .

increases in proportion to  $E_T^{2/3}$ . Fig. 8 shows the relation between  $h_G$  and  $m_p$  under the condition,  $D_T=0.12$  m. From this figure, it is clear that  $h_G$  increases with increasing  $m_p$ , and that power to  $m_p$  is 1/3.

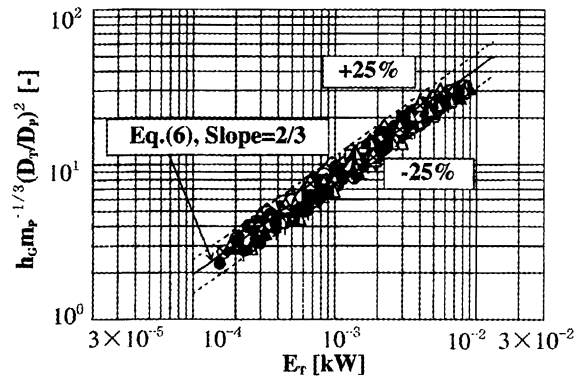
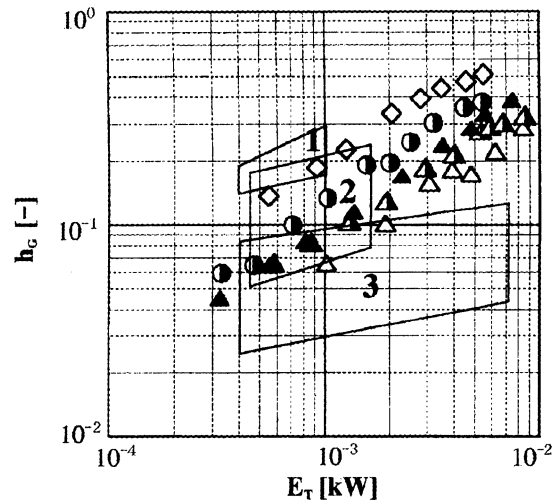
The relationship between  $h_G m_p^{-1/3}$  and  $D_T/D_p$  is shown in Fig. 9 in order to clarify the effect of  $D_T$  on  $h_G$ . As a result, it was found that  $h_G$  was inversely proportional to square of  $D_T$  with constant  $E_T$ . Considering all above results concerning  $h_G$ ,  $h_G m_p^{-1/3} (D_T/D_p)^2$  was plotted against  $E_T$  in Fig. 10.

Consequently, the following equation concerning  $h_G$  was obtained.

$$h_G = 9.0 \times 10^2 m_p^{1/3} (D_T/D_p)^{-2} E_T^{2/3} \quad (6)$$

This equation agrees with the all experimental data with an accuracy of  $\pm 25\%$ .

Fig. 11 shows a comparison of the observed values of  $h_G$  in this apparatus with those in other jet-type bubble columns [Nishikawa et al., 1976; Ohkawa et al., 1985; Weisweiler et al., 1978], where other Author's  $h_G$  were obtained on the basis of dispersion height, that is,  $h_G = (H - H_0)/H$ . As can be seen from this figure, it is found that the gas-liquid two phase plunging jet absorber gives large gas holdup.

Fig. 10. Relation between  $h_G m_p^{-1/3} (D_T/D_p)^2$  and  $E_T$ .

	$D$ [m]	$V_N$ [m/s]	$D_T$ [m]	Author
1	0.013-0.025	0.12-0.2	0.06-0.2	Ohkawa et al., 1985
2	0.008-0.045	0-2.6	0.05-0.07	Nishikawa et al., 1976
3	0.002	0-25	0.16	Weisweiler et al., 1978

Fig. 11. Comparison of  $h_G$  observed in this apparatus with those in other jet-type of bubble columns.

## CONCLUSION

The effects of various conditions in the gas sucking type multi-jet ejector nozzle, the column diameter and the length of liquid jet on penetration depth of air bubbles  $l_b$  and gas holdup  $h_G$  in a gas-liquid two phase plunging jet absorber were studied experimentally. The following conclusions were obtained in the experimental conditions of the system for  $2.0 < l_b/D_p < 4.0 \times 10^1$ ,  $2.0 \times 10^{-2} < h_G < 6.0 \times 10^{-1}$ ,  $0.061 \leq m_p \leq 0.166$ ,  $2.78 \leq D_T/D_p \leq 6.67$ ,  $1.0 \times 10^{-4} \text{ kW} < E_T < 1.0 \times 10^{-2} \text{ kW}$ .

1. Penetration depth of air bubbles  $l_b$  and gas holdup  $h_G$  increased with increasing hole area ratio of the perforated plate  $m_p$  under condition that the column diameter  $D_T$  and liquid jet's total power  $E_T$  were constant.

2.  $l_b$  and  $h_G$  decreased with increasing  $D_T$  for constant  $E_T$ .

3. The empirical equations concerning  $l_b$  and  $h_G$  were obtained, respectively. These equations agree with the experimental data with an accuracy of  $\pm 20\%$  for  $l_b$  and  $\pm 25\%$  for  $h_G$ .

## NOMENCLATURE

- $d$  : hole diameter of perforated plate [m]  
 $D$  : inside diameter of nozzle [m]  
 $D_p$  : diameter of the liquid inlet duct to nozzle [m]  
 $D_T$  : column diameter [m]  
 $E_T$  : liquid jet's total power [kW]  
 $g$  : acceleration of gravity [ $\text{m/s}^2$ ]  
 $H$  : dispersion height of air bubbles [m]  
 $H_0$  : static dispersion height [m]  
 $h_G$  : gas holdup [-]  
 $l_B$  : penetration depth of air bubbles [m]  
 $l_J$  : liquid jet length [m]  
 $l_z$  : distance from perforated plate to liquid surface ( $=l_J+4.8 \times 10^{-2}$ ) [m]  
 $m_p$  : hole area ratio of perforated plate ( $=nd^2/D_p^2$ ) [-]  
 $n$  : number of holes of perforated plate [-]  
 $P$  : jet kinetic power [kW]  
 $Q_L$  : volumetric flow rate of liquid [ $\text{m}^3/\text{s}$ ]  
 $u_0$  : liquid velocity based on cross-sectional area of holes for the perforated plate [m/s]  
 $V$  : volume of liquid content [ $\text{m}^3$ ]  
 $V_J$  : jet velocity at nozzle exit [m/s]

## Greek Letter

- $\rho_L$  : liquid density [ $\text{kg/m}^3$ ]

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