

Application of PC-SAFT EoS for calculating gas solubility and viscosity of ammonium-based ionic liquids

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Abstract—The well-known perturbed-chain-statistical-association-fluid-theory (PC-SAFT) EoS was employed to model CO₂ and H₂S absorption in some protic ammonium-based ionic liquids, including Methyl-diethanol-ammonium Formate, Methyl-diethanol-ammonium Acetate, Dimethyl-ethanol-ammonium Formate, and Dimethyl-ethanol-ammonium Acetate. In this way, all the acidic gases and the ILs were considered as associative compounds so that they can establish hydrogen bonding by their own or other molecules. Accordingly, 4C, 2B, and 1A association schemes were assumed for H₂S, the ILs, and CO₂, respectively. Moreover, to estimate the liquid phase concentrations, a complex formation reaction (CFR) approach was followed. In this concept, acidic gases are supposed to form chemical complexes with the ILs. To show the importance of the reactions, the solubilities were calculated with and without using them, and the achieved results were compared. As the outputs show, considering the reactions, the excellent overall AADs% equal to 1.38 and 0.17 were obtained for H₂S and CO₂ absorption, respectively. While without them, these values were about 5.05 and 8.57. In the second part of the work, the viscosity of the used ILs was estimated through a new approach that combines the free-volume-theory (FVT) and the PC-SAFT, CPA, and mSRK EoSs. Accordingly, the density of the ILs computed using the EoSs, and then FVT was applied to estimate the dynamic viscosity. Based on the outputs, all the EoSs illustrate good ability to calculate viscosities, precisely, so that all the models present AAD% of about 2.5. This is because of the high ability of the FVT to obtain a precise estimation of viscosity using a rough estimation of the density.

Keywords: PC-SAFT, EoS, Viscosity, CFR, FVT, CPA

INTRODUCTION

The tunability of the Ionic Liquids (ILs) makes them good candidates for various applications. Indeed, it is possible to arrive at the desired characteristics by choosing suitable cations and anions. One of the ongoing uses of the ILs is to employ them as solvents or cosolvents of acidic gases [1]. A specific category of such compounds, known as Protic ILs (PILs) are able to form hydrogen bonding with the acidic gases and therefore can dissolve them. It is for the sake of their potential to release at least one proton [2]. This potency, along with the insignificant volatility, thermodynamical and electrochemical stability and etcetera, are the main reasons to select these materials.

Despite the mentioned advantages, up to now, limited experimental studies have been done on the absorption of acidic gases by the ILs. It is because of the time, cost, and energy-consuming essence of such experiments. Thus, a theoretical study based on rigorous models could be noticed [3].

So far, many thermodynamical models from different categories have been proposed and investigated for these systems. Recently, among the existing models, SAFT variants have been noticed because of their accuracies [4]. A few such works are reviewed here.

Al-Fnaish and Lue [5] employed PC-SAFT EoS to model absorption of CO₂ and H₂S in [C_{2.8} mim][Tf₂N] ionic liquids. The pure parameters were found by using ILs density data. Moreover, solubility data were used to find binary interaction parameters. According to the results, overall ARD% below 7 and 5 were obtained for H₂S and CO₂, respectively.

EPC-SAFT EoS was implemented to investigate gas solubility in some ILs with [BF₄], [PF₆], and [Tf₂N] anions by Ji et al. [6]. The Debye-Hückel theory was also utilized to take the long-range interactions into account. In a similar survey [7], they also applied the same EoS to correlate hydrogen sulfide absorption in some imidazolium-based ILs with acceptable deviations.

SAFT-VR EoS was used to calculate phase equilibria in CO₂ removal using aqueous alkylamine solutions in the work of MacDowel et al. [8]. In all the studied systems, AADs% below 4 are observed.

Zhu et al. [9] presented two machine learning approaches including artificial neural networks and eXtreme gradient boosting to assist filtered two-fluid model to predict multiphase flows.

Xiong et al. [10] utilized four super-basic ILs as solvents for CO₂/H₂S removal from methane. Physical properties of the ILs were measured. Moreover, the 'deactivated model' was implemented to estimate thermodynamic parameters such as enthalpy and entropy. In another work [11], they designed some TSILs to absorb and convert H₂S to useful mercaptan acids.

On the other hand, physical properties estimation using a precise

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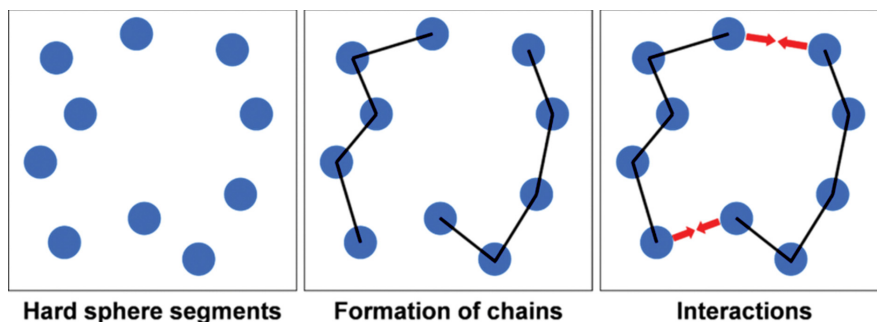


Fig. 1. Chain dispersion concept in the PC-SAFT EoS: Segment attractions- Chain formation- Association formation.

model is another challenge in the way of modeling processes. One of these properties is the dynamic viscosity as a transport property. There exist some approaches to estimating the dynamic viscosity by using thermodynamic models. One of them is to use of free-volume-theory (FVT). Some works on FVT are mentioned here.

Llovel et al. [12] combined FVT and Soft-SAFT EoS to obtain the viscosity of Lennard-Jones (LJ) fluids. They investigated a large family of n-alkanes and compared the results with those of molecular simulation data. Good agreement between both of results was seen so that AADs were calculated under 4%.

The viscosity of petroleum fluids was predicted using FVT+PCSAFT by Khoshnamvand & Assareh [13]. They studied twenty-two real samples with °API between 22 to 45. The overall AAD% equal to 9.7 was achieved.

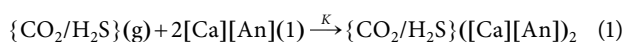
In the work of Shen et al. [14], FVT was combined with the ePC-SAFT to model the viscosity of ILs. In this work, 12 adjustable parameters were utilized and good results were obtained.

Considering good results of the FVT model and the PC-SAFT EoS, in the present research, the solubility of solitary acidic gases (including CO₂ and H₂S) in four ammonium-based PILs including Methyl-diethanol-ammonium Formate ([MDEAH][For]), Methyl-diethanol-ammonium Acetate ([MDEAH][Ac]), Dimethyl-ethanol-ammonium Formate ([DMEAH][For]) and Dimethyl-ethanol-ammonium Acetate ([DMEAH][Ac]) was simulated applying PC-SAFT EoS with and without employing complex formation reaction (CFR) approach. In addition, the dynamic viscosity of the pure ILs was predicted through a new approach combining FVT and PC-SAFT/CPA/mSRK EoS.

THERMODYNAMIC MODELING

1. Complex Formation Reactions (CFR)

The formation of some complexes between acid gas and IL was first proposed by Huang et al. [15] to describe the absorption process through a chemical reaction-like mechanism. As shown in [2], the possibility of the first reaction is almost zero for the investigated system. Therefore:



in which Ca, An, stand for the cations and anions, respectively.

Therefore, equilibrium constant relations together with Henry's law and mass balance equations could be combined and simplified as the below relation [15]:

$$\bar{n}_{AG_0} = \frac{\bar{n}_{IL_0}}{2} + \frac{P}{H} + \frac{[1 - \sqrt{8KP\bar{n}_{IL_0} + 1}]}{8KP} \quad (2)$$

where \bar{n}_{AG_0} and \bar{n}_{IL_0} represent the initial molality of the acidic gas and the IL, respectively.

Parameters K (equilibrium constants of the complex formation reaction) and H (Henry's law constant) were taken from the previous work [2].

After computing the liquid phase mole fractions, VLE calculations will be the next step.

More descriptive details about the CFR can be found in [15].

2. Perturbed Chain SAFT (PC-SAFT) Equation of State

The PC-SAFT was introduced by Gross and Sadowski as an SAFT variant EoS [16]. The main difference between this model and other variants of SAFT EoS returns to the implemented dispersion term. This term tries to take the dispersion attraction between whole chains into account. A conceptual molecular model of PC-SAFT EoS is presented in Fig. 1.

The PC-SAFT can be presented on the basis of reduced residual Helmholtz energy as Eq. (3):

$$\tilde{a}^{res} = \tilde{a}^{hc} + \tilde{a}^{disp} + \tilde{a}^{assoc}. \quad (3)$$

where \tilde{a}^{hc} , \tilde{a}^{disp} , and \tilde{a}^{assoc} denote reduced Helmholtz energy of the hard chain, dispersion, and the association terms, respectively. According to the PC-SAFT variation, the mentioned terms could be defined as below.

2-1. Hard Chain Term

Based on Chapman et al's EoS [17,18], the reduced Helmholtz energy of the hard chain term is as below:

$$\tilde{a}^{hc} = m\tilde{a}^{hs} - \sum_i x_i(m_i - 1) \ln g_{ii}^{hs}(\sigma_{ii}) \quad (4)$$

where m , \tilde{a}^{hs} , $g_{ii}^{hs}(\sigma_{ii})$ stand for segment number, hard-sphere reduced Helmholtz energy and radial distribution function [19], respectively. The mentioned parameters are defined as:

$$m = \sum_i x_i m_i \quad (5)$$

$$\tilde{a}^{hs} = \frac{1}{\xi_0} \left[\frac{3\xi_1\xi_2}{(1-\xi_3)} + \frac{\xi_2^3}{\xi_3(1-\xi_3)^2} - \left(\xi_0 - \frac{\xi_2^2}{\xi_3} \right) \right] \ln(1-\xi_3) \quad (6)$$

$$g_{ij}^{hs} = \frac{1}{1-\xi_3} + \left(\frac{d_i d_j}{d_i + d_j} \right) \frac{3\xi_2}{(1-\xi_3)^2} + \left(\frac{d_i d_j}{d_i + d_j} \right)^2 \frac{2\xi_2^2}{(1-\xi_3)^3} \quad (7)$$

that

$$\xi_k = \left(\frac{\pi}{6}\rho\right) \sum x_i m_i d_i^k \quad n \in \{0, 1, 2, 3\} \quad (8)$$

$$d_i = \sigma_i \left[1 - 0.12 \exp\left(-3\frac{\varepsilon_i}{kT}\right) \right] \quad (9)$$

σ_p , ε_i/k and ρ represent segment diameter, segment energy and density, respectively.

2-2. Dispersion Term

The reduced Helmholtz energy of the dispersion term is as below [16,20]:

$$\tilde{a}^{disp} = (-2\pi\rho I_1 \overline{m^2 \sigma^3}) + (-\pi\rho m C_1 I_2 \overline{m^2 \varepsilon^2 \sigma^3}) \quad (10)$$

in which

$$\overline{m^2 \sigma^3} = \sum_i \sum_j x_i x_j m_i m_j \left(\frac{\varepsilon_{ij}}{kT}\right) \sigma_{ij}^3 \quad (11)$$

$$\overline{m^2 \varepsilon^2 \sigma^3} = \sum_i \sum_j x_i x_j m_i m_j \left(\frac{\varepsilon_{ij}}{kT}\right)^2 \sigma_{ij}^3 \quad (12)$$

$$C_1 = \left(1 + m \frac{8\xi_3 - 2\xi_3^2}{(1-\xi_3)^4} + (1-m) \frac{20\xi_3 - 27\xi_3^2 + 12\xi_3^3 - 2\xi_3^4}{[(1-\xi_3)(2-\xi_3)]^2} \right)^{-1} \quad (13)$$

$$I_1(\xi_3, m) = \sum_{i=0}^6 a_i(m) \xi_3^i \quad (14)$$

$$I_2(\xi_3, m) = \sum_{i=0}^6 b_i(m) \xi_3^i \quad (15)$$

So that

$$\sigma_{ij} = \frac{1}{2}(\sigma_i + \sigma_j) \quad (16)$$

$$\varepsilon_{ij} = \sqrt{\varepsilon_i \varepsilon_j} (1 - k_{ij}) \quad (17)$$

$$a_i(m) = a_{0i} + \frac{m-1}{m} a_{1i} + \frac{m-1}{m} \frac{m-2}{m} a_{2i} \quad (18)$$

$$b_i(m) = b_{0i} + \frac{m-1}{m} b_{1i} + \frac{m-1}{m} \frac{m-2}{m} b_{2i} \quad (19)$$

The constants a_{ki} and b_{ki} have been reported in the literature [21]. Moreover, k_{ij} s are the binary interaction coefficients between i and j species and can be optimized utilizing experimental data.

2-3. Association Term

The Wertheim's association term [22-25] contributes the hydrogen bonding effects as follows:

$$\tilde{a}^{assoc} = \sum_i x_i \sum_{A_i} \left[\ln X_{A_i} - \frac{1}{2} X_{A_i} + \frac{1}{2} \right] \quad (20)$$

X_{A_i} is the main parameter of the association term. It stands for the A-type site fractions at i^{th} molecule that do not establish hydrogen bonding with the other active sites. It is calculated as

$$X^{A_i} = \frac{1}{1 + \rho \sum_j x_j \sum_{B_j} X^{B_j} \Delta^{A,B_j}} \quad (21)$$

So that the Δ^{A,B_j} is interpreted as the association strength and de-

fined as below:

$$\Delta^{A,B_j} = d_{ij}^3 g_{ij}^{hs}(d_{ij}) \kappa^{A,B_j} \left[\exp\left(\frac{\varepsilon^{AB}}{kT}\right) - 1 \right] \quad (22)$$

where ε^{AB} and κ^{A,B_j} are known as the energy and volume of the association, respectively.

3. Modified SRK Equation of States

A specialized version of the Redlich-Kwong EoS [26] for ILs, by Yokozeki and Schiflett [27], was applied to correlate acid gas solubility in the previous work [2]. In this work, this model will be utilized to estimate the ILs dynamic viscosities. For a pure component we have:

$$P = \frac{RT}{V-b} - \frac{a(T)}{V(V+b)} \quad (23)$$

$$a(T) = 0.427480 \frac{R^2 T_c^2}{P_c} \alpha(T) \quad (24)$$

$$b = 0.08664 \frac{RT_c}{P_c} \quad (25)$$

So that for ILs

$$\alpha(T) = 1 + \beta_1 \left(\frac{T_c}{T} - \frac{T}{T_c} \right) \quad (26)$$

In which β_1 belong to the pure ILs and have been taken from [2].

4. Cubic Plus Association (CPA) Equation of State

As expected from its name, EoS contains a cubic part and an association one. The classic form of this model was proposed by Kontogeorgis et al. [28] in which cubic part is the SRK EoS and the association term is from Wertheim's theory.

$$\tilde{a}_{CPA} = \tilde{a}_{SRK} + \tilde{a}_{Assoc} \quad (27)$$

In this way, the association part will be the same presented in section 2.2.3. Moreover, the SRK part could be presented as below:

$$\tilde{a}_{SRK} = \frac{a(T)}{RTb} \ln\left(\frac{v}{v+b}\right) + \ln\left(\frac{v}{v-b}\right) \quad (28)$$

wherein

$$a(T) = a_0 [1 + c(1 - \sqrt{T_r})]^2 \quad (29)$$

Complete details about the model together with the obtained parameters have been presented in the previous works [1,2,29].

5. Free Volume Theory (FVT)

Allal et al. [30] introduced their model to estimate dynamic viscosity based on the free volume theory of Cohen and Turnbull [31]. Their proposed model is known as the FVT model. According to the model, the dynamic viscosity (η) of a dense fluid (e.g., liquids) can be determined through the following relation:

$$\eta = \eta_0 + \Delta\eta \quad (30)$$

In which η_0 is related to the dilute gas viscosity while $\Delta\eta$ is the dense states correction term.

$$\eta_0 = 4.0785 \times 10^{-5} \sqrt{\frac{M_w T}{v_c^2 \Omega^*}} (1 - 0.2756w) \quad (31)$$

$$\Delta\eta = \rho L \frac{\left(E_0 + \frac{PM_w}{\rho}\right)}{\sqrt{3RTM_w}} \exp\left(B\left(\frac{E_0 + \frac{PM_w}{\rho}}{2RT}\right)^{1.5}\right) \quad (32)$$

So that

$$\Omega^* = \frac{1.16145}{T^{0.14874}} + \frac{0.52478}{e^{0.7732T^*}} + \frac{2.16178}{e^{2.73787T^*}} - 6.43 \times 10^{-4} T^{0.14874} \sin(18.0323T^* - 7.27371) \quad (33)$$

wherein

$$T^* = \frac{1.2593T}{T_c} \quad (34)$$

M_w , v_c , w , ρ and R represent molecular weight, critical volume, acentric factor, density, and the universal gas constant, respectively. Moreover, L , E_0 and B are the adjustable parameters of the model and stand for the diffuse barrier energy of the molecule, free space formation parameter and a dimensionless constant, respectively. All the parameters are in the SI system.

More details for FVT are presented in [30].

RESULTS AND DISCUSSION

1. The Pure Component Physical Properties

To implement the FVT model, some physical properties including T_c , w and v_c should be determined. As these data do not exist in the literature, the Modified Lydersen-Joback-Reid: mLJR method by Valderrama and Robles [32] was employed. In this way, critical temperature, critical volume and acentric factor can be estimated applying the below relations, respectively.

$$T_b = 198.2 + \sum n \Delta T_{bM} \quad (35)$$

$$T_c = \frac{T_b}{A_M + B_M \sum n \Delta T_{cM} - (\sum n \Delta T_{cM})^2} \quad (36)$$

$$P_c = \frac{M}{[C_M + \sum n \Delta P_M]^2} \quad (37)$$

$$v_c = D_M + \sum n \Delta v_M \quad (38)$$

$$\omega = \frac{(T_b - 43)(T_c - 43)}{(T_c - T_b)(0.7T_c - 43)} \log \left[\frac{P_c}{P_b} \right] - \frac{(T_b - 43)}{(T_c - T_b)} \log \left[\frac{P_c}{P_b} \right] + \log \left[\frac{P_c}{P_b} \right] - 1 \quad (39)$$

wherein ΔT_{bM} , ΔT_{cM} , Δv_M and ΔP_M are the model parameters that can be found in the literature [32]. Moreover, $A_M=0.5703$, $B_M=1.0121$, $C_M=0.2573$, $D_M=6.75$. All the estimated parameters for the studied ILs, reported in Table 1.

More details about the obtained results and their verification may be found in the previous work [2].

2. The PC-SAFT EoS Pure Parameters

Five optimizable parameters, including $(m, \sigma, \varepsilon, \varepsilon^{AB_i}, \text{ and } \kappa^{AB_i})$, should be fitted for every associating component while they reduce to three (m, σ, ε) for a non-associating one. To find these variables, usually, the model fits the experimental data of liquid densities and vapor pressures. As no experimental data exist for the investigated ILs, only the liquid density data was used through the following cost function:

$$OF = \frac{100}{N_p} \sum_i \frac{|\rho_i^{exp} - \rho_i^{calc}|}{\rho_i^{exp}} \quad (40)$$

Pure CO₂ and H₂S parameters were taken from the literature [33,

Table 1. Estimated physical properties for the pure components using mLJR method

Component	T_c (K)	P_c (bar)	v_c (cm ³ /mol)	ω	M_w
[DMEA][Ac]	692.80	35.06	458.41	0.94	135.1600
[DMEA][For]	565.60	40.86	404.61	0.84	121.1327
[MDEA][Ac]	783.96	37.37	479.11	1.34	151.1640
[MDEA][For]	660.94	43.80	425.31	1.26	137.1317
CO ₂	304.13	73.85	---	0.22	44.0095
H ₂ S	373.10	90.00	---	0.10	34.0820

Table 2. Adjusted PC-SAFT parameters of pure components for ILs and gases

Component	m	σ (Å)	ε/k (K)	κ^{AB_i}	ε^{AB_i}/k (K)	N_p	Ref.	AAD%* (For IL density)
[DMEA][Ac]	2.6421	4.1006	305.5337	0.0025	3,392.7948	12	This work	0.0101
[DMEA][For]	2.3637	4.1031	362.0474	0.0020	4,120.4660	12	This work	0.0132
[MDEA][Ac]	2.8093	4.1455	330.7674	0.0024	3,599.1562	12	This work	0.0116
[MDEA][For]	2.1959	4.4205	540.6711	0.0013	3,659.1829	12	This work	0.0156
CO ₂	2.729	2.7852	169.21	---	---	---	[20]	---
H ₂ S	1.616	3.084	231.61	0.00125	417.69	---	[21]	---

$$*AAD\% = \frac{100}{N_p} \sum_i \frac{|\rho_i^{exp} - \rho_i^{calc}|}{\rho_i^{exp}}$$

34].

Where N_p denotes the total number of data points. Experimental densities for all of the ionic liquids were obtained from the literature [35]. The adjusted parameters along with AAD% values of the used ILs have been reported in Table 2. According to the calculated results, PC-SAFT presents excellent accuracy in estimation of the density so that the densities of all the ILs have been computed with AADs% below 0.02. The experimental and calculated liquid densities of the ILs in various temperatures are plotted in Fig. 2. Detailed values are presented in Table S1 (Supporting Information).

3. Binary Systems

The first step for modeling the absorption of acidic gases into ILs is to find liquid phase concentrations. To do this, two different approaches were followed. The first one is to use experimental liquid concentration data, while the other way tries to compute them through CFR. As one can expect, the latest method needs an extra step for solving CFR. Actually, the first step is to compute the liquid mole fractions using CFR and the latest belongs to VLE calculations by PC-SAFT to obtain the pressure of the bubble point together with the vapor phase composition. K_2 and H parameters were taken from the literature [2] and correlated as a uniform function

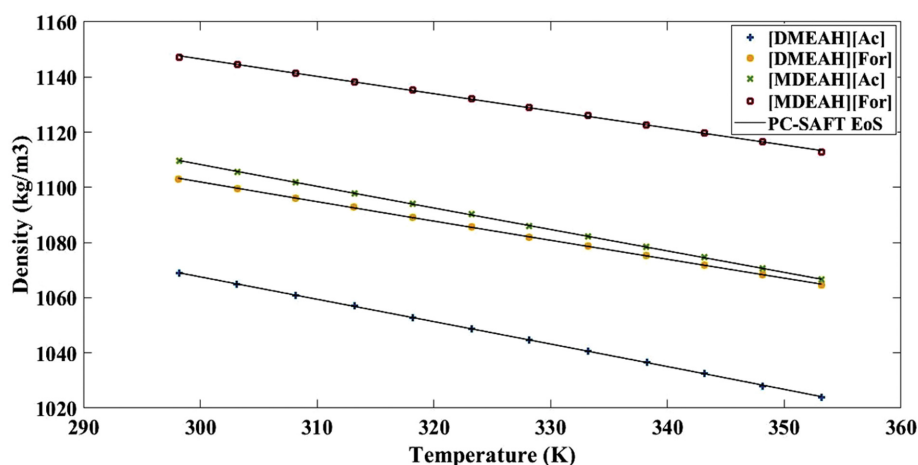


Fig. 2. Experimental and calculated liquid densities of the ionic liquids in various temperatures using PC-SAFT EoS.

Table 3. Optimized parameters of the CFR for the IL+CO₂ and IL+H₂S binary systems

Binary	Parameter	Coefficients of Eq. (41)*				AAD%** (For IL molality)
		A	B	C	D	
[DMEA][Ac]+CO ₂	$K \times 10^{-3}$	-0.0420	0.0001	4.0616	-0.0001	4.40
	H (bar)	-15.6125	0.0555	395.2506	-0.0939	
[DMEA][Ac]+H ₂ S	$K \times 10^{-3}$	-0.0539	0.0001	9.3835	0.0001	4.91
	H (bar)	-16.9996	0.0602	-557.9932	0.1162	
[DMEA][For]+CO ₂	$K \times 10^{-3}$	0.0236	-0.0002	-18.4357	0.0178	4.42
	H (bar)	-64.1185	0.3346	16399.7644	-15.4436	
[DMEA][For]+H ₂ S	$K \times 10^{-3}$	0.0328	-0.0002	-17.3834	0.0174	4.30
	H (bar)	-65.6448	0.4357	9512.2367	-16.8283	
[MDEA][Ac]+CO ₂	$K \times 10^{-3}$	-0.1223	-0.0020	146.0216	0.2106	4.63
	H (bar)	21.1300	0.0277	-2786.6019	-3.2188	
[MDEA][Ac]+H ₂ S	$K \times 10^{-3}$	0.0123	3×10^{-6}	0.9279	-0.0035	4.45
	H (bar)	23.5092	0.0156	-6032.7010	-1.3586	
[MDEA][For]+CO ₂	$K \times 10^{-3}$	-0.0131	-0.00003	-0.00002	-0.00001	13.54
	H (bar)	-2.3084	0.0172	-2.0818	-0.0454	
[MDEA][For]+H ₂ S	$K \times 10^{-3}$	-0.0377	0.00007	8.7547	-0.0003	4.48
	H (bar)	-2.0719	0.0206	-171.9824	-0.2740	

*All the coefficients were taken from [2].

$$** \text{AAD\%} = \frac{100}{N_p} \left| \frac{m_{A_0}^{\text{Exp.}} - m_{A_0}^{\text{Calc.}}}{m_{A_0}^{\text{Exp.}}} \right|$$

Table 4. Binary interaction parameters for solubility of the acid gases in the ILs using PC-SAFT EoS with and without applying the CFR

Binary	PC-SAFT (Without CFR)				AAD%** (For total pressure)	PC-SAFT (With CFR)				AAD%** (For total pressure)
	a	b	c	$\kappa^{Cross,*}$		a	b	c	$\kappa^{Cross,*}$	
[DMEA][Ac]+CO ₂	-2.2301	0.0043	320.4504	-0.4128	5.11	-2.5294	0.0053	312.2902	0.0785	0.15
[DMEA][Ac]+H ₂ S	-3.8589	0.0067	520.5075	---	8.71	-3.9991	0.0090	365.7770	---	1.02
[DMEA][For]+CO ₂	0.0002	0.0005	-0.0001	0.0981	4.14	-17.4593	0.0318	2,429.2690	0.0021	0.36
[DMEA][For]+H ₂ S	-3.8841	0.0064	569.4749	---	10.37	-39.1202	0.0744	5,045.0001	---	2.79
[MDEA][Ac]+CO ₂	-2.1440	0.0039	322.3603	0.0497	4.79	-2.4891	0.0051	313.4102	0.0431	0.15
[MDEA][Ac]+H ₂ S	-3.9094	0.0065	568.2691	---	7.66	-4.0359	0.0089	403.7807	---	0.84
[MDEA][For]+CO ₂	-0.5953	0.0011	128.8935	-1.2429	6.24	-0.6656	0.0012	135.2690	0.0152	0.03
[MDEA][For]+H ₂ S	-1.2702	0.0021	195.6693	---	7.06	-1.1864	0.0023	186.5445	---	0.76

*This cross-association parameter adjusted for CO₂ containing systems only.

$$**AAD\% = \frac{100}{N_p} \sum_i \left| \frac{P^{cal} - P^{exp}}{P^{exp}} \right|$$

***All the presented results have been obtained in the present work.

in terms of operating temperature as below:

$$\ln(H(\text{bar})/K_2) = A + BT + \frac{C}{T} + D \ln(T) \quad (41)$$

The coefficients of Eq. (41) are reported in Table 3.

To determine the binary interaction parameters, a nonlinear simple form relation was considered as a function of temperature:

$$K_{i,j} = a + bT + \frac{c}{T} \quad (42)$$

The coefficients of Eq. (42) were obtained through minimizing the following cost function and all of them are presented in Table 4.

$$OF = \frac{100}{N_p} \sum_i \left| \frac{P^{cal} - P^{exp}}{P^{exp}} \right| \quad (43)$$

P^{cal} and P^{exp} represent computed and experimental pressures, respectively.

All the calculated pressure values have been presented in detail in the Supporting Information file.

Based on the presented results in the table, CFR could impressively promote correlation accuracy. Indeed, the combination of the CFR and the PC-SAFT EoS leads to overall AAD% equal to 0.89 for all the surveyed systems, while without CFR, this value increases to 6.88. Actually, CFR can cause an almost 90% improvement in the overall AAD%.

Elliott's combining rule (ECR) (Eq. (44)) was used to model H₂S solubility, while the modified CR-1 combining rule (Eq. (45)) was applied for CO₂ as a non-self-associating component [36].

$$\varepsilon^{A,B_i} = \frac{\varepsilon^{A,B_i} \varepsilon^{A_j,B_j}}{2}; \quad \kappa^{A,B_i} = \sqrt{\kappa^{A,B_i} \kappa^{A_j,B_j}} \left(\frac{\sqrt{\sigma_i \sigma_j}}{\sigma_{ij}} \right)^3 \quad (44)$$

$$\varepsilon^{A,B_i} = \frac{\varepsilon_{IL}}{2}; \quad \kappa^{A,B_i} = \text{fitted} \quad (45)$$

The fitted values are reported in Table 4.

Table 5. Comparison between the results of PC-SAFT, CPA and mSRK EoSs for correlating acid gas solubility in the ILs

Binaries	Overall AADs% for total pressure*		
	PC-SAFT+CFR	CPA+CFR	mSRK
[DMEA][Ac]+CO ₂	0.15	0.21	2.52
[DMEA][Ac]+H ₂ S	1.02	1.50	5.29
[DMEA][For]+CO ₂	0.36	0.40	2.17
[DMEA][For]+H ₂ S	2.79	2.98	7.33
[MDEA][Ac]+CO ₂	0.15	0.21	4.57
[MDEA][Ac]+H ₂ S	0.84	0.77	7.66
[MDEA][For]+CO ₂	0.03	0.11	4.14
[MDEA][For]+H ₂ S	0.76	0.73	4.17
Overall	0.80	0.92	4.77
Reference	This work	[2]	[2]

$$*AAD\% = \frac{100}{N_p} \sum_i \left| \frac{P^{cal} - P^{exp}}{P^{exp}} \right|$$

In the previous work [2], the CPA, and the mSRK EoSs by Yokozeki and Schiflett [27], were used to model the present systems. For the sake of difference in the approaches used in the two works, a precise comparison cannot be accomplished. But Table 5 presents a rough comparison between the studied models.

Based on the results, the PC-SAFT demonstrates minimum mean overall AAD%=0.8 for both CO₂ and H₂S included systems. On the other hand, CPA shows a bit better accuracy in a few cases. As a result, despite lower AAD% of the PC-SAFT, no meaningful difference can be seen between this model and the CPA, in the case of acid gas solubility estimation. This could be because of two reasons. At first, both PC-SAFT and CPA are of the association models family and can take into account the possible hydrogen bonding effects. Second, might be for the sake of using CFR. Indeed, both CFR and the association term can have a high impact on the model's

accuracy.

Another advantage of the PC-SAFT in comparison with the CPA and mSRK is that PC-SAFT does not need critical properties of

the components. This will be more important when experimental data of such properties are not available. However, according to the accomplished sensitivity analysis in the previous work [2], CPA and

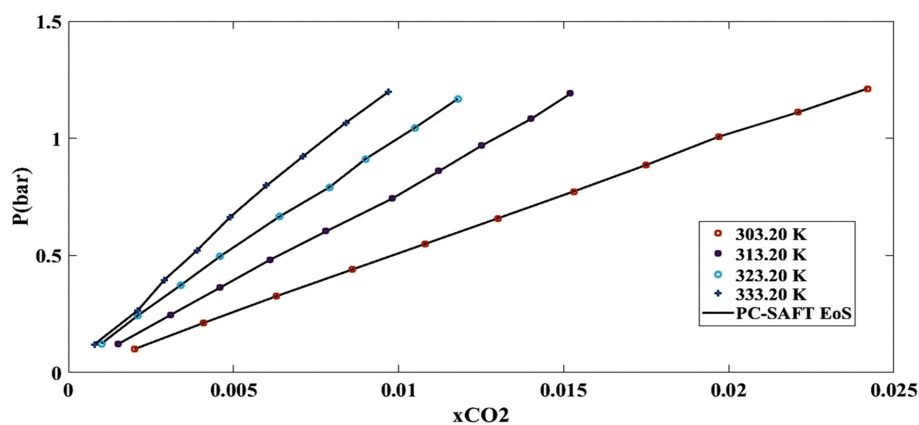


Fig. 3. The experimental and calculated total pressures versus CO_2 liquid mole fractions in ionic liquid [DMEAH][Ac] at different temperatures using PC-SAFT EoS.

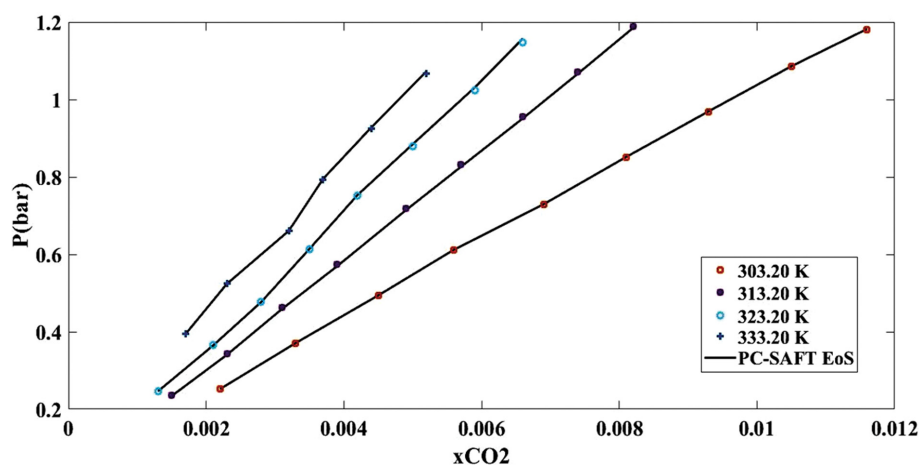


Fig. 4. The experimental and calculated pressure versus CO_2 liquid mole fractions in ionic liquid [DMEAH][For] at different temperatures using PC-SAFT EoS.

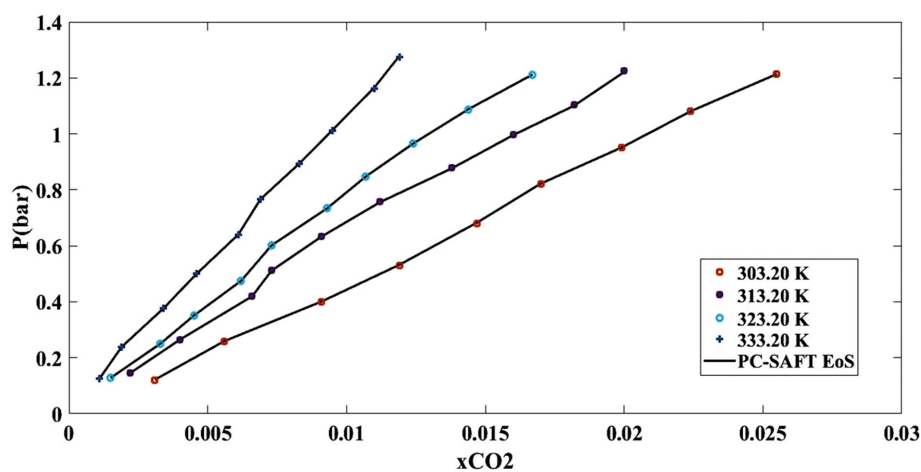


Fig. 5. The experimental and calculated pressure versus CO_2 liquid mole fractions in ionic liquid [MDEAH][Ac] at different temperatures using PC-SAFT EoS.

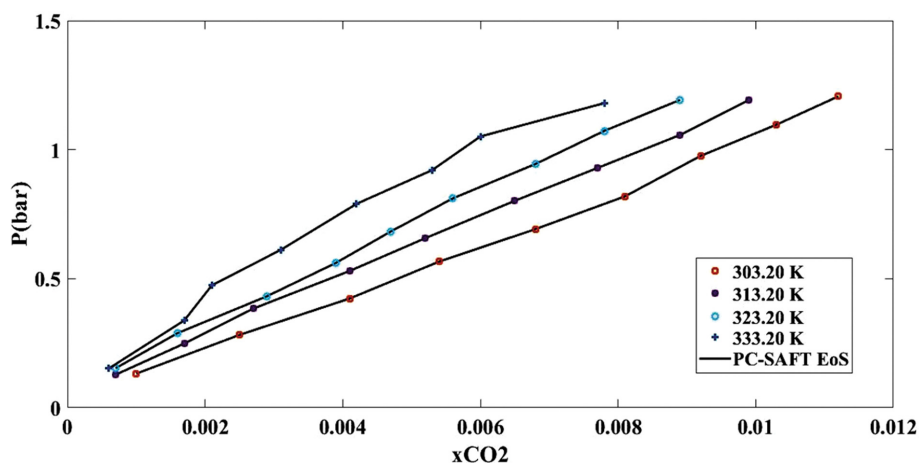


Fig. 6. The experimental and calculated pressure versus CO_2 liquid mole fractions in ionic liquid [MDEAH][For] at different temperatures using PC-SAFT EoS.

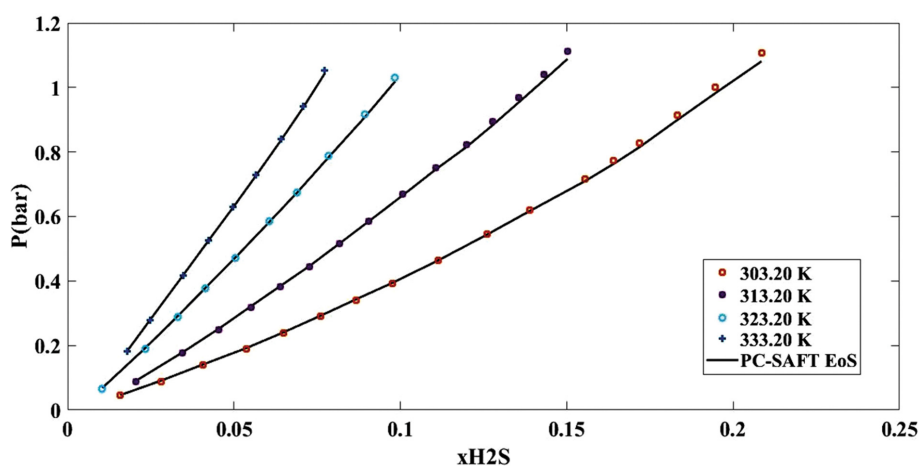


Fig. 7. The experimental and calculated pressure versus H_2S liquid mole fractions in ionic liquid [DMEAH][Ac] at different temperatures using PC-SAFT EoS.

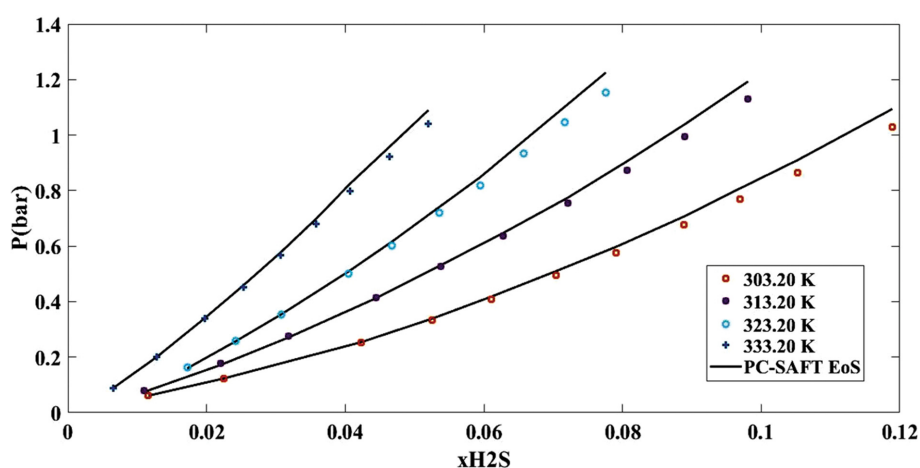


Fig. 8. The experimental and calculated pressure versus H_2S liquid mole fractions in ionic liquid [DMEAH][For] at different temperatures using PC-SAFT EoS.

mSRK show very low sensitivity towards the accuracy of the estimated values.

Figs. 3 to 6 demonstrate total pressures versus the experimental and computed (by PC-SAFT) CO_2 mole fractions in [DMEAH]

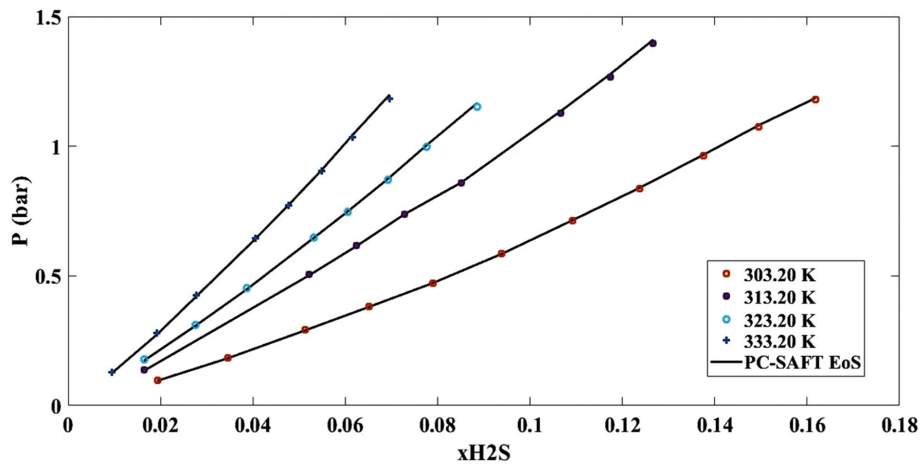


Fig. 9. The experimental and calculated pressure versus H_2S liquid mole fractions in ionic liquid [MDEAH][Ac] at different temperatures using PC-SAFT EoS.

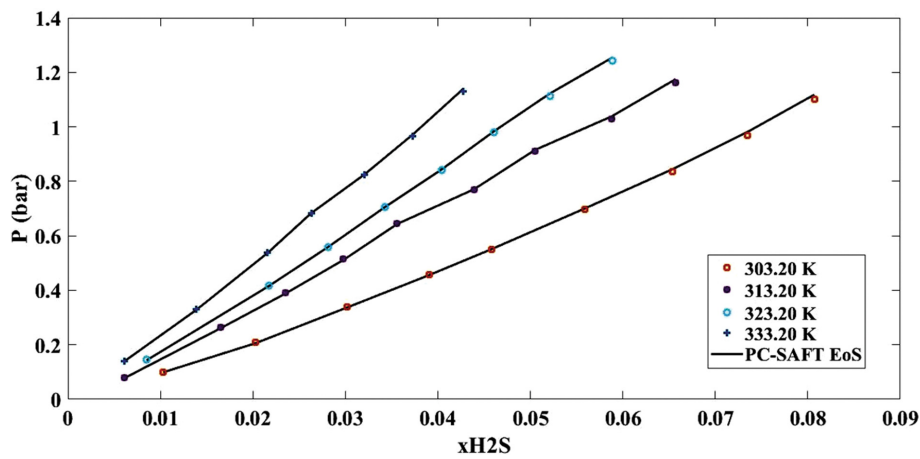


Fig. 10. The experimental and calculated pressure versus H_2S liquid mole fractions in ionic liquid [MDEAH][For] at different temperatures using PC-SAFT EoS.

Table 6. The adjusted parameters of the FVT model in combination with PC-SAFT/CPA/mSRK EoS for the studied ILs

Model	Ionic liquid	The FVT parameters			Reference
		L (m)	E_0 (kJ·mol ⁻¹)	B	
PC-SAFT+FVT	[DMEAH][Ac]	0.5178	20.7985	0.6114	This work
	[DMEAH][For]	3.4807	15.7228	0.7154	
	[MDEAH][Ac]	0.1584	19.2067	0.7853	
	[MDEAH][For]	0.4556	18.7498	0.8174	
CPA+FVT	[DMEAH][Ac]	0.5178	20.8116	0.6114	This work
	[DMEAH][For]	3.2875	21.3572	0.5288	
	[MDEAH][Ac]	0.1570	18.9575	0.7954	
	[MDEAH][For]	0.4517	18.7109	0.8196	
mSRK+FVT	[DMEAH][Ac]	0.0008	9.7169	3.5548	This work
	[DMEAH][For]	0.0011	24.8329	0.7216	
	[MDEAH][Ac]	0.0001	29.5698	0.8335	
	[MDEAH][For]	0.0002	30.0120	0.7836	

[Ac], [DMEAH][For], [MDEAH][Ac], and [MDEAH][For] ILs at various temperatures.

Figs. 7 to 10 exhibit solubility of H_2S in the investigated ILs, respectively. According to these figures, a very good performance of the

PC-SAFT is seen.

4. Viscosity of the Ionic Liquids

FVT was mixed with the PC-SAFT/CPA/mSRK EoSs to estimate the dynamic viscosity of the investigated ILs. In this way, a new approach was followed. In the approach, the density of the ILs is calculated through the EoSs and then the obtained values are utilized to calculate $\Delta\eta$ in Eq. (30). Thus, the densities are obtained using the adjusted parameters in section 3.2. Then, these values are employed to estimate viscosities through optimizing three parameters related to the FVT. The obtained parameters of the FVT model have been reported in Table 6. A comparison between the results of the applied models is presented in Table 7. As anybody can observe, overall AADs% equal to 2.55, 2.52, and 2.59 were obtained using PC-SAFT, CPA, and mSRK, respectively.

Based on the achieved results, no significant discrepancy is observed between the used EoSs. It could be justified by the fact that the FVT model has enough correlative parameters to calculate viscosities using even a rough estimation of density values. As all the used EoSs can correlate the density of the ILs with enough accuracy, the final obtained viscosity results are very close to each other. This low sensitivity of the FVT to the used EoS could be considered as a distinguished positive characteristic of the model.

The experimental versus calculated viscosities of the ionic liquids using PCSAFT+FVT at different temperatures have been shown

Table 7. Comparison between the accuracy of the estimated viscosities of the pure ILs using combination of PC-SAFT/CPA/mSRK EoSs and the FVT model

IL	Overall AADs% for the ILs viscosities*		
	PC-SAFT+FVT	CPA+FVT	mSRK+FVT
[DMEA][Ac]	1.73	1.73	1.75
[DMEA][For]	2.00	1.97	2.07
[MDEAH][Ac]	3.49	3.44	3.50
[MDEAH][For]	3.00	2.94	3.04
Overall	2.55	2.52	2.59
Reference	This work	This work	This work

$$*AAD\% = \frac{100}{N_p} \sum_i^N \left| \frac{\eta^{cal} - \eta^{exp}}{\eta^{exp}} \right|$$

in Fig. 11.

5. Model Predictability

To check the predictability of the models used for equilibrium data and viscosity calculations, a scenario was followed. In this way, for equilibrium calculation, between investigated temperatures including 303, 313, 323 and 333 K, two of them (303 and 333 K) were selected to obtain the model parameters (Correlation part). Data

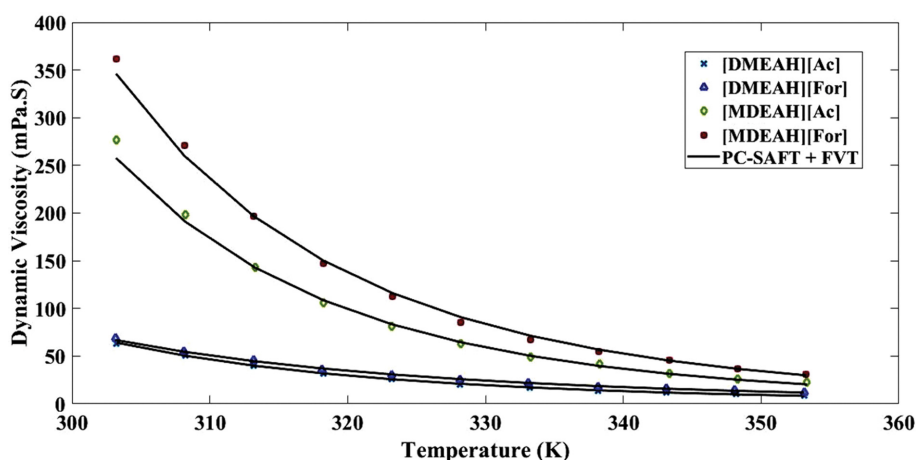


Fig. 11. The experimental and calculated dynamic viscosities of the ionic liquids using PCSAFT+FVT at different temperatures.

Table 8. AADs% for prediction of equilibrium data for different binaries

Binaries	AAD%		Binary interaction parameters			
	Correlation (303 & 333 K)	Prediction (313 & 323 K)	$a \times 10^{-2}$	$b \times 10^{-2}$	$c \times 10^{-2}$	κ^{Cross}
[DMEA][Ac]+CO ₂	0.15	0.19	-0.025480	0.000053	3.153815	0.000736
[DMEA][Ac]+H ₂ S	0.98	1.05	-0.040024	0.000090	3.663009	---
[DMEA][For]+CO ₂	0.81	17.86	-0.064655	0.000145	6.849608	0.000861
[DMEA][For]+H ₂ S	1.84	34.33	-0.137139	0.000345	10.118581	---
[MDEAH][Ac]+CO ₂	0.11	0.13	-0.023391	0.000049	2.891995	0.000505
[MDEAH][Ac]+H ₂ S	0.82	0.87	-0.040368	0.000089	4.039189	---
[MDEAH][For]+CO ₂	0.03	0.029	-0.006805	0.000013	1.37606	0.000156
[MDEAH][For]+H ₂ S	0.79	0.73	-0.012239	0.000023	1.924963	---

Table 9. AADs% for prediction of dynamic viscosities for different ILs

Binaries	AAD%		FVT Parameters		
	Correlation (6 data points)	Prediction (5 data points)	L (m)	E_0 (kJ·mol ⁻¹)	B
[DMEA][Ac]	1.07	2.69	0.5910	20,820.7276	0.6020
[DMEA][For]	0.86	3.80	3.2054	15,801.1873	0.7203
[MDEAH][Ac]	3.42	3.57	0.1617	21,464.1584	0.7061
[MDEAH][For]	2.65	3.74	0.4838	18,829.0486	0.8099

of the two other temperatures (313 and 323 K) were predicted using the obtained parameters in the correlation part. Table 8 presents obtained results for the equilibria calculations.

As one can see from the results, the used model presents good ability in both correlation and prediction approaches.

Following the latest approach, for prediction of dynamic viscosities, six experimental data were utilized to obtain model parameters (Correlation part) and the other five data were employed to check the model's predictability. In this way, data in 303.19, 313.19, 323.27, 333.26, 343.35 and 353.25 K were used for correlation scenario and those in 308.15, 318.23, 328.22, 338.21 and 348.30 K for the prediction part.

Table 9 presents obtained parameters and the results in both scenarios.

According to the obtained AADs%, it can be concluded that the PC-SAFT+FVT model has high ability in both correlation and prediction of viscosity values.

CONCLUSIONS

A combination of the PC-SAFT EoS and CFR was employed to compute the acidic gas solubility in ionic liquids [DMEA][Ac], [DMEA][For], [MDEAH][Ac] and [MDEAH][For] through a VLE calculation approach. In this way, CFR calculates the liquid phase mole fractions and then PC-SAFT is implemented for the VLE calculation part.

Experimental density data of the ILs were utilized to find the PC-SAFT pure parameters. Accordingly, all the parameters were adjusted with excellent AADs% about 0.01 for all the ILs.

In addition, for the investigated binaries, including [DMEA][Ac]+CO₂, [DMEA][For]+CO₂, [MDEAH][Ac]+CO₂, [MDEAH][For]+CO₂, [DMEA][Ac]+H₂S, [DMEA][For]+H₂S, [MDEAH][Ac]+H₂S, and [MDEAH][For]+H₂S, the AADs% equal to 0.15, 0.36, 0.15, 0.03, 1.02, 2.79, 0.84 and 0.76 were found, respectively. Moreover, overall AADs% equal to 1.38 for H₂S and 0.17 for CO₂ solubility were calculated. To show the CFR impact, results were obtained with and without using CFR. As the outputs present, meaningful improvement (from AAD%=6.88 to AAD%=0.8) is observed in the case of CFR use.

The PC-SAFT results were also compared with those of CPA and mSRK EoSs. Based on the results, the PC-SAFT and the CPA show close results so that using these models, 0.8 and 0.92 were obtained as total AADs%, respectively. This nearness can be because of the presence of the association term and the CFR.

In the next part of the work, the dynamic density of the stud-

ied ILs was estimated by merging the PC-SAFT, CPA and mSRK EoSs and the FVT model. In the followed approach, the density of the IL is calculated using the EoSs and then these values are utilized to compute viscosity. According to the results, all the implemented EoSs show very close AADs% equal to almost 2.5. This is because FVT has enough optimizable parameters by itself. Actually, it could be concluded that the FVT can present suitable accuracy with low sensitivity toward paired EoS.

LIST OF SYMBOLS

\tilde{a}	: reduced Helmholtz energy
B	: dimensionless constant of FVT model
d	: temperature-dependent diameter [Å]
E_0	: free space formation parameter
g	: radial distribution function
H	: Henry's law constant
k	: Boltzmann's constant (1.38066×10 ⁻²³ J K ⁻¹)
K_i	: equilibrium constant of reaction <i>i</i>
L	: diffuse barrier energy
\bar{m}_i	: molality of component I [mol/kg]
m	: number of segments
M_w	: molecular weight
N_p	: number of data points
N_i	: number of molecules of component <i>i</i>
N_A	: Avogadro's number [6.02205×10 ²³ /mol]
P	: total pressure
P_b	: boiling pressure
P_C	: critical pressure
R	: universal gas constant [8.31415 J/mol·K]
β	: mSRK parameter
T	: absolute temperature [K]
T_b	: normal boiling temperature [K]
T_C	: critical temperature [K]
T_r	: reduced temperature [T/ T_C]
v	: molar volume
v_C	: critical volume
V	: volume [m ³]
w	: acentric factor
X_{Ai}	: fraction of A-type unbounded sites on molecule <i>i</i>
Z	: compressibility factor

Greek Letters

Δ^{AB_i}	: association strength
ε_i	: segment energy

ε^{AB}	: association energy
η	: dynamic viscosity [mPa·S]
κ^{A,B_j}	: association volume
ρ	: density
σ	: temperature-independent diameter [Å]
ξ	: hard chain term parameter

Superscript

Assoc.	: association
Cal.	: calculated
disp.	: dispersion
Exp.	: experimental
hs.	: hard sphere
hc	: hard chain
res.	: residual

SUPPORTING INFORMATION

Additional information as noted in the text. This information is available via the Internet at <http://www.springer.com/chemistry/journal/11814>.

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Application of PC-SAFT EoS for calculating gas solubility and viscosity of ammonium-based ionic liquids

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Temperature (K)	Liquid density (kg/m ³)											
	[DMEA][AC]			[DMEA][For]			[MDEA][Ac]			[MDEA][For]		
	Calc.	Exp.	AAD%	Calc.	Exp.	AAD%	Calc.	Exp.	AAD%	Calc.	Exp.	AAD%
298.21	1,069.02	1,068.90	0.011	1,103.33	1,103.10	0.021	1,109.73	1,109.50	0.021	1,147.69	1,147.29	0.035
303.15	1,065.00	1,065.00	0.000	1,099.70	1,099.50	0.018	1,105.79	1,105.60	0.017	1,144.56	1,144.46	0.008
308.19	1,060.91	1,060.90	0.001	1,096.10	1,096.10	0.000	1,101.80	1,101.80	0.000	1,141.37	1,141.37	0.000
313.24	1,056.82	1,057.00	0.017	1,092.59	1,092.80	0.019	1,097.83	1,097.90	0.006	1,138.20	1,138.29	0.008
318.18	1,052.81	1,052.90	0.008	1,089.05	1,089.20	0.014	1,093.95	1,094.10	0.014	1,135.10	1,135.20	0.009
323.22	1,048.72	1,048.80	0.007	1,085.52	1,085.60	0.007	1,090.01	1,090.20	0.017	1,131.95	1,132.11	0.014
328.16	1,044.71	1,044.70	0.001	1,082.09	1,082.00	0.008	1,086.16	1,086.10	0.006	1,128.87	1,129.03	0.014
333.21	1,040.60	1,040.60	0.000	1,078.60	1,078.60	0.000	1,082.24	1,082.20	0.003	1,125.74	1,125.94	0.018
338.25	1,036.48	1,036.50	0.002	1,075.20	1,075.30	0.009	1,078.40	1,078.40	0.000	1,122.67	1,122.60	0.006
343.19	1,032.42	1,032.60	0.018	1,071.75	1,071.90	0.014	1,074.49	1,074.80	0.029	1,119.55	1,119.77	0.020
348.14	1,028.33	1,028.00	0.032	1,068.36	1,068.30	0.006	1,070.64	1,070.70	0.006	1,116.49	1,116.43	0.006
353.18	1,024.14	1,023.90	0.024	1,064.93	1,064.50	0.040	1,066.72	1,066.50	0.020	1,113.38	1,112.83	0.049

[illegible]

Table S3. Experimental and calculated pressures for [DMEA][For]+CO₂ system in various temperatures

[DMEA][AC]+CO ₂											
T=303.2 K			T=313.2 K			T=323.2 K			T=333.2 K		
P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%
10,015.92	10,000	0.159	12,105.03	12,100	0.042	12,368.68	12,300	0.558	12,191.75	12,000	1.598
21,208.14	21,200	0.038	24,653.65	24,700	0.188	24,320.75	24,300	0.085	26,510.29	26,400	0.418
32,602.94	32,600	0.009	36,310.93	36,400	0.245	37,284.16	37,300	0.042	39,454.47	39,400	0.138
44,000.00	44,000	0.000	48,072.52	48,200	0.264	49,664.01	49,700	0.072	52,215.91	52,200	0.030
54,898.87	54,900	0.002	60,237.58	60,400	0.269	66,659.60	66,700	0.061	66,392.13	66,400	0.012
65,798.98	65,800	0.002	74,203.20	74,400	0.265	79,073.19	79,100	0.034	79,787.99	79,800	0.015
77,300.00	77,300	0.000	85,779.15	86,000	0.257	91,200.00	91,200	0.000	92,199.96	92,200	0.000
88,601.46	88,600	0.002	96,759.91	97,000	0.248	104,544.80	104,500	0.043	106,632.87	106,600	0.031
100,703.03	100,700	0.003	108,143.47	108,400	0.237	116,900.42	116,800	0.086	119,880.97	119,800	0.068
111,104.00	111,100	0.004	119,030.95	119,300	0.226	12,368.68	12,300	0.558	12,191.75	12,000	1.598
121,204.28	121,200	0.004	12,105.03	12,100	0.042	24,320.75	24,300	0.085	26,510.29	26,400	0.418
10,015.92	10,000	0.159	24,653.65	24,700	0.188	37,284.16	37,300	0.042	39,454.47	39,400	0.138

Table S4. Experimental and calculated pressures for [MDEA][AC]+CO₂ system in various temperatures

[MDEA][AC]+CO ₂											
T=303.2 K			T=313.2 K			T=323.2 K			T=333.2 K		
P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%
12,182.85	12,100	0.685	14,500.00	14,500	0.000	12,790.74	12,800	0.072	12,504.63	12,500	0.037
25,950.45	25,800	0.583	26,487.59	26,500	0.047	25,076.94	25,100	0.092	23,892.12	23,900	0.033
40,093.01	39,900	0.484	41,960.51	42,000	0.094	35,070.96	35,100	0.083	37,589.93	37,600	0.027
53,207.68	53,000	0.392	51,138.45	51,200	0.120	47,470.00	47,500	0.063	50,000.00	50,000	0.000
68,294.44	68,100	0.286	63,302.25	63,400	0.154	60,176.33	60,200	0.039	64,025.10	64,000	0.039
82,252.94	82,100	0.186	75,557.63	75,700	0.188	73,390.65	73,400	0.013	76,660.10	76,600	0.078
95,089.47	95,000	0.094	87,705.23	87,900	0.222	84,809.28	84,800	0.011	89,407.26	89,300	0.120
108,100.00	108,100	0.000	99,546.19	99,800	0.254	96,534.37	96,500	0.036	101,462.75	101,300	0.161
121,382.07	121,500	0.097	110,086.95	110,400	0.284	108,867.18	108,800	0.062	116,547.00	116,300	0.212
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Table S5. Experimental and calculated pressures for [MDEA][For]+CO₂ system in various temperatures

[MDEA][For]+CO ₂											
T=303.2 K			T=313.2 K			T=323.2 K			T=333.2 K		
P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%
13,209.21	13,200	0.070	12,799.88	12,800	0.001	15,300.00	15,300	0.000	15,186.23	15,200	0.091
28,215.72	28,200	0.056	24,899.77	24,900	0.001	28,902.70	28,900	0.009	33,876.73	33,900	0.069
42,318.00	42,300	0.043	38,399.68	38,400	0.001	43,208.31	43,200	0.019	47,475.06	47,500	0.053
56,616.49	56,600	0.029	52,999.62	53,000	0.001	56,115.84	56,100	0.028	61,177.87	61,200	0.036
69,211.94	69,200	0.017	65,699.61	65,700	0.001	68,325.13	68,300	0.037	78,988.31	79,000	0.015
81,904.29	81,900	0.005	80,199.63	80,200	0.000	81,137.14	81,100	0.046	92,100.92	92,100	0.001
97,590.56	97,600	0.010	92,899.70	92,900	0.000	94,452.12	94,400	0.055	105,117.61	105,100	0.017
109,676.74	109,700	0.021	105,699.82	105,700	0.000	107,268.95	107,200	0.064	118,038.30	118,000	0.032
120,661.72	120,700	0.032	119,200.00	119,200	0.000	119,286.89	119,200	0.073	15,186.23	15,200	0.091
13,209.21	13,200	0.070	12,799.88	12,800	0.001	15,300.00	15,300	0.000	33,876.73	33,900	0.069
28,215.72	28,200	0.056	24,899.77	24,900	0.001	28,902.70	28,900	0.009	47,475.06	47,500	0.053
42,318.00	42,300	0.043	38,399.68	38,400	0.001	43,208.31	43,200	0.019	---	---	---

[illegible][illegible]

Table S8. Experimental and calculated pressures for [MDEAH][Ac]+H₂S system in various temperatures

[MDEAH][Ac]+H ₂ S											
T=303.2 K			T=313.2 K			T=323.2 K			T=333.2 K		
P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%
9,552.99	9,700	1.516	13,401.55	13,700	2.178	17,293.25	17,700	2.298	12,560.04	12,900	2.635
18,188.84	18,400	1.148	50,130.91	50,500	0.731	30,673.42	31,200	1.688	27,335.81	27,900	2.022
28,979.87	29,200	0.754	61,561.03	61,800	0.387	44,704.95	45,200	1.095	42,009.20	42,600	1.387
38,017.82	38,200	0.477	73,853.01	73,900	0.064	64,677.09	64,900	0.343	64,183.83	64,500	0.490
47,186.70	47,300	0.240	85,982.34	85,800	0.213	74,800.00	74,800	0.000	77,300.00	77,300	0.000
58,500.00	58,500	0.000	113,595.11	112,800	0.705	87,342.84	87,000	0.394	90,830.48	90,400	0.476
71,450.49	71,300	0.211	127,833.80	126,700	0.895	100,366.44	99,600	0.770	104,355.93	103,400	0.924
84,001.13	83,700	0.360	141,048.13	139,600	1.037	116,679.04	115,300	1.196	119,863.29	118,200	1.407
96,643.64	96,200	0.461	---	---	---	---	---	---	---	---	---
108,155.42	107,600	0.516	---	---	---	---	---	---	---	---	---
118,534.95	117,900	0.539	---	---	---	---	---	---	---	---	---

Table S9. Experimental and calculated pressures for [MDEAH][For]+H₂S system in various temperatures

[MDEAH][For]+H ₂ S											
T=303.2 K			T=313.2 K			T=323.2 K			T=333.2 K		
P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%	P ^{Calc.} (Pa)	P ^{Exp.} (Pa)	AAD%
9,901.77	10,100	1.963	7,750.24	7,900	1.896	14,300.10	14,500	1.379	13,938.26	14,100	1.147
20,601.98	20,900	1.426	26,071.85	26,400	1.243	41,521.82	41,800	0.665	32,861.30	33,100	0.721
33,716.60	34,000	0.834	38,773.84	39,100	0.834	55,816.90	56,000	0.327	53,746.46	53,900	0.285
45,639.96	45,800	0.349	51,160.50	51,400	0.466	70,600.00	70,600	0.000	68,300.00	68,300	0.000
55,101.12	55,100	0.002	64,332.88	64,400	0.104	84,339.24	84,100	0.284	82,619.30	82,400	0.266
70,052.14	69,700	0.505	77,068.35	76,900	0.219	98,446.88	97,900	0.559	97,206.50	96,700	0.524
84,484.28	83,700	0.937	91,506.42	91,000	0.557	112,201.08	111,300	0.810	113,804.91	112,900	0.802
98,162.62	96,900	1.303	103,847.55	103,000	0.823	125,489.01	124,200	1.038	---	---	---
111,793.28	110,000	1.630	117,472.48	116,200	1.095	---	---	---	---	---	---