

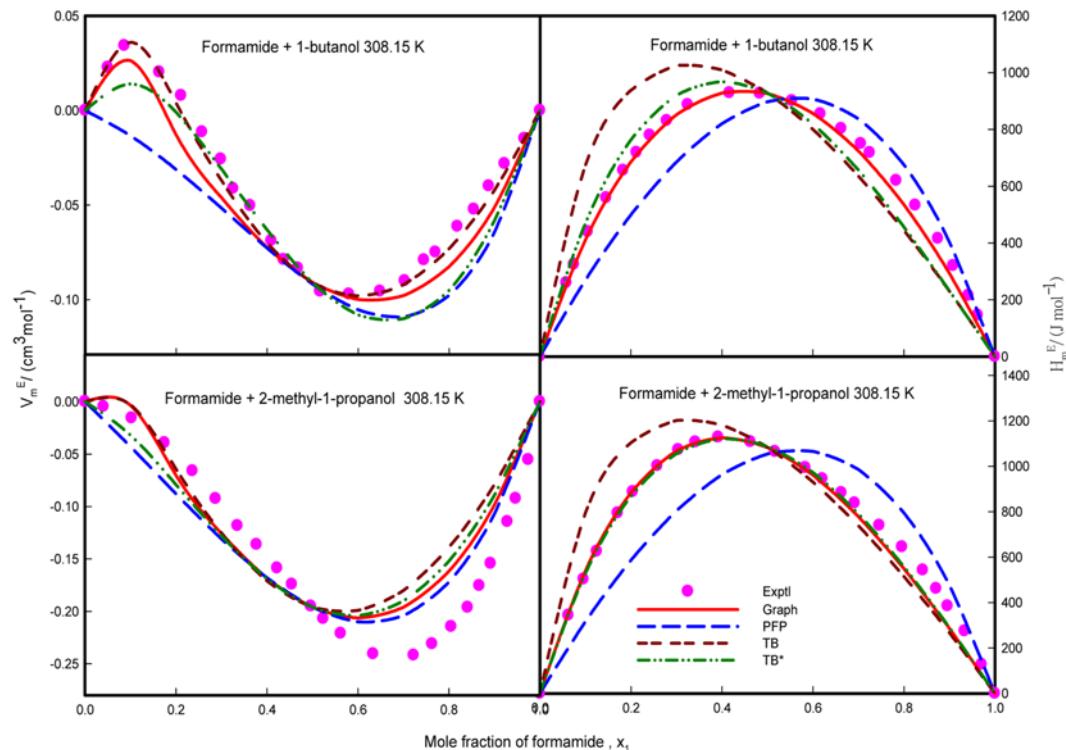
## Thermodynamics of molecular interactions in binary mixtures containing associated liquids

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**Abstract**—Experimentally measured data of excess molar volumes and enthalpies at 308.15 K for binary mixtures of formamide with 1-butanol or 2-methyl-1-propanol were fitted to the Redlich-Kister polynomial equation. Thermodynamics of molecular interaction in these mixtures was discussed using Prigogine-Flory-Patterson theory, Treszczanowicz-Benson association model and Graph theoretical approach. Extent of inter-molecular H-bonding in formamide and butanol in their binary mixtures was also reflected in their molar enthalpy of association of H-bonding  $\Delta h_H^0$  and association constant  $K_H$  calculated from Treszczanowicz-Benson association model. All the three theories predict the excess property data reasonably well.



Key words: Excess Molar Enthalpy, Excess Molar Volume, Prigogine-Flory-Patterson Theory, Treszczanowicz-Benson Association Model, Graph Theoretical Approach

### INTRODUCTION

Formamide is the simplest amide that contains a peptide linkage which combines amino acids into polypeptide to form the building block of proteins. Addition of alkanol to amide may result in the intermolecular H-bonding [1-3]. Thus the thermo-physical properties

of binary mixtures of amide and alkanol would be of great importance in chemical designing and also for researchers to understand the nature of intermolecular interactions [3,4].

Addition of inert solvents like alkane to the self associated alkanol leads to pronounced thermodynamic non-ideal behavior [5-12]. Any excess thermodynamic property  $X_m^E$  for such binary systems may be considered to consist of two parts, one resulting from breaking up of the hydrogen bonded network and other due to van der Waals type interaction between the alkyl chain of alkanol and alkane [13].

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In our previous publications, we described the thermodynamics of alkanol+aromatic hydrocarbon in terms of Treszczanowicz-Benson (TB) association model [14-16]. Many researchers have interpreted binary systems containing one associated component [9,17-27], whereas systems containing both components of associated nature are relatively less [9,28-35] in literature. These considerations prompted us to study the thermodynamics of systems with formamide and butanol. In this paper, we report the excess molar enthalpies ( $H_m^E$ ) and excess molar volumes ( $V_m^E$ ) at 308.15 K for formamide (1)+1-butanol or 2-methyl-1-propanol (2) mixtures. The measured  $H_m^E$  and  $V_m^E$  data were also interpreted in terms of Prigogine-Flory-Patterson (PFP) model [36-42], Treszczanowicz-Benson (TB) association model [5,6] and Graph theoretical approach [43,44].

## EXPERIMENTAL SECTION

The methods of purification of formamide, 1-butanol and 2-methyl-1-propanol (Sigma-Aldrich) and their analysis to check purities were described in our previous publication [35,45,46]. Their purities were found to be better than 99.7 wt% when analyzed by gas chromatography.

Excess molar enthalpy of mixing ( $H_m^E$ ) data at 308.15 for the binary mixtures was measured using flow micro calorimeter (LKB-2107, Bromma, Sweden) in the manner described by Monk and Wadso [47]. Details and the operating procedure of the calorimeter were described elsewhere [48,49]. The uncertainty in the measured  $H_m^E$

values was  $\pm 1\%$ .

Excess molar volumes ( $V_m^E$ ), at 308.15 K for the binary mixtures, were measured by V-shaped dilatometer in the manner described elsewhere [50]. The uncertainty in the measured  $V_m^E$  values was  $\pm 1\%$ .

## RESULTS

The measured  $X_m^E$  ( $X=V$  or  $H$ ) data, which are recorded in Table 1, were fitted to the following Redlich and Kister equation:

$$X_m^E = x_1 x_2 \left[ \sum_{n=0}^3 X^{(n)} (x_1 - x_2)^n \right] \quad (1)$$

where  $X^{(n)}$  ( $X=V$  or  $H$ ) are the adjustable parameters, and  $x_1$  and  $x_2$  are the mole fractions of formamide (1) and butanol (2) in mixture. These parameters were evaluated by fitting  $X_m^E$  data to Eq. (1) by least squares method and recorded in Table 2 along with the standard deviations of  $X_m^E$ , ( $\sigma(X_m^E)$ ) [35].

## DISCUSSION

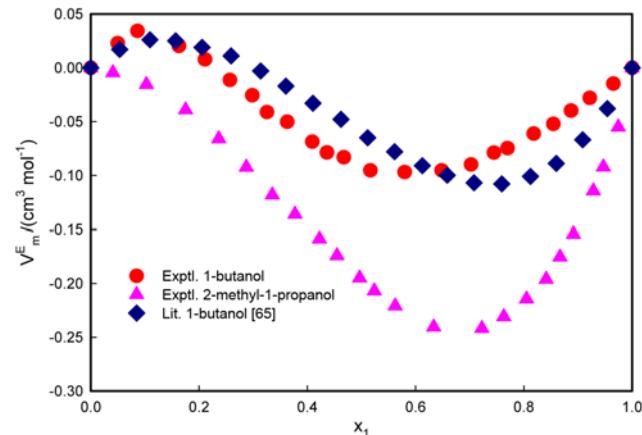
The  $V_m^E$  data for formamide+1-butanol were reported at 308.15 K [58]. A comparison of present data with reported values is shown in Fig. 1. Our  $V_m^E$  values are somewhat lower than those reported for the mole fraction ( $0.2 < x_1 < 0.7$ ) but little higher thereafter ( $x_1 >$

**Table 1. Measured excess molar volumes,  $V_m^E$ , and excess molar enthalpies,  $H_m^E$ , data for (1+2) binary mixtures as functions of mole fractions of formamide,  $x_1$ , at 308.15 K**

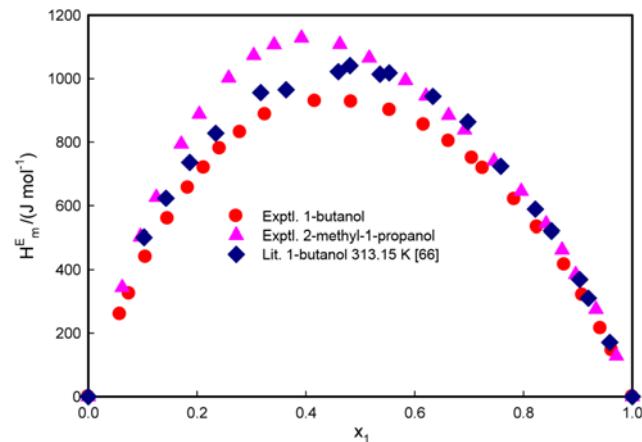
$x_1$	$V_m^E$ ( $\text{cm}^3 \text{mol}^{-1}$ )	$x_1$	$V_m^E$ ( $\text{cm}^3 \text{mol}^{-1}$ )	$x_1$	$H_m^E$ ( $\text{J mol}^{-1}$ )	$x_1$	$H_m^E$ ( $\text{J mol}^{-1}$ )
Formamide (1)+1-butanol (2)							
0.0499	0.023	0.5166	-0.095	0.0582	260	0.5540	901
0.0862	0.034	0.5799	-0.097	0.0750	325	0.6166	855
0.1629	0.020	0.6482	-0.095	0.1052	440	0.6624	803
0.2111	0.008	0.7025	-0.090	0.1458	559	0.7054	750
0.2571	-0.011	0.7446	-0.079	0.1832	656	0.7250	718
0.2983	-0.026	0.7699	-0.075	0.2124	719	0.7832	620
0.3254	-0.041	0.8183	-0.061	0.2416	780	0.8250	533
0.3629	-0.050	0.8544	-0.052	0.2790	831	0.8750	416
0.4092	-0.069	0.8873	-0.040	0.3250	887	0.9082	320
0.4363	-0.079	0.9218	-0.028	0.4166	929	0.9416	215
0.4675	-0.083	0.9654	-0.015	0.4832	927	0.9624	146
Formamide (1)+2-methyl-1-propanol (2)							
0.0408	-0.005	0.5622	-0.221	0.0624	344	0.5832	994
0.1027	-0.016	0.6334	-0.241	0.0958	503	0.6208	945
0.1751	-0.039	0.7224	-0.242	0.1250	626	0.6624	884
0.2364	-0.066	0.7631	-0.231	0.1708	794	0.6916	838
0.2873	-0.093	0.8051	-0.215	0.2040	888	0.7458	740
0.3353	-0.118	0.8412	-0.196	0.2580	1002	0.7958	645
0.3772	-0.136	0.8669	-0.176	0.3040	1073	0.8416	543
0.4225	-0.159	0.8917	-0.154	0.3416	1107	0.8708	462
0.4548	-0.174	0.9285	-0.114	0.3918	1128	0.8958	385
0.4967	-0.195	0.9469	-0.092	0.4624	1108	0.9332	275
0.5238	-0.207	0.9745	-0.055	0.5166	1065	0.9708	128

**Table 2.** Values of adjustable parameters,  $X^{(n)}$ , of Redlich-Kister equation along with standard deviation,  $\sigma(X_m^E)$ , (where X=V or H) of the molar excess volumes or enthalpy for the various (1+2) binary mixtures at 308.15 K

System	Property	$X^{(0)}$	$X^{(1)}$	$X^{(2)}$	$X^{(3)}$	$\sigma(X_m^E)$
Formamide (1)+1-butanol (2)	$V_m^E$	-0.3634	-0.3247	0.5270	-0.2283	0.0018
	$H_m^E$	3705.6	-642.0	837.6	216.5	2.728
Formamide (1)+2-methyl-1-propanol (2)	$V_m^E$	-0.7840	-0.8365	-0.1702	-0.1297	0.0030
	$H_m^E$	4330.1	-1618.2	1070.8	979.3	3.010

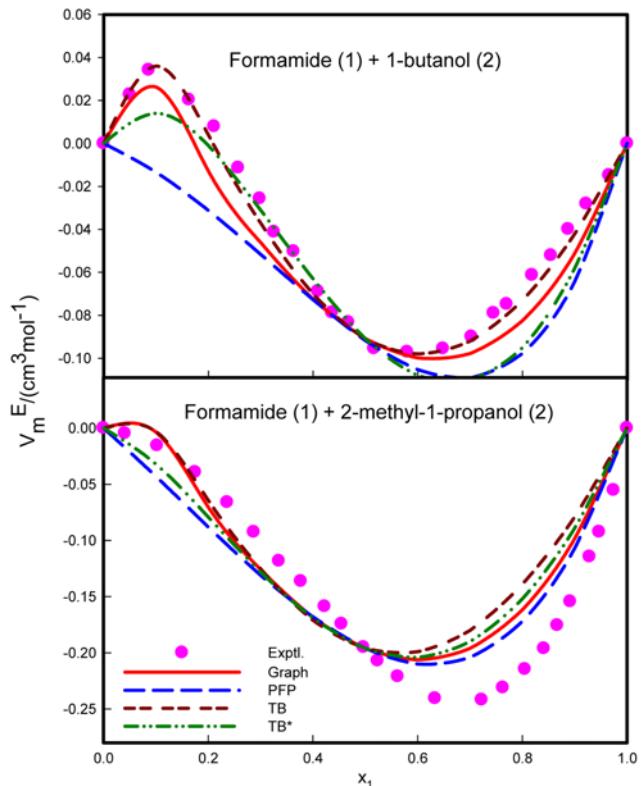


**Fig. 1.** Measured excess molar volumes ( $V_m^E$ ) of formamide (1)+ alkanol (2) as function of mole fraction of formamide ( $x_1$ ) at 308.15 K.



**Fig. 2.** Measured excess molar enthalpies ( $H_m^E$ ) of formamide (1)+ alkanol (2) as function of mole fraction of formamide ( $x_1$ ) at 308.15 K.

0.7). The  $H_m^E$  data for these systems were reported for formamide+1-butanol at 313.15 K by Pikkarainen [51] and compared with present  $H_m^E$  data in Fig. 2. The  $H_m^E$  values were lower than those reported by Pikkarainen [51], and that might be due to our lower experimental temperature. The  $V_m^E$  values for formamide+butanol systems are negative over the whole composition range (Fig. 3) and the  $H_m^E$  values are positive for these systems (Fig. 4). At the simplest qualitative level, the observed  $X_m^E$  ( $X=V$  or  $H$ ) values may be attributed to the resultant of two opposing effects/contributions. The positive contribution arises from the breaking of intermolecular hydrogen bonding in self associated pure components, physical dipole-

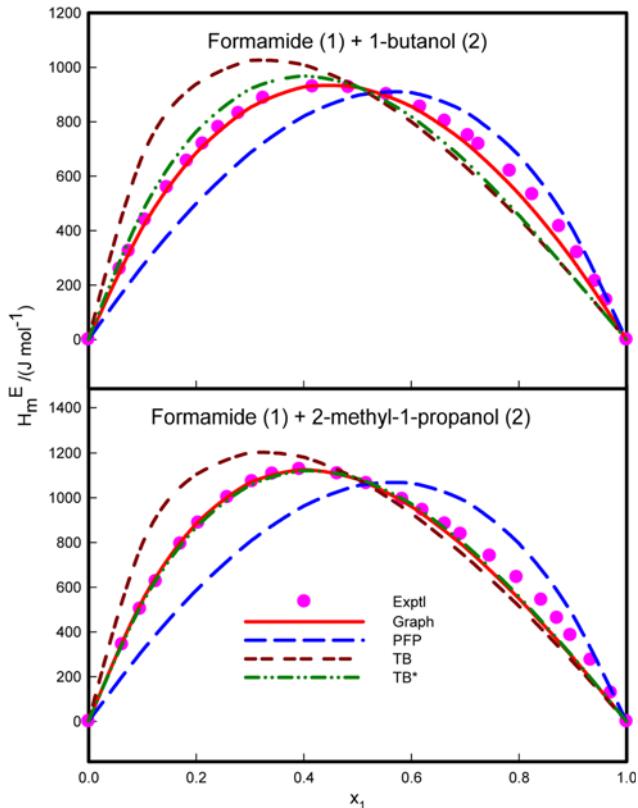


**Fig. 3.** Excess molar volume ( $V_m^E$ ) of formamide (1)+alkanol (2) as function of mole fraction of formamide ( $x_1$ ) at 308.15 K.

dipole interactions between monomers and multimers, and also due to disruption in favorable orientation order of pure components; the negative contribution is due to the formation of hydrogen bonded interactions between formamide and butanol. At higher temperature the positive contribution decreases due to weakening of self association/interaction in pure components, and negative contribution also decreases owing to lesser interaction in unlike molecules. The higher value of  $H_m^E$  (Fig. 2) at higher temperature indicates that the decrease in negative contribution outweighs the decrease in positive contribution. Similar effect of temperature was also observed for formamide+propanol mixtures [45]. The measured  $V_m^E$  and  $H_m^E$  data were next analyzed in terms of PFP theory, TB association model and Graph theoretical approach.

### 1. Prigogine-flory-patterson Theory

According to PFP theory [39], excess molar volume ( $V_m^E$ ) is the result of three contributions: (i) due to interaction between unlike molecules that is proportional to interaction parameter ( $\chi_{12}^*$ ), (ii) the free volume contribution owing to the dependence of reduced volume upon reduced temperature due to the difference between the



**Fig. 4.** Excess molar enthalpies ( $H_m^E$ ) of formamide (1)+alkanol (2) as function of mole fraction of formamide ( $x_1$ ) at 308.15 K.

degree of expansion of the components, and (iii) the  $P^*$  contribution that depends on the difference of internal pressures as well as the difference of reduced volumes of the components. Similarly, excess molar enthalpy is expressed as the sum of only two contributions: interactional contribution, and free volume contribution. Thus  $V_m^E$  and  $H_m^E$  may be expressed as

$$V_m^E = V_{\text{free vol}}^E + V_p^E \quad (2)$$

$$\begin{aligned} \frac{V_m^E}{x_1 V_1^* + x_2 V_2^*} &= \frac{(\tilde{V}^{1/3} - 1)\tilde{V}^{2/3}\psi_1\theta_2(\chi_{12}^*/P_1^*)}{((4/3)\tilde{V}^{-1/3} - 1)} \\ &\quad - \frac{(\tilde{V}_1 - \tilde{V}_2)^2((14/9)\tilde{V}^{-1/3} - 1)\psi_1\psi_2}{((4/3)\tilde{V}^{-1/3} - 1)\tilde{V}} \\ &\quad + \frac{(\tilde{V}_1 - \tilde{V}_2)(P_1^* - P_2^*)\psi_1\psi_2}{P_2^*\psi_1 + P_2^*\psi_2} \end{aligned} \quad (3)$$

$$H_m^E = H_{\text{free vol}}^E + H_{\text{inter}}^E \quad (4)$$

$$H_m^E = (x_1 U_1^* + x_2 U_2^*)[-\tilde{U}(\tilde{T}) + \tilde{T}\tilde{C}_p(\tilde{T})]\chi_{12}\psi_1\theta_2/P_1^*$$

$$+ (x_1 U_1^* + x_2 U_2^*)\tilde{C}_p(\tilde{T})(\psi_1\tilde{T}_1 + \psi_2\tilde{T}_2 - \tilde{T}) \quad (5)$$

where all the terms have their usual meanings [36,37]. The characteristic pressure, volume and temperature ( $P_i^*$ ,  $V_i^*$  and  $T_i^*$ ) of the pure components are reported in Table 3. Calculation of  $V_m^E$  and  $H_m^E$  from Eq. (2) and Eq. (4) requires the knowledge of Flory interaction parameters  $\chi_{12}^*$  (for excess volume) and  $\chi_{12}$  (for excess enthalpy). These interaction parameters were computed employing equimolar experimental data of  $V_m^E$  and  $H_m^E$  and were subsequently used to calculate  $V_m^E$  and  $H_m^E$  at other mole fraction ( $x_i$ ). The calculated  $V_m^E$  and  $H_m^E$  values are recorded in Table 4, respectively. The calculated values of various contributions to the values of  $V_m^E$  and  $H_m^E$  for equimolar mixture, Flory interaction parameters  $\chi_{12}^*$  (for excess volumes) and  $\chi_{12}$  (for excess enthalpies) are recorded in Table 5. Calculated  $V_m^E$  values were found to agree well with respective experimental data as shown in Fig. 3. But the comparison between calculated and experimental  $H_m^E$  values is reasonably good for  $x_i > 0.5$  (Fig. 4) and for  $x_i < 0.5$  the calculated  $H_m^E$  values are less (at the most 150 J mol<sup>-1</sup> at  $x_i = 0.3$ ) than corresponding experimental data (Fig. 4). In these binary mixtures,  $P_1^* > P_2^*$  and  $\tilde{V}_1 < \tilde{V}_2$  results in the large negative contribution of  $V_p^E$  which determines the sign of excess molar volume [52]. The larger  $P^*$  and  $\tilde{V}$  smaller values of formamide as compared to butanol lead to negative value of  $V_m^E$  as well as positive  $H_m^E$ . The branching of alkyl chain in butanol further decreases the  $P_2^*$  and increases the  $\tilde{V}_2$ . This further increases the negative contribution of  $V_p^E$  term as well as dominant  $H_{\text{inter}}^E$  (Table 5), thus making  $V_m^E$  more negative and  $H_m^E$  more positive (Fig. 3 and 4).

## 2. Treszczanowicz and Benson Association Model

Treszczanowicz-Benson association model [5] was proposed for alkane (1)+alkanol (2) mixtures, and it assumes that the mode of self association of alkanol is of Mecke-Kempter type in which linear multimers A are formed due to the consecutive association reaction,



The consecutive thermodynamic association constant  $K_{i,i-1}$  can be expressed in terms of the association parameters for standard enthalpy  $\Delta h_{i,i-1}^0$  and entropy  $\Delta s_{i,i-1}^0$  of H-bond formation. In TB association model, these parameters are taken to be independent of the degree of association i. Kehiaian [53] observed that standard entropy of H-bond formation  $\Delta s_{i,i-1}^0$  for alkanol depends on the number of segment  $r_2$  in a molecule of monomer. Thus, for an alkanol

$$\Delta h_{i,i-1}^0 = \Delta h_H^0 \quad (7)$$

$$\Delta s_{i,i-1}^0 = \Delta s_H^0 - R \ln r_2 \quad (8)$$

These assumptions indicate that

$$K_{i,i-1} = \frac{K_H}{r_2} \quad (9)$$

**Table 3.** Molar volume, V, isobaric expansivity,  $\alpha$ , and isothermal compressibility,  $\kappa_T$ , characteristic pressure,  $P^*$ , characteristic molar volume,  $V^*$ , and characteristic temperature,  $T^*$ , obtained from Flory theory for the pure liquids at 308.15 K

Compound	V (cm <sup>3</sup> mol <sup>-1</sup> )	$10^3 \times \alpha$ (K <sup>-1</sup> )	$10^6 \times \kappa_T$ (cm <sup>3</sup> J <sup>-1</sup> )	P* (J cm <sup>-3</sup> )	V* (cm <sup>3</sup> mol <sup>-1</sup> )	T* (K)
Formamide	40.20	0.758	417	808.69	33.46	6236.52
1-Butanol	92.88	1.041	1004	509.72	73.53	5196.82
2-Methyl-1-propanol	93.76	1.066	1116	473.41	73.93	5132.24

**Table 4.** Comparison of excess property,  $X_m^E$ , ( $X=V$  or  $H$ ) calculated from Prigogine-Flory-Patterson theory and Treszczanowicz-Benson association model with their corresponding experimental values (calculated from Eq. (1) at round mole fractions) for the binary mixtures as functions of mole fraction of formamide,  $x_1$ , at 308.15 K. TB and TB\* represent the values of  $X_m^E$  when either butanol or formamide was assumed to be associated, respectively

$V_m^E$ (cm <sup>3</sup> mol <sup>-1</sup> )					$H_m^E$ (J mol <sup>-1</sup> )				
Exptl	PFP	TB	TB*	Graph	Exptl	PFP	TB	TB*	Graph
Formamide (1)+1-butanol (2)									
0.1	0.032	-0.009	0.036	0.014	0.026	418	269	673	469
0.2	0.011	-0.026	0.004	-0.001	-0.013	695	499	938	763
0.3	-0.028	-0.047	-0.037	-0.031	-0.046	857	685	1025	920
0.4	-0.066	-0.069	-0.070	-0.063	-0.072	928	820	1009	968
0.5	-0.091	-0.091	-0.091	-0.091	-0.091	926	897	928	928
0.6	-0.098	-0.107	-0.098	-0.108	-0.100	867	907	800	819
0.7	-0.089	-0.112	-0.092	-0.110	-0.098	755	837	636	657
0.8	-0.067	-0.102	-0.073	-0.095	-0.082	587	676	445	457
0.9	-0.036	-0.067	-0.042	-0.058	-0.051	346	404	231	293
Formamide (1)+2-methyl-1-propanol (2)									
0.1	-0.014	-0.043	-0.003	-0.032	-0.003	523	316	794	529
0.2	-0.050	-0.088	-0.064	-0.079	-0.070	876	586	1104	868
0.3	-0.098	-0.131	-0.125	-0.128	-0.126	1068	804	1202	1056
0.4	-0.149	-0.168	-0.171	-0.169	-0.168	1125	963	1181	1121
0.5	-0.196	-0.196	-0.196	-0.196	-0.196	1083	1054	1083	1083
0.6	-0.230	-0.210	-0.199	-0.204	-0.206	974	1065	930	972
0.7	-0.242	-0.204	-0.180	-0.190	-0.196	823	985	738	790
0.8	-0.220	-0.172	-0.139	-0.152	-0.162	633	795	515	558
0.9	-0.147	-0.107	-0.079	-0.089	-0.098	380	476	267	290

**Table 5.** PFP interaction parameters  $\chi_{12}^*$ ,  $\chi_{12}$  and equimolar values of the contributions to excess volume and excess enthalpy at 308.15 K

System	$V_{Inter}^E$	$V_{Free\ vol}^E$	$V_{P^*}^E$	$\chi_{12}^*$	$H_{Inter}^E$	$H_{free\ vol}^E$	$\chi_{12}$
Formamide (1)+1-butanol (2)	0.334	-0.074	-0.351	54.65	926.40	-29.51	84.93
Formamide (1)+2-methyl-1-propanol (2)	0.337	-0.088	-0.445	52.29	1082.54	-33.48	99.04

where

$$K_H = \exp\left[\frac{-(\Delta h_H^0 - T\Delta s_H^0)}{RT}\right] \quad (10)$$

is a constant for a homologous series of self-associating components. The number of segments in an alkanol molecule was calculated from the relation,

$$r_2 = \frac{V_2^*}{17.12} \quad (11)$$

where  $V_2^*$  is the characteristic molar volume of the alkanol and 17.12 cm<sup>3</sup>mol<sup>-1</sup> is the van der Waals molar volume for methane [54].

This model was developed for alkane+alkanol mixtures where the alkane behaves as an inert solvent [5]. It assumes that the  $X_m^E$  ( $X=V$  or  $H$ ) are composed of a chemical contribution (Mecke-Kemper type of association of alkanol) term and a physical contribution described by Flory theory [36,37]:

$$H_m^E = H_{MK}^E + H_F^E \quad (12)$$

$$V_m^E = V_{MK}^E + V_F^E \quad (13)$$

The chemical contribution is given by

$$H_{MK}^E = \Delta h_H^0 x_2 h(K^\phi, \phi_2) \quad (14)$$

$$V_{MK}^E = \Delta v_H^0 x_2 h(K^\phi, \phi_2) \quad (15)$$

where

$$h(K^\phi, \phi_2) = \frac{[\phi_2 \ln(1+K^\phi) - \ln(1+K^\phi \phi_2)]}{K^\phi \phi_2} \quad (16)$$

$$\ln K^\phi = 1 + \ln(K_H/r_2) \quad (17)$$

In these equations R is the gas constant, T is the temperature and  $K^\phi$  is the volume fraction based association constant and  $x_2$  and  $V_2^*$  are mole fraction and hard core molar volume of associating component.  $\Delta v_H^0$ ,  $\Delta h_H^0$  and  $\Delta s_H^0$  are the standard volume, enthalpy and entropy of association of alkanol.

The physical contribution is obtained from Flory theory [36,37], which contains the effect of nonspecific interaction between the real molecular species in the mixture, together with the free volume term. According to Flory theory [36,37]

$$H_F^E = x_2 \theta_1 \left(\frac{V_2^*}{V}\right) \chi_{12} + \sum_{i=1}^2 [x_i P_i^* V_i^* (\tilde{V}_i^{-1} - \tilde{V}^{-1})] \quad (18)$$

$$V_F^E = V^* [\tilde{V} - (\tilde{V}_1 \phi_1 + \tilde{V}_2 \phi_2)] \quad (19)$$

where  $\chi_{12}$  is Flory's interaction parameter,  $V^* = x_1 V_1^* + x_2 V_2^*$  is the characteristic molar volume for the mixture,  $\alpha$  and  $\kappa_T$  are the isobaric expansivity and isothermal compressibility of pure components and were taken from literature [55-57] and recorded in Table 3.

The association parameters ( $\Delta V_H^0$ ,  $\Delta H_H^0$  and  $\Delta S_H^0$ ) for butanol in these mixtures were calculated as suggested elsewhere [58]. As the experimental  $C_p^E$  values for these mixtures were not available in literature,  $C_p^E$  data (0.925 J mol<sup>-1</sup> K<sup>-1</sup>) for an equimolar mixture of dimethylformamide+ethanol at 298.15 K reported by Conti et al. [59] was used for the calculation of association parameters for the present binary systems at 308.15 K. The most suitable value for  $\Delta V_H^0$  that predicts  $V_m^E$  data close to experimental is -5 cm<sup>3</sup> mol<sup>-1</sup>. The same value was also reported by Liu et al. [60], though Treszczanowicz and Benson [5] and Stoke [61] calculated -10 and -7.5 cm<sup>3</sup> mol<sup>-1</sup> for alkane+alkanol mixtures. The values of association parameters ( $\Delta V_H^0$ ,  $\Delta H_H^0$  and  $\Delta S_H^0$ ), association constants,  $K_H$  and  $K^\phi$ , and Flory interaction parameter  $\chi_{12}$  for the present binary systems, when butanol is assumed to be associated, are recorded in Table 6. It has been observed from Fig. 3 and Fig. 4 that calculated and experimental  $V_m^E$  and  $H_m^E$  values are in good agreement for these systems. The agreement would have been much better if the exact experimental values of  $C_p^E$  for all these systems were known. This model was again applied on these systems by assuming that formamide is associated and association parameters ( $\Delta V_H^0$ ,  $\Delta H_H^0$  and  $\Delta S_H^0$ ),  $K_H$  and  $K^\phi$ , and Flory interaction parameter  $\chi_{12}$  were again calculated by the same procedure and reported in Table 6 as TB\*. The calculated  $V_m^E$  and  $H_m^E$ , when formamide was assumed to be associated, were reported in Table 4 and plotted in Fig. 3 and Fig. 4 as TB\*. It can be seen from the Fig. 3 and Fig. 4 that the comparison between calculated and experimental  $V_m^E$  and  $H_m^E$  values was better when formamide was assumed to be associated. Since inter-molecular H-bonding in formamide is weaker than butanol, enthalpy of association of H-bonding  $\Delta H_H^0$  and association constant  $K_H$  should also be less in formamide than butanol in these systems. This is indeed true in our case as evident from Table 6. The same was also observed by Funke et al. [9].

### 3. Graph Theoretical Approach

According to this theory  $V_m^E$  may be expressed by [43].

$$V_m^E = \alpha_{12} \left[ \sum_{i=1}^2 [x_i (\xi_i)^m]^{-1} - \sum_{i=1}^2 \frac{x_i}{\xi_i} \right] \quad (20)$$

**Table 6.** Values of association parameters,  $\Delta H_H^0$ ,  $\Delta S_H^0$  and  $\Delta V_H^0$ , association constants,  $K_H$  and  $K^\phi$ , of Treszczanowicz-Benson (TB) association model and Flory interaction parameter,  $\chi_{12}$ , for the binary systems at 308.15 K. TB and TB\* represent the values of parameters when either butanol or formamide is assumed to be associated, respectively

System		$\Delta H_H^0$ (J mol <sup>-1</sup> )	$\Delta S_H^0$ (J K <sup>-1</sup> mol <sup>-1</sup> )	$\Delta V_H^0$ (cm <sup>3</sup> mol <sup>-1</sup> )	$K_H$	$K^\phi$	$\chi_{12}$
Formamide (1)+1-butanol (2)	TB	-17513	-43.56	-5	4.93	3.12	16.74
	TB*	-11865	-28.51	-5	3.32	4.62	-47.06
Formamide (1)+2-methyl-1-propanol (2)	TB	-21562	-57.15	-5	4.67	2.94	16.30
	TB*	-12895	-32.05	-5	3.25	4.52	-44.42

**Table 7.** Value of parameters involved in graph theoretical approach

System	$\xi_1$	$\xi_2$	$(\xi_i)_m$	$(\xi_i)_m$	$\alpha_{12}$	$\chi_{12}$	$\chi^*$
Formamide (1)+1-butanol (2)	0.8	1.49	0.8	1.4	1.7269	2453.42	2341.43
Formamide (1)+2-methyl-1-propanol (2)	0.8	1.4	0.8	1.36	3.4865	3277.89	718.93

where  $\alpha_{12}$  is the constant characteristic of the (1+2) mixture and can be evaluated using equimolar experimental  $V_m^E$  value ( $\xi_i$ ) and ( $\xi_i)_m$  and (i=1 or 2) are the connectivity parameter of third order in pure state and in mixtures. These  $\xi$  parameters were evaluated by fitting experimental  $V_m^E$  data to Eq. (20). Only those values of ( $\xi_i$ ) and ( $\xi_i)_m$  were retained that best reproduced the  $V_m^E$  data. The values of or (i=1 or 2) parameters are recorded in Table 7 and their significance was discussed elsewhere [35]. The  $V_m^E$  values obtained from Eq. (20) for the various binary mixtures as a function of  $x_1$  are recorded in Table 5 and found to compare well with experimental data (Fig. 3).

To understand the energetics of the various interactions present in these binary formamide (1)+alkanol (2) mixtures, it is assumed that the process of mixtures formation requires:

a) mixing of (1) with (2) to establish (1)-(2) contacts with an interaction energy  $\chi_{12}^*$  per mole of (1)-(2) contacts

b) these (1)-(2) contacts between formamide and butanol would then cause rupture of

(i) intermolecular association in formamide to yield monomers of formamide with an interactional energy  $\chi_{11}$  per mole

(ii) intermolecular association in butanol to yield monomers of butanol with an interactional energy  $\chi_{22}$  per mole

c) the monomers of formamide then interact with butanol to give 1-2 molecular entity with an interaction energy  $\chi_{12}$  per mole

The change in enthalpy due to processes (a), (b)(i), (b)(ii) and (c) would then be expressed [49,62-64] by

$$\Delta H_a = x_1 \chi_{12}^* S_2 \quad (21)$$

where  $S_2$  is the surface fraction of butanol involved in (1)-(2) contact and is defined [62,63] by:

$$S_2 = \frac{x_2 V_2}{\sum x_i V_i} \quad (22)$$

Similarly enthalpy changes due to processes (b) and (c) would be given by:

$$\Delta H_{b(i)} = x_1 \chi_{11} S'_2 \quad (23)$$

$$\Delta H_{b(ii)} = x_1 \chi_{22} S'_2 \quad (24)$$

where  $S'_2$  is the surface fraction of butanol that brings about changes in formamide and, following our earlier work has been expressed by

$$S'_2 \propto x_1 S_2 = \frac{K x_1 x_2 V_2}{\sum x_i V_i} \quad (25)$$

and

$$\Delta H_e = x_2 \chi_{12} S'_2 \quad (26)$$

The total enthalpy change due to processes (a), (b) and (c) is given by:

$$H_m^E = \left[ \frac{x_1 x_2 V_2}{\sum x_i V_i} \right] [\chi_{12}^* + K x_1 \chi_{11} + K x_1 \chi_{22} + K x_2 \chi_{12}] \quad (27)$$

$$H_m^E = \left[ \frac{x_1 x_2 (\chi_{12}^* / \chi_{12})}{x_1 + x_2 (\chi_{12}^* / \chi_{12})} \right] [\chi_{12}^* + K x_1 \chi_{11} + K x_1 \chi_{22} + K x_2 \chi_{12}] \quad (28)$$

For these mixtures, it would be reasonable to assume that  $\chi_{12}^* = K \chi_{12}$  and  $K \chi_{22} = K \chi_{11} = \chi^*$ , then Eq. (12) reduces to

$$H_m^E = \left[ \frac{x_1 x_2 (\chi_{12}^* / \chi_{12})}{x_1 + x_2 (\chi_{12}^* / \chi_{12})} \right] [(1 + \chi_2) \chi_{12}^* + \chi_1 \chi^*] \quad (29)$$

Calculation of  $H_m^E$  from Eq. (13) requires the knowledge of two unknown interaction parameters  $\chi_{12}^*$  and  $\chi^*$ . These parameters are calculated using  $H_m^E$  data at two compositions ( $x_i = 0.4$  and 0.5) for various binary mixtures, and were subsequently used to evaluate  $H_m^E$  at other mole fraction ( $x_i$ ). Such values of  $H_m^E$  along with parameters  $\chi_{12}^*$  and  $\chi^*$  are recorded in Table 6 along with previously reported  $(\chi_{12}^*)$  values [49]. The calculated  $H_m^E$  were found to compare well with their corresponding experimental values (Fig. 4). This gives additional support to the assumptions made in derivation of Eq. (29).

## CONCLUSION

The thermodynamics of binary mixtures of formamide (1)+1-butanol or 2-methyl-1-propanol (2) was discussed in terms of Prigogine-Flory-Patterson theory, Treszczanowicz-Benson association model and Graph theoretical approach. Measured excess molar enthalpies ( $H_m^E$ ) and volumes ( $V_m^E$ ) data of these mixtures were predicted reasonably well using these models. The Mecke-Kemper type TB association model was developed for binary alkane+alkanol systems having one associated component. For the first time, this TB association model was applied to systems containing both the components associated through H-bonding by considering either of them to be associated at a time. In both cases, when either formamide or butanol was assumed to be associated, the calculated  $H_m^E$  and  $V_m^E$  values compared reasonably well with corresponding experimental data. The extent of inter-molecular H-bonding in formamide and butanol in their binary mixtures was reflected in their molar association of H-bonding  $\Delta h^0$  and association constant  $K_h$ .

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## LIST OF SYMBOLS

$C_p^E$	: molar excess isobaric heat capacity
$\Delta H_a$ , $\Delta H_{b(i)}$ , $\Delta H_{b(ii)}$ , $\Delta H_c$	: enthalpy of processes in graph theory
$\Delta h_H^0$	: standard enthalpy of association
$K$	: volume fraction based association constant
$n$	: number of adjustable parameters in Eq. (1)
$P$	: pressure
$P_i^*$	: characteristic pressure
$\tilde{P}_i$	: reduced pressure
$P^*$	: characteristic pressure of mixture
$r_1$	: number of segment in a molecule of monomer
$R$	: gas constant
$\Delta s_H^0$	: standard entropy of association
$S_i$	: contact sites per segment
$S_2$	: surface fraction of butanol involved in (1)-(2) contact
$S'_2$	: surface fraction of butanol (2) that brings about changes in formamide (1)
$T$	: temperature
$T_i^*$	: characteristic temperature
$T^*$	: characteristic temperature of mixture
$\tilde{T}_i$	: reduced temperature
$\tilde{T}$	: reduced temperature of mixture
$U_i^*$	: characteristic configurational energy
$\tilde{U}_i$	: reduced configurational energy
$\tilde{U}(\tilde{T})$	: reduced configurational energy of mixture
$V$	: molar volume
$V_i^*$	: characteristic volume
$\tilde{V}_i$	: reduced volume
$V^*$	: characteristic volume of mixture
$\tilde{V}$	: reduced volume of mixture
$\Delta v_H^0$	: standard volume of association
$x_i$	: mole fraction
$X_m^E$	: excess molar property
$X^{(n)}$	: adjustable parameters of Redlich and Kister equation

## Greek Letters

$\alpha$	: isobaric expansivity
$\alpha_{12}$	: constant characteristics of binary mixture in graph theory
$\phi_i$	: hard core volume fraction
$\kappa_T$	: isothermal compressibility
$\psi_i$	: molar contact energy fraction
$\sigma$	: standard deviations of $X_m^E$
$\theta_i$	: molecular surface fraction
$\chi_{ij}$	: connectivity parameter of third order in pure state
$(\chi_{ij})_m$	: connectivity parameter of third order in binary mixture
$\chi_{12}$	: flory interaction parameter for excess enthalpies
$\chi_{12}^*$	: flory interaction parameter for excess volume

## Subscript

Expt.	: experimental
F	: flory theory
free vol.	: free volume contribution
i	: pure component
Inter.	: interactional contribution
MK	: Mecke-Kemper type of association
TB	: Treszczanowicz-Benson association model when butanol

is assumed to be associated  
 TB\* : Treszczanowicz-Benson association model when formamide is assumed to be associated

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