

Solubility and dissolution thermodynamics of hexaquoiron(III)tris(*p*-toluenesulfonate) in (ethanol+water) binary mixtures within 291.15–333.15 K

Zhijuan Huang, Chao Yu, Weilan Xue, Fucong Lin, and Zuoxiang Zeng[†]

Institute of Chemical Engineering, East China University of Science and Technology, Shanghai 200237, China

(Received 5 May 2016 • accepted 29 August 2016)

Abstract—The solubility of hexaquoiron(III)tris(*p*-toluenesulfonate) [Fe(OTs)₃·6H₂O] in (ethanol+water) mixtures with a mole fraction of 0–0.327 ethanol was measured from 291.15 to 333.15 K by using a synthetic method. The experimental results show that the solubility of Fe(OTs)₃·6H₂O increases with an increase in temperature and an enrichment in ethanol content. The solubility data were correlated by the modified Apelblat equation, the Redlich-Kister (CNIBS/R-K) model, and the hybrid model, and the results showed that the three models agree well with experimental data. The thermodynamic properties of the dissolution process, including enthalpy, entropy, and Gibbs energy were estimated from the experimental data by the modified van't Hoff equation, indicating that the process of the dissolution of Fe(OTs)₃·6H₂O is endothermic and spontaneous.

Keywords: Hexaquoiron(III)tris(*p*-toluenesulfonate), Thermodynamics, Correlation, Solubility, Phase Equilibria

INTRODUCTION

Hexaquoiron(III)tris(*p*-toluenesulfonate) [Fe(OTs)₃·6H₂O, C₂₁H₃₃FeO₁₅S₃, CAS Registry No. 312619-41-3] is an orange crystalline solid. Its structural formula is shown in Fig. 1. It is widely used as an effective catalyst for many reactions [1–6]. For example, Fe(OTs)₃·6H₂O is an effective catalyst for the intramolecular hydroalkoxylation of unactivated alkenes, the intermolecular hydroalkoxylation of styrene, and the hydrocarboxylation and hydroalkynylation of norbornene [3–6]. In addition, it is an efficient, inexpensive, easy to handle, and available catalyst for the deprotection of *tert*-butyldimethylsilyl, triethoxysilane and triisopropylsilyl ethers [7]. What's more, Fe(OTs)₃·6H₂O is the catalyst for the deprotection of a wide range of aromatic acetals in water [8].

Ethanol and water are usually used as the solvents for many organic reactions when Fe(OTs)₃·6H₂O works as catalyst [6,8]. The solubility of solute is important to design an optimized production process. However, the solubility of Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures has not been reported in the literature.

In this study, we used synthetic method to determine the solubility of Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures with different mole fractions of ethanol (0, 0.050, 0.099, 0.147, 0.193, 0.239, 0.285, 0.327) from *T*=(291.15 to 333.15) K under atmospheric pressure. The experimental solubility data were correlated

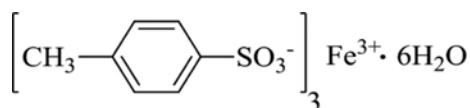


Fig. 1. Molecular structure of Fe(OTs)₃·6H₂O.

with the modified Apelblat model, the Redlich-Kister (CNIBS/R-K) model, and the hybrid model. Meanwhile, the enthalpy (ΔH_{soln}^0), the entropy (ΔS_{soln}^0) and the molar Gibbs free energy (ΔG_{soln}^0) of the dissolution process were calculated by the modified van't Hoff equation.

EXPERIMENTAL SECTION

1. Materials

Fe(OTs)₃·6H₂O (purity>99.0 mass%) was prepared in our laboratory according to the method in literature [9], and its purity was measured by high performance liquid chromatography (HPLC). The thermal gravity analysis (TGA) was carried out on TGA/SDTA851, Mettler Instrument Inc. with a heating rate of 10 K·min⁻¹ from 298.15 to 1,073.15 K. The flow rate of nitrogen gas was 50 mL·min⁻¹,

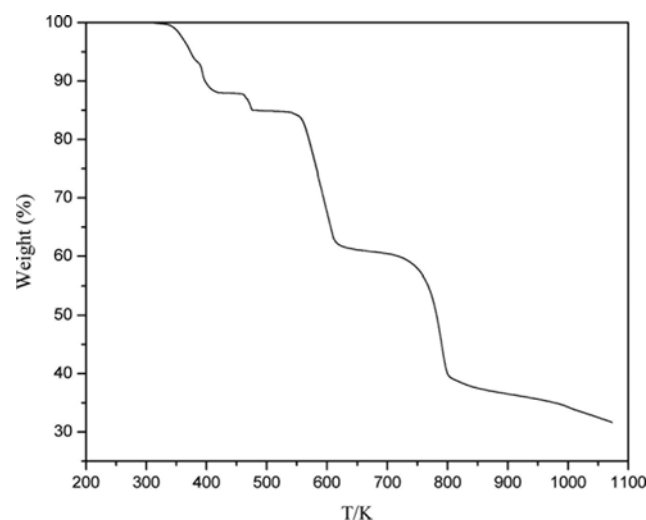


Fig. 2. TGA of Fe(OTs)₃·6H₂O.

[†]To whom correspondence should be addressed.

E-mail: zengzx@ecust.edu.cn

Copyright by The Korean Institute of Chemical Engineers.

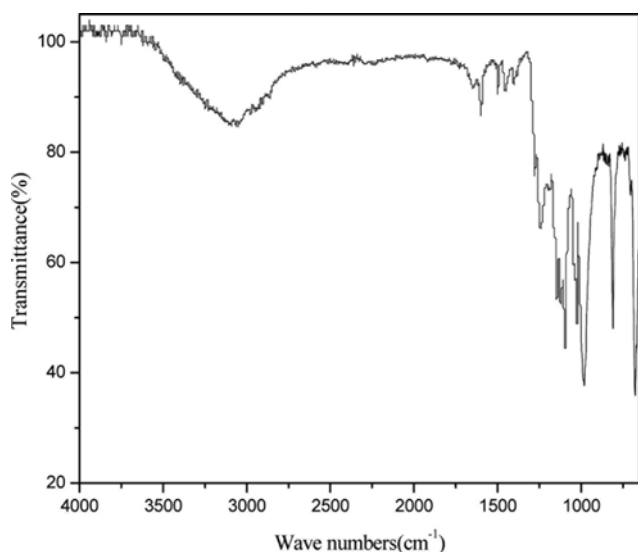


Fig. 3. IR spectrum of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$.

and the mass of TGA sample was about 10.000 mg. The dehydration temperature was determined to be accurate to ± 0.1 K. The thermal analysis result of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ is shown in Fig. 2. It can be seen that the first five water of crystallization in $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ decreases at ~ 408 K, and the last one at ~ 465 K. IR spectra were recorded in the $4000\text{--}400\text{ cm}^{-1}$ range as KBr pellets on Nexus 670, which was supplied by Thermo Electron Corporation, USA (shown in Fig. 3). The absorption band images of the energy disperse spectroscopy of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ are shown in Supporting Information (SI) Fig. S1. Anal. calcd. for $\text{C}_{21}\text{H}_{33}\text{FeO}_{15}\text{S}_3$: C, 37.23; O, 35.42; S, 14.20; Fe, 8.24. Found: C, 37.21; O, 35.40; S, 14.10; Fe, 8.22. Ethanol with purity of 99.7% was supplied by Shanghai TiTan Scientific Co., Ltd.

2. Solubility Measurement

In this work, the solubility of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ in (ethanol+water) binary mixtures was determined by the last crystal disappearance method, which is one type of synthetic method [10,11]. The crystal water in solute will become a part of the solvent during the dissolving process to change the composition of solvent. To make the final mole fractions of ethanol of the binary mixtures be the same (0, 0.050, 0.099, 0.147, 0.193, 0.239, 0.285, 0.327) at different temperatures, the initial mole fractions of ethanol of the binary mixtures were determined by the pre-experiment described in SI. The procedure of the experiment was as follows. First, a certain mass (20 ± 0.001 g) of solvent mixtures with an initial mole fraction of ethanol (x_2^0 , shown in the SI) was added into a three-necked flask that was maintained at the desired temperature (T) by a cylindrical glass thermostatic water bath (SYP-D, Jintan Guowang Experimental Instrument Factory, Changzhou, China). The solution temperature was measured by a mercury thermometer (fluctuates within ± 0.05 K). A magnetic stirrer was used to mix the suspensions. To prevent the evaporation of the solvent at high temperature, a reflux condenser was also used. Then a known amount of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ weighted by an analytical balance (Mettler H542, uncertainty of 0.0001 g) was added to the three-necked flask at the temperature. The next proper of solid (less than 0.05 g) was added to the vessel

when the former solid increment had completely dissolved. The above process was repeated until the last increment (less than 0.01 g) remained partially undissolved for 2 h. All the experiments were conducted at least three times, and the average values were used to calculate the mole fraction solubility. The mole fraction solubility of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ (x_1) was obtained by Eq. (1). The final mole fraction of ethanol in the solvent mixture (x_2) can be calculated according to Eq. (2):

$$x_1 = \frac{m_1/M_1}{7 \times m_1/M_1 + m_2/M_2 + m_3/M_3} \quad (1)$$

$$x_2 = \frac{m_2/M_2}{6 \times m_1/M_1 + m_2/M_2 + m_3/M_3} \quad (2)$$

where m_1 , m_2 , and m_3 are the mass of the $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$, ethanol, and water, respectively [12]. M_1 , M_2 , and M_3 are the molecular mass of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$, ethanol, and water, respectively. The uncertainties of temperature fluctuation of the water bath, temperature measurements, and weighing procedure may cause the uncertainty of solubility measurement of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$, which is no more than 2.0%.

RESULTS AND DISCUSSION

1. Data Correlation

To investigate the relationship of x_1 - T - x_2 , the modified Apelblat equation, the Redlich-Kister (CNIBS/R-K) model, and the hybrid model were adopted. The parameters of these models were calculated by least square method.

1-1. Modified Apelblat Equation

The modified Apelblat equation, which describes the relationship between x_1 and T , is given as follows [13,14]:

$$\ln(x_1) = a + \frac{b}{T} + c \ln T \quad (3)$$

where a , b and c are the model parameters. The values of a and b reflect the variation of the influence of solution nonidealities on the solubility of solute, and the value of c represents the effect of temperature on the enthalpy of fusion.

1-2. Redlich-Kister (CNIBS/R-K) Model

The Redlich-Kister (CNIBS/R-K) model is a theoretical model which describes the relationship between x_1 and x_2 . It is represented in Eq. (4) [15]:

$$\ln(x_1) = x_2^B \ln(x_1)_{B,T} + x_2^C \ln(x_1)_{C,T} + x_2^B x_2^C \sum_{i=0}^n S_i (x_2^B - x_2^C)^i \quad (4)$$

where x_2^B (or x_2^C) refers to the mole fraction of ethanol (or water) when the solute is not added. $(x_1)_{B,T}$ (or $(x_1)_{C,T}$) is the mole fraction of the solute in ethanol (or water) at temperature T . S_i is the model constant and n is the number of the solvents. In this experiment, $n=2$. x_2^C is substituted with $1-x_2^B$, and Eq. (4) can be written as follows:

$$\ln(x_1) = [\ln(x_1)_{B,T} - \ln(x_1)_{C,T} + S_0 - S_1 + S_2] x_2^B + (-S_0 + 3S_1 - 5S_2)(x_2^B)^2 + (-2S_1 + 8S_2)(x_2^B)^3 + (-4S_2)(x_2^B)^4 + \ln(x_1)_{C,T} \quad (5)$$

Eq. (5) can be simplified as Eq. (6)

$$\ln(x_1) = A_1 + A_2x_2^B + A_3(x_2^B)^2 + A_4(x_2^B)^3 + A_5(x_2^B)^4 \quad (6)$$

where A_1, A_2, A_3, A_4 and A_5 are the model parameters.

1-3. Hybrid Model

The hybrid model is used to describe the influence of both the composition of the solvent and the temperature on the solubility data, and can be written as Eq. (7) [16].

$$\ln(x_1) = x_2^B \ln(x_1)_{B.T} + x_2^C \ln(x_1)_{C.T} + x_2^B x_2^C \sum_{i=0}^n \frac{J_i (x_2^B - x_2^C)^i}{T} \quad (7)$$

where J_i is the model parameter, and the other symbols donate the same meaning as Eq. (4). According to Eq. (3), $\ln(x_1)_{B.T}$ and $\ln(x_1)_{C.T}$ can be expressed as the following:

$$\ln(x_1)_{B.T} = a_1 + \frac{b_1}{T} + c_1 \ln T \quad (8)$$

$$\ln(x_1)_{C.T} = a_2 + \frac{b_2}{T} + c_2 \ln T \quad (9)$$

In this work, $n=2$ and substituting x_2^C with $1-x_2^B$, Eq. (7) can be written as Eq. (10)

$$\begin{aligned} \ln(x_1) = & a_1 + \frac{b_1}{T} + c_1 \ln T + (a_1 - a_2)x_2^B + (b_1 - b_2 + J_0 - J_1 + J_2)\frac{x_2^B}{T} \\ & + (-J_0 + 3J_1 - 5J_2)\frac{(x_2^B)^2}{T} + (-2J_1 + 8J_2)\frac{(x_2^B)^3}{T} \\ & + (-4J_2)\frac{(x_2^B)^4}{T} + (c_1 - c_2)x_2^B \ln T \end{aligned} \quad (10)$$

Solving simultaneously Eqs. (8)-(10), the hybrid model equation will be obtained as Eq. (11) [17].

$$\begin{aligned} \ln(x_1) = & B_1 + \frac{B_2}{T} + B_3 \ln T + B_4 x_2^B + B_5 \frac{x_2^B}{T} + B_6 \frac{(x_2^B)^2}{T} \\ & + B_7 \frac{(x_2^B)^3}{T} + B_8 \frac{(x_2^B)^4}{T} + B_9 x_2^B \ln T \end{aligned} \quad (11)$$

in which, B_1 to B_9 are the model parameters.

2. Solubility Data of $\text{Fe}(\text{OTf})_3 \cdot 6\text{H}_2\text{O}$

The experimental solubility data of $\text{Fe}(\text{OTf})_3 \cdot 6\text{H}_2\text{O}$ shown in Table 1 were correlated with Eqs. (3), (6), and (11), and the parameters of the above models are listed in Tables 2-4. The comparisons between experimental data and calculated ones are also presented in

Table 1. Experimental and calculated solubilities of $\text{Fe}(\text{OTf})_3 \cdot 6\text{H}_2\text{O}$ in (ethanol+water) binary mixtures at temperature T and pressure $p=0.1$ MPa

T/K	$10^3 x_1^{exp}$	$(x_1^{exp} - x_1^{cal})/x_1^{exp}$			$10^3 x_1^{exp}$	$(x_1^{exp} - x_1^{cal})/x_1^{exp}$		
		Apelblat	CNIBS/R-K	Hybrid		Apelblat	CNIBS/R-K	Hybrid
$x_2=0$								
291.15	10.71	-0.0282	0.0009	-0.0759	13.11	-0.0084	-0.0042	-0.0200
295.15	12.56	0.0400	-0.0032	0.0071	14.67	0.0240	0.0092	0.0212
299.15	13.26	0.0074	-0.0011	-0.0158	15.35	-0.0083	0.0016	-0.0044
303.15	14.21	-0.0099	-0.0013	-0.0241	16.38	-0.0190	0.0017	-0.0100
306.15	15.11	-0.0113	-0.0041	-0.0191	17.81	0.0091	0.0150	0.0205
309.15	16.38	0.0073	-0.0025	0.0052	18.47	-0.0088	0.0060	0.0046
313.15	17.36	-0.0162	-0.0051	-0.0116	20.20	0.0098	0.0174	0.0241
316.15	18.88	0.0079	-0.0039	0.0166	21.25	0.0090	0.0139	0.0232
319.15	19.68	-0.0092	-0.0027	0.0034	21.98	-0.0081	0.0072	0.0054
323.15	21.64	0.0086	-0.0024	0.0250	23.64	-0.0015	0.0081	0.0096
326.15	22.92	0.0092	-0.0012	0.0281	25.09	0.0091	0.0037	0.0176
329.15	23.83	-0.0077	-0.0032	0.0136	25.87	-0.0076	0.0100	-0.0022
333.15	25.85	0.0007	-0.0005	0.0239	27.76	0.0006	0.0007	0.0006
$x_2=0.099$								
291.15	15.74	0.0029	0.0124	0.0373	17.20	0.0103	-0.0190	0.0260
295.15	16.40	-0.0096	-0.0013	0.0143	17.65	-0.0115	-0.0218	-0.0065
299.15	17.55	0.0032	0.0113	0.0174	18.55	-0.0117	-0.0298	-0.0160
303.15	18.69	0.0092	0.0074	0.0153	19.94	0.0088	-0.0209	-0.0030
306.15	19.17	-0.0089	-0.0135	-0.0080	20.76	0.0086	-0.0072	-0.0078
309.15	20.42	0.0100	0.0071	0.0066	21.28	-0.0080	-0.0300	-0.0286
313.15	21.34	-0.0060	-0.0137	-0.0144	22.69	-0.0005	-0.0147	-0.0248
316.15	22.34	-0.0058	-0.0133	-0.0171	23.97	0.0106	-0.0037	-0.0153
319.15	23.80	0.0111	0.0043	-0.0021	24.64	-0.0063	-0.0258	-0.0339
323.15	24.82	-0.0101	-0.0056	-0.0255	26.21	-0.0052	-0.0081	-0.0331
326.15	26.51	0.0082	-0.0032	-0.0076	27.87	0.0098	-0.0022	-0.0172
329.15	27.30	-0.0109	-0.0055	-0.0271	28.71	-0.0078	-0.0143	-0.0341
333.15	29.65	0.0063	0.0019	-0.0089	30.91	0.0017	-0.0087	-0.0217
$x_2=0.147$								
291.15	15.74	0.0029	0.0124	0.0373	17.20	0.0103	-0.0190	0.0260
295.15	16.40	-0.0096	-0.0013	0.0143	17.65	-0.0115	-0.0218	-0.0065
299.15	17.55	0.0032	0.0113	0.0174	18.55	-0.0117	-0.0298	-0.0160
303.15	18.69	0.0092	0.0074	0.0153	19.94	0.0088	-0.0209	-0.0030
306.15	19.17	-0.0089	-0.0135	-0.0080	20.76	0.0086	-0.0072	-0.0078
309.15	20.42	0.0100	0.0071	0.0066	21.28	-0.0080	-0.0300	-0.0286
313.15	21.34	-0.0060	-0.0137	-0.0144	22.69	-0.0005	-0.0147	-0.0248
316.15	22.34	-0.0058	-0.0133	-0.0171	23.97	0.0106	-0.0037	-0.0153
319.15	23.80	0.0111	0.0043	-0.0021	24.64	-0.0063	-0.0258	-0.0339
323.15	24.82	-0.0101	-0.0056	-0.0255	26.21	-0.0052	-0.0081	-0.0331
326.15	26.51	0.0082	-0.0032	-0.0076	27.87	0.0098	-0.0022	-0.0172
329.15	27.30	-0.0109	-0.0055	-0.0271	28.71	-0.0078	-0.0143	-0.0341
333.15	29.65	0.0063	0.0019	-0.0089	30.91	0.0017	-0.0087	-0.0217

Table 1. Continued

T/K	$10^3 x_1^{exp}$	$(x_1^{exp} - x_1^{cal})/x_1^{exp}$			$10^3 x_1^{exp}$	$(x_1^{exp} - x_1^{cal})/x_1^{exp}$			
		Apelblat	CNIBS/R-K	Hybrid		Apelblat	CNIBS/R-K	Hybrid	
$x_2=0.193$					$x_2=0.239$				
291.15	19.23	0.0044	0.0145	0.0571	19.89	0.0161	-0.0046	0.0221	
295.15	19.71	-0.0104	0.0224	0.0302	20.32	-0.0121	0.0008	-0.0036	
299.15	20.87	0.0042	0.0217	0.0334	21.51	-0.0053	0.0034	0.0047	
303.15	21.89	0.0067	0.0152	0.0266	22.44	-0.0133	0.0035	-0.0026	
306.15	22.31	-0.0099	0.0085	0.0046	23.65	0.0009	0.0128	0.0115	
309.15	23.58	0.0083	0.0170	0.0176	24.65	0.0043	0.0166	0.0143	
313.15	24.63	0.0007	0.0165	0.0050	25.82	-0.0009	0.0119	0.0080	
316.15	25.42	-0.0076	0.0049	-0.0060	26.95	0.0034	0.0129	0.0109	
319.15	26.94	0.0093	0.0153	0.0090	28.14	0.0079	0.0160	0.0136	
323.15	28.16	-0.0033	0.0086	-0.0050	29.66	0.0083	0.0052	0.0111	
326.15	29.25	-0.0089	0.0033	-0.0106	30.55	-0.0011	0.0023	-0.0008	
329.15	31.05	0.0060	0.0176	0.0050	31.78	-0.0009	0.0008	-0.0035	
333.15	32.84	0.0008	0.0123	0.0019	33.26	-0.0077	-0.0083	-0.0148	
$x_2=0.285$					$x_2=0.327$				
291.15	20.93	0.0168	-0.0002	0.0004	22.24	0.0159	0.0004	-0.0224	
295.15	21.16	-0.0116	-0.0108	-0.0308	22.95	-0.0041	0.0040	-0.0275	
299.15	22.15	-0.0083	-0.0115	-0.0287	23.73	-0.0219	0.0040	-0.0325	
303.15	23.09	-0.0117	-0.0089	-0.0322	25.11	-0.0161	0.0029	-0.0162	
306.15	24.41	0.0087	-0.0179	-0.0108	26.92	0.0161	0.0059	0.0220	
309.15	24.90	-0.0084	-0.0226	-0.0269	27.41	-0.0032	0.0071	0.0077	
313.15	26.54	0.0042	-0.0209	-0.0115	29.15	0.0088	0.0071	0.0242	
316.15	27.75	0.0090	-0.0163	-0.0041	30.34	0.0119	0.0052	0.0293	
319.15	28.44	-0.0074	-0.0214	-0.0177	31.05	-0.0016	0.0068	0.0172	
323.15	30.78	0.0151	-0.0097	0.0098	32.40	-0.0075	0.0034	0.0113	
326.15	31.95	0.0089	-0.0040	0.0077	33.97	0.0037	0.0014	0.0209	
329.15	32.87	-0.0075	-0.0095	-0.0042	35.24	0.0045	0.0036	0.0195	
333.15	34.89	-0.0088	0.0028	0.0013	36.51	-0.0075	-0.0002	0.0033	

Standard uncertainties u are $u(T)=0.05$ K, $u(p)=0.05$, $u(x_1)=0.02$, $u(x_2)=0.02$

Table 2. Parameters of the modified Apelblat equation for Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures

Solvent	a	b	c	ARD
$x_2=0$	-9.46177	-1427.38	1.73708	0.0126
$x_2=0.050$	3.71833	-1811.84	-0.32099	0.0095
$x_2=0.099$	-112.341	3769.35	16.7859	0.0079
$x_2=0.147$	-130.634	4685.41	19.4697	0.0078
$x_2=0.193$	-146.979	5554.23	21.8454	0.0062
$x_2=0.239$	-65.2474	1784.13	9.72636	0.0063
$x_2=0.285$	-146.828	5554.75	21.8310	0.0097
$x_2=0.327$	-343.788	4011.42	51.4274	0.0094
Overall ARD				0.0087

Table 1 and Fig. 4. Values of the average relative deviation (ARD) defined by Eq. (12) are also listed in Tables 2-4 [18].

$$ARD = \frac{1}{N} \sum_{i=1}^N \left| \frac{x_i^{exp} - x_i^{cal}}{x_i^{exp}} \right| \quad (12)$$

in which N is the number of experimental points, and x_i^{exp} and x_i^{cal} are the experimental and calculation solubility values, respectively.

According to the corresponding results, the overall ARD for the modified Apelblat equation, the Redlich-Kister (CNIBS/R-K) model, and the hybrid model are 0.87%, 0.89%, and 1.61%, respectively, indicating that the experimental values are well-correlated with the three equations.

3. Thermodynamic Function of Solution

The standard molar enthalpy of solution obtained from the modified van't Hoff equation could be presented as follows [19]:

$$\Delta H_{soln}^0 = -R \cdot \frac{\partial \ln x_1}{\partial (1/T)} \quad (13)$$

in which, R is gas constant.

Over a limited temperature interval, ΔH_{soln}^0 would be valid for the mean temperature (T_{mean}). In this study, the value of T_{mean} is 312.08 K. Therefore, Eq. (13) can be presented as follows [20]:

$$\Delta H_{soln}^0 = -R \cdot \frac{\partial \ln x_1}{\partial (1/T - 1/T_{mean})} \quad (14)$$

Table 3. Parameters of the Redlich-Kister (CNIBS/R-K) model for Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures

T/K	A ₁	A ₂	A ₃	A ₄	A ₅	ARD
291.15	-4.53715	4.41365	-4.00457	-32.8784	75.6924	0.0070
295.15	-4.37430	2.96455	-0.57147	-29.7867	63.7499	0.0092
299.15	-4.32169	2.92262	0.54375	-34.2428	66.4853	0.0105
303.15	-4.25274	2.66386	5.55377	-66.5765	124.906	0.0077
306.15	-4.18811	3.39255	-10.6686	15.9158	3.69291	0.0106
309.15	-4.10899	2.20605	1.99041	-35.1224	69.8715	0.0136
313.15	-4.04841	3.10822	-12.1470	28.7861	-19.0664	0.0134
316.15	-3.96582	2.26829	-5.40138	5.34204	9.99884	0.0093
319.15	-3.92530	2.13692	-1.97814	-12.8639	35.7619	0.0124
323.15	-3.83081	1.79507	-5.85476	24.0190	-35.2388	0.0064
326.15	-3.77464	1.99872	-6.50725	14.8016	-7.37672	0.0027
329.15	-3.73382	1.25939	3.91932	-30.8817	55.4087	0.0081
333.15	-3.65513	1.36978	1.77223	-23.1818	45.3439	0.0044
Overall ARD						0.0089

Table 4. Parameters of the hybrid model for Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures

Parameters	Nonlinear regression values
B ₁	-44.5278
B ₂	326.921
B ₃	6.86341
B ₄	-213.380
B ₅	12113.8
B ₆	-799.374
B ₇	-4373.42
B ₈	11996.1
B ₉	30.8282
Overall ARD	0.0161

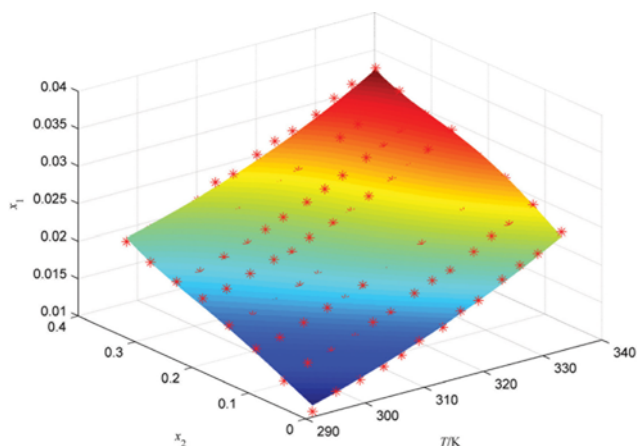
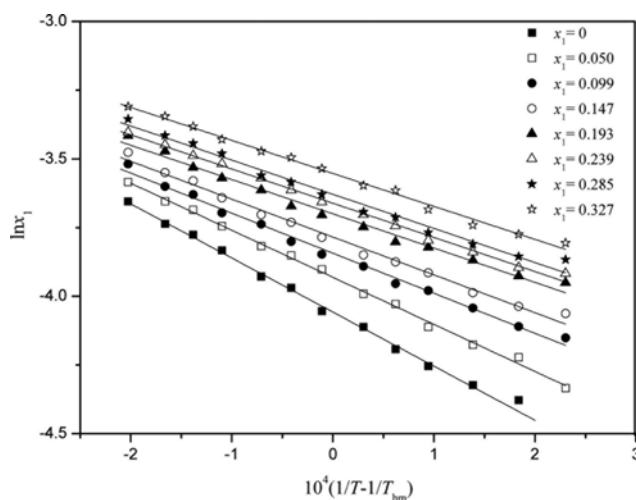
**Fig. 4. Solubility of Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures obtained from hybrid model and the points are the experimental data.**

Fig. 5 shows the plots of $\ln x_1$ versus $10^4(1/T - 1/T_{\text{mean}})$ for Fe(OTs)₃·6H₂O in (ethanol+water) mixtures. From Fig. 5, it can be seen that the plots are linear and the values of the slope (k), the inter-

**Fig. 5. Modified van't Hoff equation for Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures in mole fractions of ethanol, respectively.**

cept (d) and the correlation coefficient (r^2) are listed in Table 5. Eq. (14) can be expressed as

$$\Delta H_{\text{soln}}^0 = -R \cdot k \quad (15)$$

Based on the intercept (d) of the plots shown in Fig. 5, ΔG_{soln}^0 can be calculated by Eq. (16) [21].

$$\Delta G_{\text{soln}}^0 = -d \cdot R \cdot T_{\text{mean}} \quad (16)$$

ΔS_{soln}^0 can be calculated through ΔH_{soln}^0 and ΔG_{soln}^0 by Eq. (17) [22].

$$\Delta S_{\text{soln}}^0 = \frac{\Delta H_{\text{soln}}^0 - \Delta G_{\text{soln}}^0}{T_{\text{mean}}} \quad (17)$$

The values of ΔH_{soln}^0 , ΔG_{soln}^0 , ΔS_{soln}^0 for the dissolution process of Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures are also listed in Table 5.

The relative enthalpy (ζ_H) and entropy (ζ_{TS}) can be defined as the following equations [23,24]:

Table 5. Thermodynamic parameters for dissolution of Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures at mean temperature

x_2	k	d	r^2	ΔH_{soln}^0 kJ·mol ⁻¹	ΔG_{soln}^0 kJ·mol ⁻¹	ΔS_{soln}^0 J·mol ⁻¹ ·K ⁻¹	ζ_H	ζ_{TS}
0	-0.1968	-4.0575	0.9961	16.36	10.53	18.69	0.7372	0.2628
0.050	-0.1712	-3.9311	0.9975	14.23	10.20	12.92	0.7793	0.2207
0.099	-0.1457	-3.8433	0.9936	12.11	9.97	6.86	0.8498	0.1502
0.147	-0.1377	-3.7844	0.9909	11.45	9.82	5.22	0.8755	0.1245
0.193	-0.1247	-3.7000	0.9877	10.37	9.60	2.46	0.9310	0.0690
0.239	-0.1244	-3.6613	0.9955	10.35	9.50	2.71	0.9245	0.0755
0.285	-0.1242	-3.6289	0.9855	10.33	9.42	2.93	0.9188	0.0812
0.327	-0.1200	-3.5530	0.9944	9.98	9.22	2.44	0.9291	0.0709

Table 6. Thermodynamic functions of the transfer of Fe(OTs)₃·6H₂O from more polar solvents to less polar ones to the solution in (ethanol+water) binary mixtures at 312.08 K

x_2		$\Delta_{A \rightarrow B} H_{soln}^0$ kJ·mol ⁻¹	$\Delta_{A \rightarrow B} G_{soln}^0$ kJ·mol ⁻¹	$\Delta_{A \rightarrow B} S_{soln}^0$ J·mol ⁻¹ ·K ⁻¹	$T \Delta_{A \rightarrow B} S_{soln}^0$ kJ·mol ⁻¹
A	B				
0	0.050	-2.13	-0.33	-5.77	-1.80
0.050	0.099	-2.12	-0.23	-6.05	-1.89
0.099	0.147	-0.67	-0.15	-1.65	-0.51
0.147	0.193	-1.08	-0.22	-2.75	-0.86
0.193	0.239	-0.02	-0.10	0.24	0.08
0.239	0.285	-0.02	-0.08	0.22	0.07
0.285	0.327	-0.35	-0.20	-0.49	-0.15

$$\zeta_H = \frac{|\Delta H_{soln}^0|}{|\Delta H_{soln}^0| + |T_{mean} \Delta S_{soln}^0|} \quad (18)$$

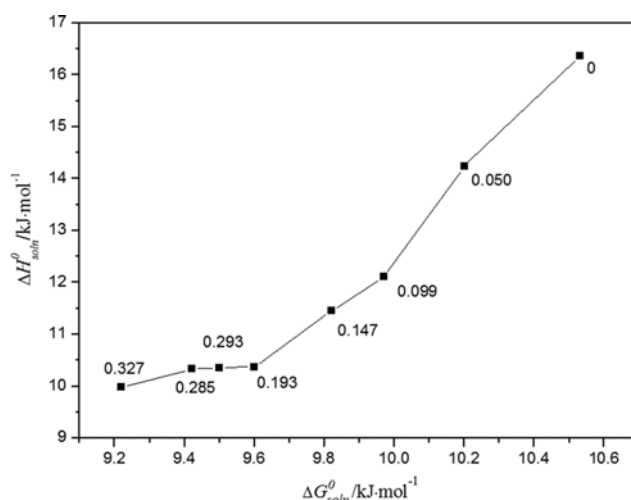
$$\zeta_{TS} = \frac{|T_{mean} \Delta S_{soln}^0|}{|\Delta H_{soln}^0| + |T_{mean} \Delta S_{soln}^0|} \quad (19)$$

The values of ζ_H and ζ_{TS} were calculated and also listed in Table 5. From Table 5, we can see that the ΔH_{soln}^0 and ΔG_{soln}^0 values are observed as positive values in the investigated solvents, indicating that the dissolution of Fe(OTs)₃·6H₂O in the solvents was endothermic and spontaneous. Moreover, the main contributor to the standard Gibbs energy of solution was enthalpy during the dissolution, because of the values of $\zeta_H > 0.7$.

4. Enthalpy-entropy Compensation

The increasing mole fraction of the solvent mixtures was regarded as ethanol being gradually added to the water; the polarity of the solvent decreases continuously with an increase in the composition of solvent mixtures in this experiment. The thermodynamic functions of transfer ($\Delta_{A \rightarrow B} H_{soln}^0$, $\Delta_{A \rightarrow B} G_{soln}^0$ and $\Delta_{A \rightarrow B} S_{soln}^0$) of Fe(OTs)₃·6H₂O from polar solvents to the less polar ones can be calculated from the data shown in Table 5, and the results are listed in Table 6. According to Table 6, the dissolution process is driven by the enthalpy when x_2 changes from 0 to 0.193 and 0.285 to 0.327 ($\Delta_{A \rightarrow B} H_{soln}^0 < 0$, $\Delta_{A \rightarrow B} G_{soln}^0 < 0$, and $\Delta_{A \rightarrow B} S_{soln}^0 < 0$), and when x_2 changes from 0.193 to 0.285 ($\Delta_{A \rightarrow B} H_{soln}^0 < 0$, $\Delta_{A \rightarrow B} G_{soln}^0 < 0$, and $\Delta_{A \rightarrow B} S_{soln}^0 > 0$).

Some physicochemical compensation effects for the solubility of several drugs in aqueous solvent mixtures were demonstrated by Bustamante et al. [25]. The weighted graphs of ΔH_{soln}^0 as a func-

**Fig. 6.** ΔH_{soln}^0 versus ΔG_{soln}^0 enthalpy-entropy compensation plot for the dissolution process of Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures at 312.08 K.

tion of ΔG_{soln}^0 at T_{mean} were used to identify the mechanism of the co-solvent action [26-29]. Fig. 6 shows the plots of ΔH_{soln}^0 versus ΔG_{soln}^0 for the dissolution of Fe(OTs)₃·6H₂O in (ethanol+water) binary mixtures. From Fig. 6, the non-linear curve has a variable positive slope when x_2 changes from 0 to 0.327. In this case, the driving mechanism for solubility is the enthalpy probably due to better solvation of the drug by ethanol molecules.

CONCLUSIONS

The solubility data of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ in (ethanol+water) binary mixtures were measured at temperatures ranging from 291.15 to 333.15 K. The mole fraction of ethanol was 0, 0.050, 0.099, 0.147, 0.193, 0.239, 0.285 and 0.327. The experimental data were correlated by the modified Apelblat equation, the Redlich-Kister (CNIBS/R-K) model, and the hybrid model with good consequences (overall $\text{ARD} < 1.7\%$). In addition, the thermodynamic parameters (ΔH_{soln}^0 , ΔG_{soln}^0 , ΔS_{soln}^0) for the dissolution process of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ in (ethanol+water) binary mixtures at mean harmonic temperature were obtained by a modified van't Hoff equation. The results showed that the dissolution process of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ is endothermic and spontaneous. The thermodynamic functions of transfer ($\Delta_{A \rightarrow B} H_{\text{soln}}^0$, $\Delta_{A \rightarrow B} G_{\text{soln}}^0$ and $\Delta_{A \rightarrow B} S_{\text{soln}}^0$) of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ from polar solvents to the less polar ones can be calculated, and the results showed that the driving mechanism is the enthalpy ($0 < x_2 < 0.327$).

NOMENCLATURE

A_1, A_2, A_3, A_4 and A_5 : parameters of the Redlich-Kister (CNIBS/R-K) model

a, b and c: parameters of the modified Apelblat equation

B_1 to B_9 : parameters of the hybrid model

d : intercept

J_i : parameters of the hybrid model

k : slope

m_1 : the mass of the $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ [g]

m_2 : the mass of the ethanol [g]

m_3 : the mass of the water [g]

M_1 : the molecular mass of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ [g/mol]

M_2 : the molecular mass of ethanol [g/mol]

M_3 : the molecular mass of water [g/mol]

n : the number of the solvents

N : the number of experiment points

p : pressure [Mpa]

R : gas constant [$8.314 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$]

r^2 : the correlation coefficient

T : temperature [K]

T_{mean} : the mean temperature [K]

x_1 : the mole fraction of the solute

x_2 : the mole fraction of the solvent

ΔH_{soln}^0 : enthalpy of the dissolution process [kJ/mol]

ΔS_{soln}^0 : entropy of the dissolution process [$\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$]

ΔG_{soln}^0 : standard mole Gibbs free energy of the dissolution process [kJ/mol]

Greek Letters

ζ_H : the relative enthalpy

ζ_{TS} : the relative entropy

Abbreviations

HPLC : high performance liquid chromatography

TGA : thermal gravity analysis

IR : infrared spectroscopy

ARD : average relative deviation

SI : supporting information

Superscripts

B : ethanol

C : water

exp : experimental

cal : calculated

SUPPORTING INFORMATION

Additional information as noted in the text. This information is available via the Internet at <http://www.springer.com/chemistry/journal/11814>.

REFERENCES

1. M. Horacio and M. M. Afonso, *Synth Commun.*, **38**, 2607 (2008).
2. M. J. Spafford, E. D. Anderson, J. R. Lacey, A. C. Palma and R. S. Mohan, *Tetrahedron. Lett.*, **48**, 8665 (2007).
3. K. Komeyama, T. Morimoto, Y. Nakayama and K. Takaki, *Tetrahedron. Lett.*, **48**, 3259 (2007).
4. F. Ke, Z. K. Li, H. F. Xiang and X. G. Zhou, *Tetrahedron. Lett.*, **52**, 318 (2011).
5. J. C. Choi, K. Kohno, D. Masuda, H. Yasuda and T. Sakakura, *Chem. Commun.*, **38**, 777 (2008).
6. M. S. Jung, W. S. Kim, Y. H. Shin, H. J. Jin, Y. S. Kim and E. J. Kang, *Org. Lett.*, **14**, 6262 (2012).
7. J. M. Bothwell, V. V. Angeles, J. P. Carolan, M. E. Olson and R. S. Mohan, *Tetrahedron. Lett.*, **51**, 1056 (2010).
8. M. E. Olson, J. P. Carolan, M. V. Chiodo, P. R. Lazzara and R. S. Mohan, *Tetrahedron. Lett.*, **51**, 3969 (2010).
9. S. M. Holmes, S. G. McKinley and G. S. Girolami, *Inorganic Syntheses*, **33**, 91 (2002).
10. J. Chen, Z. X. Zeng, W. L. Xue, D. Wang and Y. Huang, *Ind. Eng. Chem. Res.*, **50**, 11755 (2011).
11. C. Yu, Z. X. Zeng and W. L. Xue, *Ind. Eng. Chem., Res.*, **54**, 3961 (2015).
12. C. Yu, Z. J. Huang, Z. X. Zeng and W. L. Xue, *J. Solution Chem.*, **45**, 395 (2016).
13. A. Apelblat and E. Manzurola, *J. Chem. Thermodynamics*, **31**, 85 (1999).
14. A. Apelblat and E. Manzurola, *Chem. Thermodyn.*, **33**, 147 (2001).
15. Q. H. Luan, Y. L. Wang, G. Wang, J. X. Yang and H. X. Hao, *J. Chem. Eng. Data*, **59**, 2642 (2014).
16. A. Jouyban-Gharamaleki and W. E. Acree Jr., *Int. J. Pharm.*, **167**, 177 (1998).
17. Z. M. Zhou, Y. X. Qu, J. D. Wang, S. Wang, J. S. Liu and M. Wu, *J. Chem. Eng. Data*, **56**, 1622 (2011).
18. M. M. Liang, Y. H. Hu, X. Liu, J. Guan, W. G. Yang and Y. Liu, *J. Mol. Liq.*, **197**, 35 (2014).
19. X. Q. Zhou, J. S. Fan, N. Li, Z. X. Du, H. J. Ying, J. L. Wu, J. Xiong and J. X. Bai, *Fluid Phase Equilib.*, **316**, 26 (2012).
20. D. M. Cristancho and F. Martínez, *J. Mol. Liq.*, **200**, 122 (2014).
21. D. W. Wei, H. L. Li, Y. N. Li and J. Zhu, *Fluid Phase Equilib.*, **316**, 132 (2012).
22. A. Maher, D. Croker, A. C. Rasmuson and B. K. Hodnett, *J. Chem.*

- Eng. Data*, **55**, 5314 (2010).
23. Y. Yang, Q. Zhang, C. C. Cao, L. M. Cheng, Y. Shi, W. G. Yang and Y. H. Hu, *Thermochim. Acta*, **592**, 52 (2014).
24. A. R. Holguín, D. R. Delgado, F. Martínez and Y. Marcus, *J. Solution Chem.*, **40**, 1987 (2011).
25. M. A. Ruidiaz, D. R. Delgado, F. Martínez and Y. Marcus, *Fluid Phase Equilib.*, **299**, 259 (2010).
26. E. Tomlinson, *Int. J. Pharm.*, **13**, 115 (1983).
27. E. A. Ahumada, D. R. Delgado and F. Martínez, *Fluid Phase Equilib.*, **332**, 120 (2012).
28. J. Y. Zhang, P. P. Zhang, T. T. Liu, L. Zhou, L. Q. Zhang, R. Lin, G. D. Yang, W. R. Wang and Y. P. Li, *J. Mol. Liq.*, **203**, 98 (2015).
29. D. R. Delgado, G. A. Rodríguez and F. Martínez, *J. Mol. Liq.*, **177**, 156 (2013).

Supporting Information

Solubility and dissolution thermodynamics of hexaquoiron(III)tris(*p*-toluenesulfonate) in (ethanol+water) binary mixtures within 291.15-333.15 K

Zhijuan Huang, Chao Yu, Weilan Xue, Fucong Lin, and Zuoxiang Zeng[†]

Institute of Chemical Engineering, East China University of Science and Technology, Shanghai 200237, China

(Received 5 May 2016 • accepted 29 August 2016)

The procedure of the pre-experiment

The procedure of the pre-experiment was briefly described as follows. Firstly, a set of binary mixtures with the initial mole fractions of ethanol ($x_2^0=0, 0.057, 0.114, 0.171, 0.228, 0.285, 0.342, 0.399$) were prepared, then the solubility of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ at different temperature $T=(291.15 \text{ to } 333.15 \text{ K})$ was measured by the last crystal disappearance method. The final mole fractions of ethanol (x_2) at different temperatures is calculated according to Eq. (2) described in the text, and the arithmetic average value (x_2^{av}) of x_2 was calculated. The relative deviation (RD) between x_2^{av} and x_2 defined by Eq. (S1).

$$\text{RD} = \frac{x_2^{av} - x_2}{x_2^{av}} \times 100\% \quad (\text{S1})$$

The values of x_2^0 , x_2 , x_2^{av} , and RD were listed in Table S1. According to the values of x_2^{av} and RD, a new initial mole fraction of ethanol (x_2^0) can be obtained to make x_2 be approximate to x_2^{av} at a specified temperature. According to the values of x_2^0 at different temperatures, a set of (ethanol+water) binary mixtures were prepared to measured the solubility of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$ with different mole fractions of ethanol ($x_2=0, 0.050, 0.099, 0.147, 0.193, 0.239, 0.285, 0.327$) from $T=(291.15 \text{ to } 333.15 \text{ K})$. The comparisons between experimental data (x_2) and calculated ones (x_2^{av}) can be indicated by the relative deviation (RD') defined by Eq. (S2).

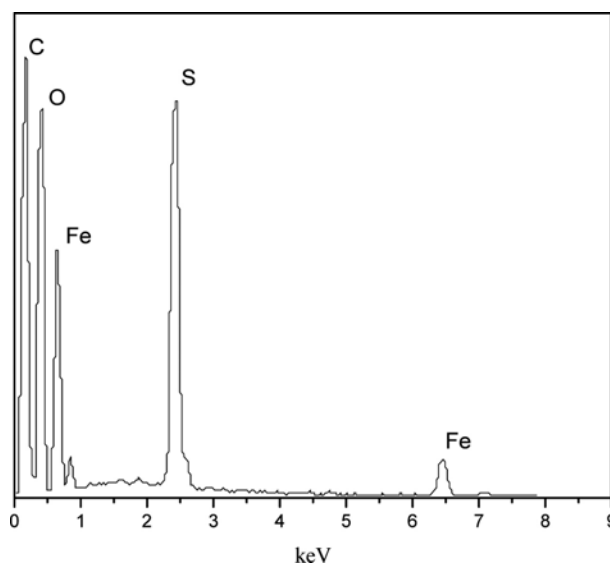


Fig. S1. Energy disperse spectroscopy image of $\text{Fe}(\text{OTs})_3 \cdot 6\text{H}_2\text{O}$.

$$\text{RD}' = \frac{x_2^{av} - x_2}{x_2^{av}} \times 100\% \quad (\text{S2})$$

The values of x_2^0 , x_2 , x_2^{av} and RD' are shown in Table (S2). From

Table S1. The values of x_2^0 , x_2 , x_2^{av} , and RD at temperature T

T/K	x_2^0	x_2	RD	x_2^0	x_2	RD	x_2^0	x_2	RD	x_2^0	x_2	RD
	$x_2^{av}=0$			$x_2^{av}=0.050$			$x_2^{av}=0.099$			$x_2^{av}=0.147$		
291.15	0	0	0	0.057	0.052	-4.91%	0.114	0.103	-4.10%	0.171	0.153	-4.11%
295.15	0	0	0	0.057	0.052	-3.81%	0.114	0.103	-3.63%	0.171	0.153	-3.79%
299.15	0	0	0	0.057	0.052	-3.34%	0.114	0.102	-2.81%	0.171	0.152	-3.14%
303.15	0	0	0	0.057	0.051	-2.61%	0.114	0.101	-1.99%	0.171	0.150	-2.13%
306.15	0	0	0	0.057	0.051	-1.60%	0.114	0.101	-1.65%	0.171	0.149	-1.53%
309.15	0	0	0	0.057	0.051	-1.13%	0.114	0.100	-0.75%	0.171	0.149	-1.15%
313.15	0	0	0	0.057	0.050	0.10%	0.114	0.099	-0.09%	0.171	0.147	-0.13%
316.15	0	0	0	0.057	0.050	0.85%	0.114	0.098	0.64%	0.171	0.146	0.81%
319.15	0	0	0	0.057	0.049	1.37%	0.114	0.097	1.70%	0.171	0.145	1.30%
323.15	0	0	0	0.057	0.049	2.56%	0.114	0.097	2.43%	0.171	0.143	2.46%
326.15	0	0	0	0.057	0.048	3.60%	0.114	0.095	3.67%	0.171	0.142	3.69%
329.15	0	0	0	0.057	0.048	4.17%	0.114	0.095	4.24%	0.171	0.141	4.31%
333.15	0	0	0	0.057	0.047	5.53%	0.114	0.093	5.96%	0.171	0.138	5.94%

Table S1. Continued

T/K	x_2^{r0}	x_2	RD	x_2^{r0}	x_2	RD	x_2^{r0}	x_2	RD	x_2^{r0}	x_2	RD
	$x_2^{av}=0.193$			$x_2^{av}=0.239$			$x_2^{av}=0.285$			$x_2^{av}=0.327$		
291.15	0.228	0.201	−4.24%	0.285	0.250	−4.73%	0.342	0.298	−4.61%	0.399	0.345	−5.37%
295.15	0.228	0.200	−3.88%	0.285	0.250	−4.41%	0.342	0.298	−4.43%	0.399	0.343	−4.82%
299.15	0.228	0.199	−3.03%	0.285	0.247	−3.52%	0.342	0.296	−3.69%	0.399	0.341	−4.22%
303.15	0.228	0.197	−2.27%	0.285	0.246	−2.82%	0.342	0.294	−2.98%	0.399	0.337	−3.17%
306.15	0.228	0.197	−1.96%	0.285	0.244	−1.92%	0.342	0.291	−1.98%	0.399	0.333	−1.76%
309.15	0.228	0.195	−1.02%	0.285	0.242	−1.16%	0.342	0.290	−1.62%	0.399	0.332	−1.39%
313.15	0.228	0.193	−0.24%	0.285	0.240	−0.29%	0.342	0.286	−0.37%	0.399	0.327	−0.04%
316.15	0.228	0.192	0.36%	0.285	0.238	0.57%	0.342	0.283	0.55%	0.399	0.324	0.89%
319.15	0.228	0.190	1.49%	0.285	0.235	1.47%	0.342	0.282	1.08%	0.399	0.322	1.44%
323.15	0.228	0.188	2.40%	0.285	0.233	2.62%	0.342	0.277	2.86%	0.399	0.319	2.50%
326.15	0.228	0.187	3.22%	0.285	0.229	4.06%	0.342	0.274	3.76%	0.399	0.315	3.73%
329.15	0.228	0.184	4.58%	0.285	0.227	4.90%	0.342	0.272	4.47%	0.399	0.312	4.72%
333.15	0.228	0.182	5.93%	0.285	0.225	5.83%	0.342	0.268	6.03%	0.399	0.308	5.73%

Table S2. The values of x_2^0 , x_2 , x_2^{av} and RD' at temperature T

T/K	x_2^0	x_2	RD'	x_2^0	x_2	RD'	x_2^0	x_2	RD'	x_2^0	x_2	RD'
	$x_2^{av}=0$			$x_2^{av}=0.050$			$x_2^{av}=0.099$			$x_2^{av}=0.147$		
291.15	0	0	0	0.054	0.0499	-0.24%	0.109	0.0988	-0.17%	0.164	0.1468	-0.17%
295.15	0	0	0	0.055	0.0499	-0.15%	0.110	0.0989	-0.13%	0.165	0.1468	-0.14%
299.15	0	0	0	0.055	0.0499	-0.11%	0.111	0.0989	-0.08%	0.166	0.1469	-0.10%
303.15	0	0	0	0.056	0.0500	-0.07%	0.112	0.0990	-0.04%	0.167	0.1469	-0.05%
306.15	0	0	0	0.056	0.0500	-0.03%	0.112	0.0990	-0.03%	0.168	0.1470	-0.02%
309.15	0	0	0	0.056	0.0500	-0.01%	0.113	0.0990	-0.01%	0.169	0.1470	-0.01%
313.15	0	0	0	0.057	0.0500	0.00%	0.114	0.0990	0.00%	0.171	0.1470	0.00%
316.15	0	0	0	0.057	0.0500	-0.01%	0.115	0.0990	0.00%	0.172	0.1470	-0.01%
319.15	0	0	0	0.058	0.0500	-0.02%	0.116	0.0990	-0.03%	0.173	0.1470	-0.02%
323.15	0	0	0	0.058	0.0500	-0.07%	0.117	0.0989	-0.06%	0.175	0.1469	-0.06%
326.15	0	0	0	0.059	0.0499	-0.13%	0.118	0.0989	-0.13%	0.177	0.1468	-0.14%
329.15	0	0	0	0.059	0.0499	-0.17%	0.119	0.0988	-0.18%	0.178	0.1467	-0.19%
333.15	0	0	0	0.060	0.0498	-0.31%	0.121	0.0986	-0.36%	0.181	0.1465	-0.35%
	$x_2^{av}=0.193$			$x_2^{av}=0.239$			$x_2^{av}=0.285$			$x_2^{av}=0.327$		
291.15	0.218	0.1927	-0.18%	0.272	0.2385	-0.22%	0.326	0.2844	-0.21%	0.378	0.3261	-0.29%
295.15	0.219	0.1927	-0.15%	0.272	0.2385	-0.19%	0.327	0.2844	-0.20%	0.380	0.3262	-0.23%
299.15	0.221	0.1928	-0.09%	0.275	0.2387	-0.12%	0.329	0.2846	-0.14%	0.382	0.3264	-0.18%
303.15	0.223	0.1929	-0.05%	0.277	0.2388	-0.08%	0.332	0.2847	-0.09%	0.386	0.3267	-0.10%
306.15	0.224	0.1929	-0.04%	0.280	0.2389	-0.04%	0.335	0.2849	-0.04%	0.392	0.3269	-0.03%
309.15	0.226	0.1930	-0.01%	0.282	0.2390	-0.01%	0.336	0.2849	-0.03%	0.393	0.3269	-0.02%
313.15	0.227	0.1930	0.00%	0.284	0.2390	0.00%	0.341	0.2850	0.00%	0.399	0.3270	0.00%
316.15	0.229	0.1930	0.00%	0.287	0.2390	0.00%	0.344	0.2850	0.00%	0.403	0.3270	-0.01%
319.15	0.231	0.1930	-0.02%	0.289	0.2389	-0.02%	0.346	0.2850	-0.01%	0.405	0.3269	-0.02%
323.15	0.233	0.1929	-0.06%	0.292	0.2388	-0.07%	0.352	0.2848	-0.08%	0.409	0.3268	-0.06%
326.15	0.235	0.1928	-0.10%	0.297	0.2386	-0.17%	0.355	0.2846	-0.14%	0.414	0.3265	-0.14%
329.15	0.238	0.1926	-0.21%	0.299	0.2384	-0.24%	0.357	0.2844	-0.20%	0.418	0.3263	-0.22%
333.15	0.242	0.1923	-0.35%	0.302	0.2382	-0.34%	0.363	0.2840	-0.36%	0.422	0.3259	-0.33%

Table (S2), the absolute values of RD' are less than 0.36% which means this method has promising feasibility and efficiency.