

# Measurement and Correlation of Isobaric Vapor-Liquid Equilibria for Binary and Ternary Systems Containing Methyl Tertiary Butyl Ether (MTBE), Methanol and Alkanes

Toru Watanabe<sup>†</sup>, Katsumi Honda\* and Yasuhiko Arai\*

Department of Chemical Science and Engineering, Ariake National College of Technology, Omuta, 836-8585, Japan

\*Department of Chemical Engineering, Faculty of Engineering, Kyushu University, Fukuoka, 812-8581, Japan

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**Abstract**—Isobaric vapor-liquid equilibria (VLE) of four binary systems—methyl tertiary butyl ether (MTBE)+methanol, MTBE+heptane, MTBE+octane and MTBE+i-octane—were measured at atmospheric pressure by using Othmer-type circulation method. The VLE of a ternary system, MTBE+methanol+heptane, were also measured at atmospheric pressure. These VLE data were predicted by ASOG and correlated by Wilson equation, and the prediction and correlation performances were discussed.

Key words: Vapor-Liquid Equilibria, Measurement, Correlation, MTBE, Alkane

## INTRODUCTION

Ethers and alcohols used as gasoline additives have been remarked as octane number enhancing and environmental protection agents. The vapor-liquid equilibria (VLE) are required to assess the phase behavior of those mixtures in producing and blending operations. Methyl tertiary butyl ether (MTBE) seems to be a promising ether.

In this study, isobaric VLE data of four binary systems (MTBE+methanol, MTBE+heptane, MTBE+octane and MTBE+i-octane), and of a ternary system (MTBE+methanol+heptane) were measured at atmospheric pressure by using an Othmer-type circulation still. Although a few isobaric VLE data of binary systems containing MTBE have been reported to date in the literature for MTBE+methanol [Aim and Ciprin, 1980; Arce et al., 1996; Toghiani et al., 1996; Komatsu et al., 1997; Loras et al., 1999], for MTBE+heptane [Wisniak et al., 1997a] and for MTBE+octane [Wisniak et al., 1997b; Hiaki et al., 1999], there is no isobaric VLE data for MTBE+i-octane and the present ternary system. The VLE data obtained in this work were predicted by ASOG [Tochigi et al., 1990] and correlated by Wilson equation [Wilson et al., 1964]. Their prediction and correlation performances were discussed.

## EXPERIMENTAL

### 1. Materials

MTBE supplied by Tokyo Kasei Kogyo and methanol, heptane, octane and i-octane supplied by Wako Pure Chemical Industries were special grade reagents. They were used without further purification because no impurities were detected by the gas chromatographic analysis. The purities are estimated to be more than 99.8%, 99%, 99%, 99% and 98% for methanol, MTBE, heptane, i-octane and octane, respectively.

### 2. Apparatus and Procedure

An all-glass Othmer-type apparatus modified by the author [Wata-

nabe, 1985] was used to measure the VLE relation at atmospheric pressure. The equilibrium still is about 160 mL in volume and is equipped with four baffle plates and a propeller agitator to sufficiently mix the liquid mixture. After the liquid mixture was evaporated, liquid drops of the condensed vapor were adjusted to be a proper rate for one hour. Liquid and vapor phase samples were analyzed with a gas chromatograph (Yanagimoto G2800-F) equipped with a flame ionization detector (FID) and an integrator. To determine their compositions, an internal standard method was adopted for calibration of the FID response.

The temperatures were measured with copper- or iron-constantan thermocouples. The uncertainties of the present experiment are believed to be  $\pm 0.1$  K in temperature measurements. From the reproducibility, the uncertainties of mole fractions reported are estimated to be within  $\pm 0.001$ .

## RESULTS AND DISCUSSION

### 1. Fundamental Equation

VLE relation at low pressure can be calculated based on the following equation when no significant interaction such as association occurs in vapor phase.

$$\pi y_i = \gamma_i x_i P_i^0 \quad (1)$$

**Table 1. Antoine constants<sup>a</sup>**

| Component | Boiling point [K] | Constants |          |         | Lit. |
|-----------|-------------------|-----------|----------|---------|------|
|           |                   | A         | B        | C       |      |
| MTBE      | 328.3             | 6.038757  | 1149.261 | -43.150 | b    |
| Methanol  | 337.7             | 7.025886  | 1474.078 | -44.020 | b    |
| Heptane   | 371.6             | 6.020230  | 1263.909 | -56.718 | c    |
| Octane    | 398.9             | 6.043940  | 1351.938 | -64.030 | d    |
| i-Octane  | 372.4             | 5.936790  | 1257.840 | -53.415 | e    |

<sup>a</sup> $\log(P/kPa) = A - B / [(T/K) + C]$ . <sup>b</sup>Arce et al. [1996]. <sup>c</sup>Wisniak et al. [1997a]. <sup>d</sup>Hiaki et al. [1999]. <sup>e</sup>Loras et al. [2000].

<sup>†</sup>To whom correspondence should be addressed.

E-mail: watanabe@ce.ariake-nct.ac.jp

where  $\pi$  is the total pressure,  $\gamma_i$  is the liquid phase activity coefficient,  $p_i^0$  is the vapor pressure of pure component,  $x_i$  and  $y_i$  are liquid and vapor phase mole fractions, respectively. In this case  $\pi=101.3$  kPa and  $p_i^0$  can be calculated by using Antoine equation of which constants are presented in Table 1.

## 2. VLE Data and Consistency Tests

VLE data of four binary systems at atmospheric pressure are presented in Tables 2-5. The activity coefficients were evaluated by Eq. (1) using the present x-y data and they are given in Tables 2-5. The experimental data were examined by thermodynamic consistency tests: the area test [Herington, 1951] and the point test [Van Ness et al., 1973]. The results are summarized in Table 6. As shown in Table 6, the consistency tests are not satisfied for MTBE+heptane and MTBE+octane. This may be due to the fact that these binary mixtures are almost ideal and therefore activity coefficients are nearly unity [Miyamoto et al., 2001]. The present VLE data of MTBE+methanol and MTBE+octane are compared with the literature data. As shown in Figs. 1 and 2, they are in good agreement though the results of Komatsu et al. [1997] for MTBE+methanol show deviation.

VLE data at atmospheric pressure of a ternary system, MTBE+methanol+heptane, are shown in Table 7. The data were obtained in the homogeneous liquid region. The activity coefficients evalu-

**Table 2. Experimental VLE data for MTBE(1)+methanol(2) at atmospheric pressure**

| T/K   | $x_1$  | $y_1$ | $\gamma_1$ | $\gamma_2$ |
|-------|--------|-------|------------|------------|
| 336.7 | 0.0091 | 0.055 | 4.617      | 0.992      |
| 335.6 | 0.024  | 0.090 | 2.998      | 1.013      |
| 334.6 | 0.037  | 0.131 | 2.910      | 1.021      |
| 333.9 | 0.042  | 0.150 | 3.012      | 1.031      |
| 334.1 | 0.059  | 0.191 | 2.688      | 0.992      |
| 332.1 | 0.085  | 0.246 | 2.545      | 1.031      |
| 331.6 | 0.120  | 0.311 | 2.315      | 1.001      |
| 330.2 | 0.132  | 0.351 | 2.501      | 1.011      |
| 329.6 | 0.174  | 0.383 | 2.102      | 1.037      |
| 328.5 | 0.190  | 0.422 | 2.201      | 1.036      |
| 328.5 | 0.218  | 0.458 | 2.082      | 1.006      |
| 327.7 | 0.250  | 0.473 | 1.925      | 1.055      |
| 327.3 | 0.274  | 0.471 | 1.769      | 1.113      |
| 327.5 | 0.288  | 0.500 | 1.776      | 1.064      |
| 326.1 | 0.313  | 0.497 | 1.697      | 1.178      |
| 325.7 | 0.357  | 0.546 | 1.658      | 1.154      |
| 325.8 | 0.394  | 0.556 | 1.524      | 1.194      |
| 325.7 | 0.438  | 0.575 | 1.423      | 1.237      |
| 325.2 | 0.484  | 0.592 | 1.349      | 1.320      |
| 324.7 | 0.523  | 0.613 | 1.313      | 1.387      |
| 324.9 | 0.575  | 0.643 | 1.245      | 1.421      |
| 324.6 | 0.664  | 0.672 | 1.137      | 1.676      |
| 324.2 | 0.697  | 0.693 | 1.133      | 1.768      |
| 324.7 | 0.725  | 0.708 | 1.094      | 1.814      |
| 325.1 | 0.826  | 0.760 | 1.018      | 2.312      |
| 325.2 | 0.847  | 0.787 | 1.024      | 2.327      |
| 325.3 | 0.884  | 0.798 | 0.991      | 2.900      |
| 325.4 | 0.933  | 0.891 | 1.045      | 2.702      |

**Table 3. Experimental VLE data for MTBE(1)+heptane(2) at atmospheric pressure**

| T/K   | $x_1$ | $y_1$ | $\gamma_1$ | $\gamma_2$ |
|-------|-------|-------|------------|------------|
| 366.6 | 0.046 | 0.195 | 1.405      | 0.979      |
| 365.8 | 0.056 | 0.217 | 1.315      | 0.986      |
| 364.4 | 0.069 | 0.233 | 1.190      | 1.022      |
| 360.0 | 0.135 | 0.381 | 1.110      | 1.019      |
| 354.5 | 0.216 | 0.515 | 1.088      | 1.051      |
| 353.1 | 0.250 | 0.554 | 1.049      | 1.059      |
| 351.0 | 0.277 | 0.588 | 1.064      | 1.090      |
| 349.9 | 0.299 | 0.615 | 1.065      | 1.089      |
| 345.0 | 0.384 | 0.704 | 1.090      | 1.130      |
| 342.0 | 0.489 | 0.778 | 1.036      | 1.132      |
| 341.2 | 0.502 | 0.786 | 1.042      | 1.156      |
| 340.6 | 0.514 | 0.795 | 1.049      | 1.158      |
| 337.4 | 0.572 | 0.824 | 1.076      | 1.269      |
| 336.8 | 0.588 | 0.839 | 1.085      | 1.233      |
| 336.2 | 0.615 | 0.846 | 1.066      | 1.291      |
| 334.4 | 0.664 | 0.865 | 1.067      | 1.386      |
| 335.2 | 0.674 | 0.875 | 1.037      | 1.286      |
| 334.2 | 0.723 | 0.899 | 1.025      | 1.269      |
| 332.5 | 0.746 | 0.914 | 1.066      | 1.259      |
| 332.1 | 0.816 | 0.940 | 1.015      | 1.225      |
| 330.4 | 0.881 | 0.967 | 1.021      | 1.126      |
| 329.7 | 0.924 | 0.981 | 1.009      | 1.052      |
| 330.0 | 0.934 | 0.980 | 0.988      | 1.267      |

**Table 4. Experimental VLE data for MTBE(1)+octane(2) at atmospheric pressure**

| T/K   | $x_1$ | $y_1$ | $\gamma_1$ | $\gamma_2$ |
|-------|-------|-------|------------|------------|
| 395.0 | 0.010 | 0.058 | 1.031      | 1.060      |
| 396.0 | 0.011 | 0.060 | 0.906      | 1.030      |
| 395.0 | 0.017 | 0.097 | 0.955      | 1.025      |
| 393.4 | 0.025 | 0.140 | 0.985      | 1.029      |
| 388.7 | 0.056 | 0.296 | 1.042      | 0.997      |
| 387.7 | 0.061 | 0.305 | 1.012      | 1.019      |
| 386.1 | 0.062 | 0.339 | 1.147      | 1.017      |
| 385.2 | 0.077 | 0.327 | 0.907      | 1.082      |
| 380.8 | 0.092 | 0.440 | 1.119      | 1.049      |
| 379.4 | 0.106 | 0.468 | 1.076      | 1.055      |
| 377.8 | 0.114 | 0.501 | 1.111      | 1.052      |
| 379.0 | 0.115 | 0.463 | 0.983      | 1.092      |
| 378.8 | 0.118 | 0.487 | 1.016      | 1.053      |
| 377.2 | 0.118 | 0.503 | 1.092      | 1.071      |
| 373.4 | 0.154 | 0.590 | 1.075      | 1.041      |
| 365.9 | 0.204 | 0.681 | 1.127      | 1.105      |
| 366.4 | 0.204 | 0.682 | 1.113      | 1.086      |
| 363.4 | 0.235 | 0.721 | 1.106      | 1.096      |
| 358.8 | 0.272 | 0.753 | 1.123      | 1.202      |
| 357.1 | 0.299 | 0.792 | 1.125      | 1.116      |
| 352.7 | 0.369 | 0.840 | 1.091      | 1.121      |
| 348.7 | 0.415 | 0.859 | 1.108      | 1.238      |
| 343.2 | 0.505 | 0.902 | 1.120      | 1.263      |

**Table 4. Continued**

| T/K   | $x_1$ | $y_1$ | $\gamma_1$ | $\gamma_2$ |
|-------|-------|-------|------------|------------|
| 340.5 | 0.587 | 0.926 | 1.073      | 1.270      |
| 338.2 | 0.665 | 0.949 | 1.041      | 1.195      |
| 334.9 | 0.736 | 0.962 | 1.054      | 1.292      |
| 333.5 | 0.797 | 0.972 | 1.029      | 1.295      |
| 331.6 | 0.863 | 0.983 | 1.020      | 1.296      |
| 329.7 | 0.943 | 0.993 | 1.002      | 1.336      |

**Table 5. Experimental VLE data for MTBE(1)+i-octane(2) at atmospheric pressure**

| T/K   | $x_1$ | $y_1$ | $\gamma_1$ | $\gamma_2$ |
|-------|-------|-------|------------|------------|
| 366.6 | 0.047 | 0.167 | 1.169      | 1.034      |
| 361.3 | 0.114 | 0.326 | 1.086      | 1.054      |
| 358.0 | 0.172 | 0.454 | 1.097      | 1.011      |
| 353.6 | 0.208 | 0.540 | 1.213      | 1.023      |
| 354.2 | 0.226 | 0.538 | 1.091      | 1.033      |
| 351.0 | 0.283 | 0.632 | 1.123      | 0.981      |
| 348.9 | 0.332 | 0.663 | 1.065      | 1.033      |
| 347.4 | 0.359 | 0.689 | 1.068      | 1.046      |
| 346.5 | 0.360 | 0.688 | 1.090      | 1.084      |
| 344.8 | 0.406 | 0.737 | 1.086      | 1.044      |
| 345.1 | 0.408 | 0.739 | 1.075      | 1.028      |
| 342.3 | 0.477 | 0.778 | 1.052      | 1.085      |
| 342.2 | 0.496 | 0.794 | 1.036      | 1.048      |
| 341.0 | 0.499 | 0.792 | 1.064      | 1.112      |
| 340.2 | 0.514 | 0.807 | 1.077      | 1.096      |
| 339.8 | 0.550 | 0.825 | 1.042      | 1.088      |
| 339.8 | 0.568 | 0.838 | 1.025      | 1.050      |
| 337.9 | 0.618 | 0.862 | 1.026      | 1.081      |
| 336.8 | 0.643 | 0.871 | 1.030      | 1.123      |
| 334.0 | 0.753 | 0.917 | 1.009      | 1.164      |
| 331.8 | 0.834 | 0.950 | 1.014      | 1.116      |
| 329.6 | 0.925 | 0.978 | 1.009      | 1.176      |

**Table 6. Thermodynamic consistency tests**

| System        | Area test |         | Point test |         |
|---------------|-----------|---------|------------|---------|
|               | D-J       | Results | $\Delta y$ | Results |
| MTBE+methanol | 1.6       | +       | 0.008      | +       |
| MTBE+heptane  | 31.4      | -       | 0.021      | -       |
| MTBE+octane   | 70.1      | -       | 0.021      | -       |
| MTBE+i-octane | 28.3      | -       | 0.007      | +       |

Criterion of consistency (character: +) D-J < 10  $\Delta y$  < 0.01

where  $D = 100 \left| \int_0^1 \log(\gamma_1/\gamma_2) dx_1 \right| \left| \int_0^1 \log(\gamma_1/\gamma_2) dx_1 \right|$ ,

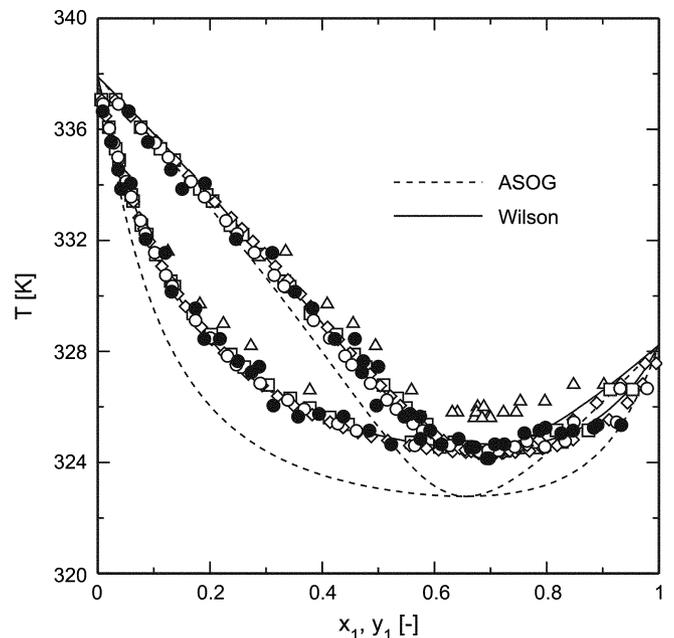
$$J = 150(T_{max} - T_{min})/T_{min}, \Delta y = \frac{1}{N} \sum_k |y_{cat} - y_{exp}|_k,$$

N = number of data points.

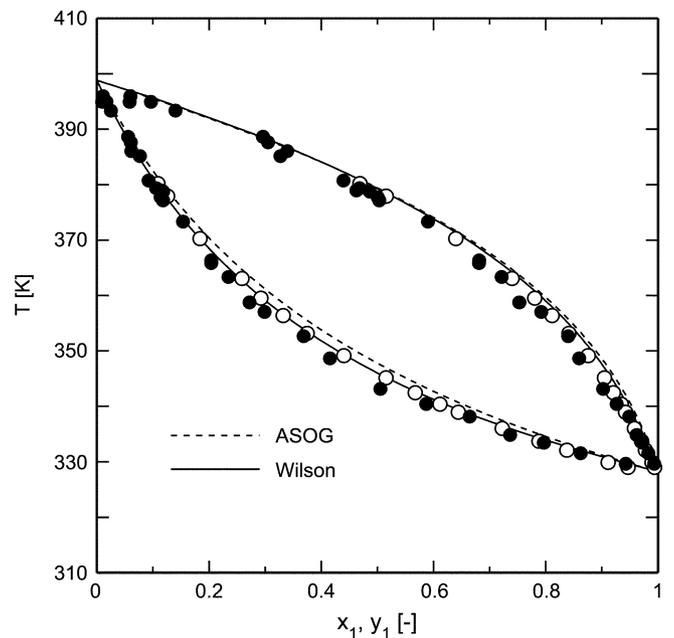
ated by Eq. (1) are also given in Table 7. The present ternary system does not form a ternary azeotrope, though the minimum boiling point azeotrope is found in MTBE+methanol as shown in Fig. 1.

### 3. Correlation and Prediction

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**Fig. 1. VLE relation for MTBE(1)+methanol(2) at atmospheric pressure: (●) this work; (○) Aim and Ciprin; (◇) Arce et al., (△) Komatsu et al., (□) Toghiani et al.**



**Fig. 2. VLE relation for MTBE(1)+octane(2) at atmospheric pressure: (●) this work; (○) Hiaki et al.**

VLE relation  $x_1 \sim y_1$  can be obtained by using Eq. (1) when the liquid phase activity coefficients are given by any model. First, we attempted to predict the activity coefficients by ASOG because it is widely used, as well as UNIFAC, in the prediction of phase equilibria for many mixtures. The ASOG parameters required were cited from the literature [Tochigi et al., 1990]. For the binary systems the prediction performances are listed in Table 8 and the comparisons between experimental and predicted results are illustrated in Figs. 1

**Table 7. Experimental VLE data for MTBE(1)+methanol(2)+heptane(3) at atmospheric pressure**

| T/K   | x <sub>1</sub> | x <sub>2</sub> | y <sub>1</sub> | y <sub>2</sub> | γ <sub>1</sub> | γ <sub>2</sub> | γ <sub>3</sub> |
|-------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| 340.1 | 0.077          | 0.071          | 0.105          | 0.612          | 0.930          | 7.883          | 0.929          |
| 330.7 | 0.087          | 0.478          | 0.149          | 0.667          | 1.574          | 1.851          | 1.681          |
| 330.7 | 0.090          | 0.841          | 0.190          | 0.674          | 1.942          | 1.062          | 7.886          |
| 329.7 | 0.091          | 0.777          | 0.159          | 0.660          | 1.667          | 1.174          | 5.657          |
| 333.6 | 0.096          | 0.095          | 0.111          | 0.654          | 0.976          | 8.114          | 1.032          |
| 330.6 | 0.098          | 0.587          | 0.126          | 0.683          | 1.186          | 1.550          | 2.421          |
| 329.9 | 0.098          | 0.832          | 0.207          | 0.655          | 1.997          | 1.078          | 8.113          |
| 330.1 | 0.100          | 0.748          | 0.191          | 0.644          | 1.789          | 1.170          | 4.441          |
| 330.0 | 0.101          | 0.816          | 0.193          | 0.662          | 1.797          | 1.108          | 7.148          |
| 330.7 | 0.102          | 0.575          | 0.113          | 0.675          | 1.019          | 1.557          | 2.609          |
| 330.3 | 0.105          | 0.654          | 0.147          | 0.662          | 1.307          | 1.363          | 3.209          |
| 331.8 | 0.119          | 0.312          | 0.135          | 0.657          | 1.011          | 2.671          | 1.395          |
| 336.0 | 0.119          | 0.090          | 0.146          | 0.586          | 0.961          | 6.960          | 1.098          |
| 330.0 | 0.120          | 0.777          | 0.213          | 0.644          | 1.676          | 1.132          | 5.642          |
| 332.0 | 0.130          | 0.194          | 0.138          | 0.638          | 0.938          | 4.132          | 1.257          |
| 331.6 | 0.139          | 0.220          | 0.141          | 0.645          | 0.908          | 3.749          | 1.285          |
| 329.4 | 0.143          | 0.737          | 0.223          | 0.640          | 1.498          | 1.216          | 4.764          |
| 333.3 | 0.149          | 0.144          | 0.168          | 0.601          | 0.952          | 4.976          | 1.180          |
| 329.7 | 0.161          | 0.718          | 0.249          | 0.617          | 1.472          | 1.188          | 4.570          |
| 329.5 | 0.166          | 0.670          | 0.296          | 0.570          | 1.704          | 1.186          | 3.413          |
| 334.7 | 0.168          | 0.063          | 0.204          | 0.539          | 0.985          | 9.607          | 1.141          |
| 329.5 | 0.176          | 0.672          | 0.258          | 0.604          | 1.402          | 1.252          | 3.798          |
| 329.9 | 0.189          | 0.456          | 0.220          | 0.604          | 1.098          | 1.816          | 2.034          |
| 329.2 | 0.198          | 0.592          | 0.239          | 0.632          | 1.169          | 1.506          | 2.580          |
| 330.4 | 0.221          | 0.276          | 0.236          | 0.582          | 0.993          | 2.834          | 1.459          |
| 329.7 | 0.231          | 0.358          | 0.253          | 0.574          | 1.040          | 2.217          | 1.745          |
| 331.5 | 0.237          | 0.140          | 0.225          | 0.581          | 0.853          | 5.336          | 1.200          |
| 335.1 | 0.253          | 0.067          | 0.316          | 0.452          | 1.001          | 7.485          | 1.146          |
| 328.7 | 0.270          | 0.582          | 0.296          | 0.623          | 1.079          | 1.544          | 2.335          |
| 331.4 | 0.280          | 0.158          | 0.293          | 0.543          | 0.940          | 4.424          | 1.136          |
| 329.5 | 0.289          | 0.274          | 0.294          | 0.545          | 0.971          | 2.778          | 1.536          |
| 329.2 | 0.303          | 0.434          | 0.313          | 0.564          | 0.999          | 1.833          | 1.972          |
| 326.6 | 0.304          | 0.642          | 0.449          | 0.503          | 1.551          | 1.234          | 4.187          |
| 329.2 | 0.308          | 0.445          | 0.342          | 0.530          | 1.074          | 1.682          | 2.185          |
| 328.7 | 0.313          | 0.455          | 0.357          | 0.520          | 1.120          | 1.647          | 2.279          |
| 329.0 | 0.314          | 0.346          | 0.335          | 0.528          | 1.038          | 2.169          | 1.719          |
| 329.2 | 0.314          | 0.342          | 0.332          | 0.527          | 1.022          | 2.178          | 1.721          |
| 330.4 | 0.332          | 0.175          | 0.359          | 0.477          | 1.005          | 3.663          | 1.337          |
| 329.7 | 0.351          | 0.368          | 0.369          | 0.532          | 0.998          | 1.999          | 1.460          |
| 329.0 | 0.368          | 0.386          | 0.391          | 0.496          | 1.032          | 1.832          | 1.949          |
| 332.4 | 0.374          | 0.077          | 0.431          | 0.393          | 1.007          | 6.316          | 1.192          |
| 329.4 | 0.398          | 0.219          | 0.398          | 0.474          | 0.960          | 3.024          | 1.403          |
| 326.5 | 0.435          | 0.512          | 0.514          | 0.457          | 1.248          | 1.412          | 2.557          |
| 327.8 | 0.448          | 0.277          | 0.459          | 0.438          | 1.036          | 2.371          | 1.662          |
| 329.7 | 0.479          | 0.166          | 0.495          | 0.387          | 0.983          | 3.218          | 1.380          |
| 328.5 | 0.490          | 0.226          | 0.490          | 0.410          | 0.988          | 2.639          | 1.536          |
| 325.1 | 0.503          | 0.467          | 0.560          | 0.408          | 1.231          | 1.468          | 5.206          |
| 325.3 | 0.529          | 0.407          | 0.572          | 0.395          | 1.188          | 1.618          | 2.469          |
| 327.7 | 0.532          | 0.264          | 0.529          | 0.396          | 1.008          | 2.255          | 1.660          |
| 330.2 | 0.535          | 0.086          | 0.582          | 0.292          | 1.018          | 4.584          | 1.353          |
| 328.5 | 0.568          | 0.166          | 0.589          | 0.329          | 1.025          | 2.886          | 1.338          |
| 327.3 | 0.614          | 0.187          | 0.605          | 0.328          | 1.014          | 2.684          | 1.516          |
| 328.8 | 0.661          | 0.089          | 0.696          | 0.222          | 1.031          | 3.571          | 1.416          |
| 325.8 | 0.727          | 0.231          | 0.705          | 0.280          | 1.047          | 1.969          | 1.841          |
| 326.7 | 0.769          | 0.088          | 0.753          | 0.201          | 1.028          | 3.581          | 1.491          |

**Table 8. Prediction and correlation performances for binary systems**

| System        | N  | ASOG   |                     | Wilson |                     |
|---------------|----|--------|---------------------|--------|---------------------|
|               |    | ΔT [K] | Δy <sub>1</sub> [-] | ΔT [K] | Δy <sub>1</sub> [-] |
| MTBE+methanol | 28 | 1.8    | 0.034               | 0.3    | 0.009               |
| MTBE+heptane  | 23 | 1.9    | 0.015               | 0.9    | 0.012               |
| MTBE+octane   | 29 | 2.1    | 0.010               | 1.0    | 0.013               |
| MTBE+i-octane | 22 | 1.9    | 0.011               | 0.4    | 0.006               |

$$\Delta T = \frac{1}{N} \sum_i |T_{cal} - T_{exp}|, \Delta y_1 = \frac{1}{N} \sum_i |y_{1,cal} - y_{1,exp}|,$$

N=number of data points.

and 2 for example. As shown in Table 8 and Figs. 1 and 2, the agreement seems to be insufficient. The ASOG parameters should be re-evaluated in the future work.

Then VLE relations for the binary systems were correlated by using the Wilson equation:

$$\ln \gamma_1 = -\ln(x_1 + \Lambda_{12}x_2) + x_2 \left( \frac{\Lambda_{12}}{x_1 + \Lambda_{12}x_2} - \frac{\Lambda_{21}}{\Lambda_{21}x_1 + x_2} \right) \quad (2)$$

$$\ln \gamma_2 = -\ln(\Lambda_{21}x_1 + x_2) - x_1 \left( \frac{\Lambda_{12}}{x_1 + \Lambda_{12}x_2} - \frac{\Lambda_{21}}{\Lambda_{21}x_1 + x_2} \right) \quad (3)$$

where  $\Lambda_{12}$  and  $\Lambda_{21}$  are the parameters adjusted by using experimental VLE data. The binary parameters determined by using present VLE data are in Table 9. The correlation performances of Wilson equation presented in Table 8 and Figs. 1 and 2 for binary systems. A good agreement between experiment and correlation is obtained. An advantage of Wilson equation is that the VLE relation for a multicomponent system can be calculated with the binary parameters of the constituent binary systems. VLE of the present ternary system, MTBE+methanol+heptane, were calculated by using the binary parameters given in Table 9. The correlation performance is presented in Table 10 in which the prediction performance of ASOG is also given for comparison. Comparisons of the experimental data with the correlated values for typical tie-lines are shown in Fig. 3. As shown in Table 10 and Fig. 3, a fairly good agreement is ob-

**Table 9. Wilson parameters**

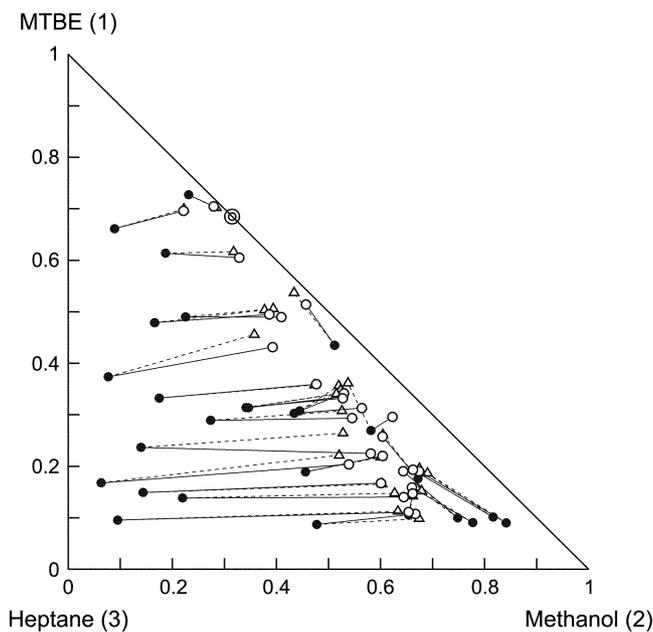
| System              | $\Lambda_{12}$ [-] | $\Lambda_{21}$ [-] |
|---------------------|--------------------|--------------------|
| MTBE(1)+methanol(2) | 0.50044            | 0.48033            |
| MTBE(1)+heptane(2)  | 0.42008            | 1.49185            |
| MTBE(1)+octane(2)   | 2.08019            | 0.21056            |
| MTBE(1)+i-octane(2) | 0.88652            | 0.92845            |

**Table 10. Prediction and correlation performances for MTBE(1)+methanol(2)+heptane(3)**

| Model  | ΔT [K] | Δy <sub>1</sub> [-] | Δy <sub>2</sub> [-] | Δy <sub>3</sub> [-] |
|--------|--------|---------------------|---------------------|---------------------|
| ASOG   | 1.1    | 0.020               | 0.026               | 0.013               |
| Wilson | 1.0    | 0.009               | 0.017               | 0.014               |

$$\Delta T = \frac{1}{N} \sum_i |T_{cal} - T_{exp}|, \Delta y_i = \frac{1}{N} \sum_i |y_{i,cal} - y_{i,exp}|, (i=1, 2, 3),$$

N=number of data points.



**Fig. 3.** Tie-lines for MTBE(1)+methanol(2)+heptane(3) at atmospheric pressure: (●) experimental data of liquid phase; (○) experimental data of vapor phase; (△) predicted values of vapor phase by Wilson equation; (⊙) azeotrope.

tained.

### CONCLUSION

Isobaric VLE relations of binary and ternary systems containing MTBE were measured at atmospheric pressure by using a modified Othmer-type circulation apparatus. The data are reported for four binary systems—MTBE+methanol, MTBE+heptane, MTBE+octane and MTBE+i-octane, and also for a ternary system—MTBE+methanol+heptane. For the present data, the prediction performance of ASOG and the correlation performance of Wilson equation were discussed. It is noted that ASOG parameters should be re-evaluated in the future work to give better prediction results. The Wilson equation can be adopted to correlate VLE of the present binary and ternary systems.

### NOMENCLATURE

- $p_i^0$  : vapor pressure of pure component  $i$  [Pa]  
 $x_i$  : liquid phase mole fraction of component  $i$  [-]  
 $y_i$  : vapor phase mole fraction of component  $i$  [-]

### Greek Letters

- $\gamma_i$  : liquid phase activity coefficient of component  $i$  [-]  
 $A_{12}, A_{21}$  : Wilson interaction parameters between components 1 and 2 for binary system [-]

$\pi$  : total pressure [Pa]

### REFERENCES

- Aim, K. and Ciprin, M., "Vapor Pressures, Refractive Index at 20.0 °C, and Vapor-Liquid Equilibrium at 101.325 kPa in the Methyl tert-Butyl Ether - Methanol System," *J. Chem. Eng. Data*, **25**, 100 (1980).
- Arce, A., Ageitos, J. M. and Soto, A., "VLE Measurements of Binary Mixtures of Methanol, Ethanol, 2-Methoxy-2-Methylpropane, and 2-Methoxy-2-methylbutane at 101.325 kPa," *J. Chem. Eng. Data*, **41**, 718 (1996).
- Herington, E. F. G., "Tests for Consistency of Experimental Isobaric Vapor Liquid Equilibrium Data," *J. Inst. Petrol.*, **37**, 457 (1951).
- Hiaki, T., Tatsuhami, K., Tsuji, T. and Hongo, M., "Isobaric Vapor-Liquid Equilibria for 2-Methoxy-2-methylpropane+Ethanol+Octane and Constituent Binary Systems at 101.3 kPa," *J. Chem. Eng. Data*, **44**, 323 (1999).
- Komatsu, H., Nakamura, M., Yamashita, Y. and Hirai, C., "Vapor-Liquid Equilibrium Data for Five Binary Systems of Methanol, tert-Butylalcohol, tert-Butylmethylether and Water, and Quaternary Reactive System Producing tert-Butylmethylether from Methanol and tert-Butylalcohol," *Kagaku Kogaku Ronbunshu*, **23**, 983 (1997).
- Loras, S., Aucejo, A., Munoz, R. and Wisniak, J., "Azeotropic Behavior in the System Methanol+Methyl 1,1-Dimethylethyl Ether," *J. Chem. Eng. Data*, **44**, 203 (1999).
- Miyamoto, S., Nakamura, S., Iwai, Y. and Arai, Y., "Measurement of Isothermal Vapor-Liquid Equilibria for Monocarboxylic Acid+Monocarboxylic Acid Binary Systems with a Flow Type Apparatus," *J. Chem. Eng. Data*, **46**, 405 (2001).
- Tochigi, K., Tiegs, D., Gmehling, J. and Kojima, K., "Determination of New ASOG Parameters," *J. Chem. Eng. Jpn.*, **23**, 453 (1990).
- Toghiani, R. K., Toghiani, H. and Venkateswarlu, G., "Vapor-Liquid Equilibria for Methyl tert-Butyl Ether+Methanol and tert-Amyl Methyl Ether+Methanol," *Fluid Phase Equilibria*, **122**, 157 (1996).
- Van Ness, H. C., Byer, S. M. and Gibbs, R. E., "Vapor-Liquid Equilibrium: Part I. An Appraisal of Data Reduction Methods," *AIChE J.*, **19**, 238 (1973).
- Watanabe, T., "Measurement of Vapor-Liquid Equilibria under Low Pressure and Examination of Thermodynamic Consistency," *Memoirs of Ariake Coll. Tech.*, **21**, 59 (1985).
- Wilson, G. M., "Vapor-Liquid Equilibrium. XI. A New Expression for the Excess Free Energy of Mixing," *J. Am. Chem. Soc.*, **86**, 127 (1964).
- Wisniak, J., Magen, E., Shacher, M., Zeroni, I., Reich, R. and Segura, H., "Isobaric Vapor-Liquid Equilibria in the Systems Methyl 1,1-Dimethyl Ether+Hexane and +Heptane," *J. Chem. Eng. Data*, **42**, 243 (1997a).
- Wisniak, J., Embon, G., Shafir, R., Segura, H. and Reich, R., "Isobaric Vapor-Liquid Equilibria in the Systems 2-Methoxy-2-methylpropane +Octane and Heptane+Octane," *J. Chem. Eng. Data*, **42**, 1191 (1997b).