

## Multi-objective optimization of a methanol synthesis process: CO<sub>2</sub> emission vs. economics

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**Abstract**—This work addresses the modeling and multi-objective optimization of methanol synthesis to efficiently utilize CO<sub>2</sub> from the CO<sub>2</sub> emissions and economics perspectives. Kinetic reactors for reforming and methanol synthesis reactions were used in the process simulator for modeling the entire process, and multi-objective optimization was conducted using the developed process model to maximize CO<sub>2</sub> reduction and the economic profit. The feed composition, operating temperature and pressure of the reformer, and utility temperature of the methanol synthesis reactor were considered as arguments in the non-dominated sorting genetic algorithm (NSGA II) method with the net change of CO<sub>2</sub> and economic profit as the objective elements, and the Pareto front showed a trade-off between CO<sub>2</sub> reduction and economic profit. When the amount of CH<sub>4</sub> in the feed was fixed at 500 kmol/h, CO<sub>2</sub> reduction was 11,588 kg/h, whereas the profit was −5.79 million dollars per year. Meanwhile, a maximum profit of 20 million dollars per year resulted in CO<sub>2</sub> emissions of 7,201 kg/h. The feed composition had the most significant influence on both objective elements (net change of CO<sub>2</sub> and economics); as CO<sub>2</sub> in the feed increased, CO<sub>2</sub> reduction increased and profit decreased, while the increase of H<sub>2</sub>O in the feed increased CO<sub>2</sub> emissions and profit.

Keywords: Methanol Synthesis Process, Reforming, Multi-objective Optimization, Economic Analysis, CO<sub>2</sub> Reduction

### INTRODUCTION

Since the Industrial Revolution, the increase in greenhouse gas concentrations has resulted in severe global warming. As many climate change abnormalities have already occurred, several countries insist on a net CO<sub>2</sub>-zero policy, and research on carbon capture and storage (CCS) and carbon capture and utilization (CCU) has been actively conducted. Various CCS and CCU methods include post-combustion, direct air capture, and biological capture, while polycarbonation, mineralization, biological utilization, photosynthesis, electrolysis, and enhanced oil recovery are some of the methods of CO<sub>2</sub> utilization [1]. CO<sub>2</sub> can be converted to different substances and used as feedstock in many reactions, including 123 reactions reported in the literature [2]. Some of the CO<sub>2</sub> utilization reactions, such as reforming, the synthesis of methanol (MeOH), dimethyl ether (DME), dimethyl carbonate (DMC) [3], formic acid [4], and urea [5], have been described in detail.

Among the many methods of CO<sub>2</sub> utilization, MeOH synthesis has been studied extensively because of its fuel quality and high demand. Because H<sub>2</sub> is essential for converting CO<sub>2</sub> into MeOH, many reaction routes, such as steam reforming, partial oxidation (POX), auto thermal reforming (ATR), water-gas-shift (WGS), and other catalytic reactions, have been introduced to produce H<sub>2</sub>. In

addition, photoelectrochemical processes and electrolysis using renewable energy have also been developed [6,7]. Dry (CO<sub>2</sub>) reforming of CH<sub>4</sub> was adopted as an appropriate method because it can utilize CO<sub>2</sub> while producing hydrogen. The kinetics of mixed reforming of CH<sub>4</sub>, composed of steam and dry reforming, and WGS, have been developed to analyze the effects of GHSV (gas hourly space velocity) and pressure on reforming [8]. It is difficult to utilize CO<sub>2</sub> because it is a very stable molecule, and many types of catalysts and mechanisms have been studied to convert CO<sub>2</sub> into MeOH. For MeOH synthesis, several reaction kinetics related to CO and CO<sub>2</sub> hydrogenation have been developed. Kinetics of CO and CO<sub>2</sub> hydrogenation and WGS over Cu-Zn-Al catalysts were developed under 15-50 bar and 210-245 °C [9]. The design of a large-scale MeOH synthesis process was proposed using the kinetics of reforming and MeOH synthesis, and the process model was used to evaluate the effects of reaction temperature, CO<sub>2</sub> fraction in the feed, and the recycling route on MeOH productivity, and CO and CO<sub>2</sub> conversion [10]. In addition, techno-economic analysis of the MeOH synthesis process with mixed reforming showed that the CO<sub>2</sub>-utilized gas-to-MeOH process (CGTM) can be economically feasible in the plant scale range of 2,500-5,000 tons per day [11].

Many efforts have been made to analyze and improve the MeOH synthesis process. Multi-objective optimization of steam reforming was conducted by dynamic simulation and genetic algorithms, with the maximization of CH<sub>4</sub> conversion and minimization of a stoichiometric parameter as the objectives. It was proved that the tran-

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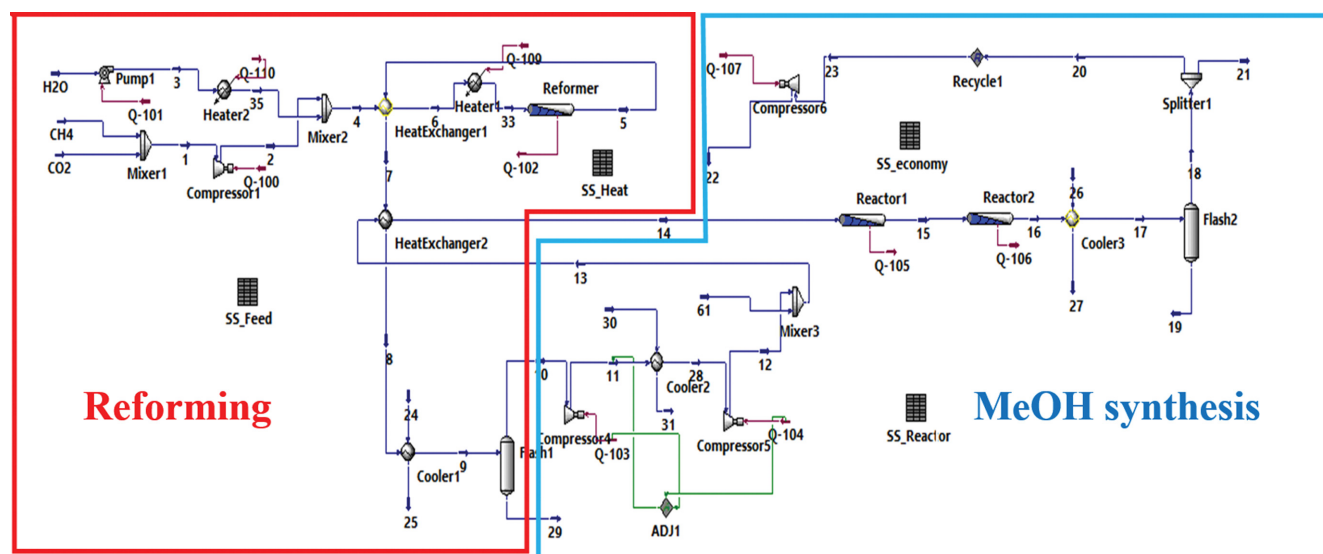


Fig. 1. Scheme of reforming and MeOH synthesis process.

sition period had the greatest effect on the objective function [12]. Using  $H_2$  and  $CO_2$ , various MeOH production processes were studied; MeOH plant, electrolysis plant, fuel cost, etc.), and economic analysis was conducted under the situation where prices are fluctuating [13].

Previous studies related to the modeling of  $CO_2$  utilization processes have mainly focused on the economy. However, as global warming has become increasingly severe, regulations on  $CO_2$  emissions have been strengthened, and studies on  $CO_2$  reduction have been conducted accordingly. The potential of  $CO_2$  reduction, market scale, and thermodynamic characteristics of some reactions, including the production of MeOH, DME, DMC, formic acid, aldehydes, and urea have been described [7]. MeOH synthesis from  $CO_2$  and green  $H_2$  was studied, where two methods of MeOH production were introduced: one with direct  $CO_2$  hydrogenation, and the other with reforming, followed by CO and  $CO_2$  hydrogenation. Under the best conditions, 1.6 tons of  $CO_2$  could be reduced per ton of MeOH [14].

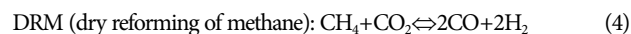
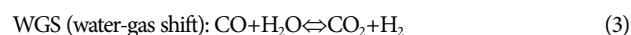
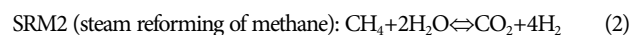
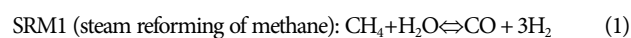
Although  $CO_2$  is consumed in the process streams, it can still be generated via energy consumption during the process. Therefore, it is necessary to study  $CO_2$  utilization from the perspective of both  $CO_2$  consumption by the reactions and  $CO_2$  emissions from energy requirements, such as heating and compression. In this study, the MeOH synthesis process using  $CO_2$ ,  $CH_4$ , and  $H_2O$  as feedstock was studied from the perspective of both  $CO_2$  reduction and economy. Syngas was produced by reforming, and MeOH was produced by CO and  $CO_2$  hydrogenation. After a process model for the entire process was developed by implementing kinetic reactor models in the simulator for both reforming and MeOH synthesis [8,10], a case study was conducted to understand the characteristics of the MeOH synthesis process. The process simulation was conducted using HYSYS (Aspen Technology). Because too many arguments require considerable computation load for case studies, the number of arguments was reduced by sensitivity analysis. Multi-object optimization (NSGA II) was conducted using Python

and HYSYS spreadsheets to consider a trade-off between  $CO_2$  reduction and economic profit, and the Pareto front was also identified.

## METHOD

### 1. Reforming

The purpose of reforming is to produce syngas from  $CH_4$ ,  $CO_2$ , and  $H_2O$ . The reforming process is shown in Fig. 1, where the reformer feed is a mixture of  $CH_4$ ,  $CO_2$ , and  $H_2O$ . The feed conditions were fixed at 25 °C and 101 kPa, and it was assumed that the  $CO_2$  supplied was 100% pure. Compressors and heaters were installed before the reformer because it was operated at 500–1,200 kPa and 750–900 °C. For thermodynamics, the Peng–Robinson equation was chosen, and the tube number, length, and diameter were specified at 80, 10 m, and 0.1016 m, respectively, resulting in a total volume of 12.972 m<sup>3</sup>. Note that the size of the single tube that was determined in our previous work [10] was used without modification, while the number of tubes was adjusted by 1.6 times so that the residence time was maintained. Because the reforming reaction rate is very fast, the early part of the tube was in a kinetic regime, and the temperature was abruptly decreased by the endothermic reaction. In the later part, it was in a thermodynamic regime, and the temperature increased owing to an excessive supply of heat to the reformer. Water in the reformer effluent was evacuated in a flash vessel (Flash1 in Fig. 1) to prevent it from entering the MeOH synthesis reactor. The overall reactions and rate equations of the present study are as follows, and the kinetic parameters were used without modification [8,10]:



$$r_{SRM1} = \frac{k_{SRM1} \left( f_{CH_4} f_{H_2O} - \frac{f_{H_2}^3 f_{CO}}{K_{pSRM1}} \right) / f_{H_2}^{2.5}}{\left[ 1 + K_{CO} f_{CO} + K_{H_2} f_{H_2} + K_{CH_4} f_{CH_4} + K_{H_2O} \left( \frac{f_{H_2O}}{f_{H_2}} \right) \right]^2} \quad (5)$$

$$r_{SRM2} = \frac{k_{SRM2} \left( f_{CH_4} f_{H_2O} - \frac{f_{H_2}^4 f_{CO_2}}{K_{pSRM2}} \right) / f_{H_2}^{3.5}}{\left[ 1 + K_{CO} f_{CO} + K_{H_2} f_{H_2} + K_{CH_4} f_{CH_4} + K_{H_2O} \left( \frac{f_{H_2O}}{f_{H_2}} \right) \right]^2} \quad (6)$$

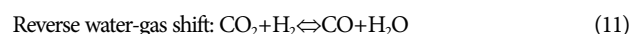
$$r_{WGS} = \frac{k_{WGS} \left( f_{CO} f_{H_2O} - \frac{f_{H_2} f_{CO_2}}{K_{pWGS}} \right) / f_{H_2}}{\left[ 1 + K_{CO} f_{CO} + K_{H_2} f_{H_2} + K_{CH_4} f_{CH_4} + K_{H_2O} \left( \frac{f_{H_2O}}{f_{H_2}} \right) \right]^2} \quad (7)$$

$$r_{DRM} = \frac{k_{DRM} \left( f_{CH_4} f_{CO_2} - \frac{f_{H_2}^2 f_{CO}}{K_{pDRM}} \right)}{[(1 + K_{CH_4} f_{CH_4} + K_{CO} f_{CO})(1 + K_{CO_2} f_{CO_2})]} \quad (8)$$

## 2. MeOH Synthesis Reactor

The MeOH synthesis reactor was used to produce MeOH from syngas. Fig. 1 displays the MeOH synthesis, which consisted of two reactors. MeOH synthesis occurred at 5,000 kPa, and the wall temperature was set at 180–230 °C. The inlet stream of the MeOH synthesis reactor was compressed using two compressors to boost energy efficiency. In our previous work [10], an inert material was used in the early part of the reactor to prevent an abrupt increase in temperature. To consider this feature, two reactors were employed in the process model, with the first reactor containing 50% inert material and the second reactor containing only catalysts; the kinetic parameters changed with the inert percentage. The two MeOH synthesis reactors had a tube diameter of 0.0411 m, tube number of 7200, and lengths of 4.4 m (the first reactor) and 8.46 m (the second reactor). The size of the single tube in the methanol synthesis reactor was specified to be the same as that of our previous work

[10]. Meanwhile, the amount of syngas from the reformer was increased compared to that of our previous work and there was a recycle stream for the reactor in this work, resulting in a higher flow rate at the reactor inlet by 5–10 times than our previous work. Therefore, the number of tubes of the methanol synthesis reactor was increased for the residence time to be maintained [8,10]. The amount of CH<sub>4</sub> in the feed was set at 500 kmol/h for commercial scale (methanol production of 100 TPD). The MeOH synthesized in the MeOH reactor effluent was separated at the bottom of a flash vessel (Flash2 in Fig. 1) at 25 °C. The recovered gas in the flash vessel was recycled to the inlet of the MeOH synthesis reactor with a purge stream to prevent the accumulation of inert gases. The overall reactions and rate equations of MeOH synthesis were as follows, and kinetic parameters were used without modification [10]:



$$r_{CO} = \frac{k_A K_{CO} \left( f_{CO} f_{H_2}^{1.5} - \frac{f_{CH_3OH}}{K_{p,A} f_{H_2}^{0.5}} \right)}{(1 + K_{CO} f_{CO})(1 + K_{H_2}^{0.5} f_{H_2} + K_{H_2O} f_{H_2O})} \quad (13)$$

$$r_{CO_2} = \frac{k_C K_{CO_2} \left( f_{CO_2} f_{H_2}^{1.5} - \frac{f_{H_2O} f_{CH_3OH}}{K_{p,C} f_{H_2}^{0.5}} \right)}{(1 + K_{CO_2} f_{CO_2})(1 + K_{H_2}^{0.5} f_{H_2} + K_{H_2O} f_{H_2O})} \quad (14)$$

$$r_{RWGS} = - \frac{k_B K_{CO_2} \left( f_{CO_2} f_{H_2} - \frac{f_{CO} f_{H_2O}}{K_{p,B}} \right)}{(1 + K_{CO_2} f_{CO_2})(1 + K_{H_2}^{0.5} f_{H_2} + K_{H_2O} f_{H_2O})} \quad (15)$$

**Table 1.** Equipment purchased cost, and utility and feed price [16,19,22] (The value of the M&S index in 1968 is 280, while that in 2018 is 1638.2)

Equipment		Purchased cost	
	Reactor	$(M\&S/280) \times 101.3 \times (A)^{0.65} \times F_m \times F_c$	
	Pump	$(M\&S/280) \times 517.5 \times (\text{bhp})^{0.82} \times F_c$	
	Pressure - vessels, columns	$(M\&S/280) \times 101.9 \times (D)^{1.066} \times H^{0.082} \times F_c$	
	Tray	$(M\&S/280) \times 4.7 \times (D)^{1.55} \times H \times F_c$	
	Compressor	$(M\&S/280) \times 517.5 \times (\text{bhp})^{0.82} \times F_c$	
	Heat exchanger	$(M\&S/280) \times 101.3 \times (A)^{0.65} \times F_c$	
	Furnace	$(M\&S/280) \times 5070 \times (Q)^{0.85} \times F_c$	
		Value	Unit
Utility	Cooling water	0.013583	\$/ton
	Electricity	0.0727	\$/KWh
	Furnace fuel	$4.22 \times 10^{-6}$	\$/kJ
Feed	CH <sub>4</sub>	0.1267	\$/kg
	H <sub>2</sub> O	0.000349	\$/kg
	CO <sub>2</sub>	0	\$/kg
Product	MeOH	0.36	\$/kg

**Table 2. Ratio factors used in the calculation of TCI [20]**

Item	Ratio factors	Values
Direct cost	Purchase equipment	1.00
	Purchase equipment installation	0.47
	Buildings	0.8
	Yard improvements	0.1
	Service facility	0.7
	Instrumentation & controls	0.36
	Piping	0.68
	Electrical systems	0.11
Indirect cost	Engineering and supervision	0.33
	Contractor's fee	0.22
	Contingency	0.44
	Construction expenses	0.41
	Legal expenses	0.04
	Working capital	0.89

$$r_{DME} = \frac{k_{DME} K_{CH_3OH}^2 \left( C_{CH_3OH}^2 - \frac{C_{H_2O} C_{DME}}{K_{P,DME}} \right)}{(1 + 2\sqrt{K_{CH_3OH} C_{CH_3OH} + K_{H_2O,DME} C_{H_2O}})^4} \quad (16)$$

### 3. Cost Estimation Method

The economy of the process was estimated using the profit and total production cost (TPC). TPC consists of a few factors listed in Table 3, total capital investment (TCI) and utility cost. The correlations for the equipment cost and the costs of utility, feed, and product are provided in Table 1 [15-21].

The following equation was used to calculate the total capital investment (TCI), and the ratio factors are listed in Table 2:

$$TCI = I_E \times \left( 1 + \sum_{i=1}^n RF_i \right) \quad (17)$$

where  $I_E$  and RF represent the total equipment cost and the ratio of the total equipment cost, respectively.

The TPC was calculated as follows:

$$TPC = (\text{Utility} + \text{Operating \& Maintenance} + \text{Others}) \times (100/90) \quad (18)$$

The correlations for operating/maintenance and other factors are shown in Table 3. Based on the TCI and TPC, the following equation was used to calculate the profit:

**Table 4. Correlations for CO<sub>2</sub> equivalent**

Item	CO <sub>2</sub> equivalent [kg/kJ]
Electricity	$1.158 \times 10^{-4}$
Furnace fuel	$7.06 \times 10^{-5}$

$$\text{Profit} = (\text{Product revenue} - \text{TPC}) \quad (19)$$

### 4. Calculation Method for CO<sub>2</sub> Equivalent

The utility and energy used in the process were converted to CO<sub>2</sub> equivalent using the correlations in Table 4 [22,23]. The efficiency of the furnace was assumed to be 70%.

The net change of CO<sub>2</sub> was calculated as follows:

$$\begin{aligned} \text{Net change of CO}_2 = & (\text{CO}_2 \text{ equivalent by fuel usage}) \\ & + (\text{CO}_2 \text{ equivalent by electricity usage}) \\ & + (\text{CO}_2 \text{ in the process outlet streams}) \\ & - (\text{CO}_2 \text{ in the process inlet streams}) \end{aligned} \quad (20)$$

where positive net change corresponds to the emission of CO<sub>2</sub> (either the amount of CO<sub>2</sub> equivalent by energy usage was larger than the consumption of CO<sub>2</sub> by the reaction, or CO<sub>2</sub> was produced by the reaction) while a negative value represents CO<sub>2</sub> reduction.

### 5. Multi-objective Optimization

The non-dominated sorting genetic algorithm (NSGA II) method, which includes non-dominated sorting and crowding distance sorting to help find the Pareto front, was used because the relationship between the result and each variable is approximately linear. The non-dominated sorting algorithm makes elements close to the Pareto front, and the crowding distance sorting algorithm spreads the elements of the group far to find a wide Pareto front. The algorithm is shown in Fig. 2 and detailed algorithms can be found in [24,25].

The feed composition, reformer temperature, reformer pressure, and MeOH synthesis reactor wall temperature were considered as variables. The objective functions were defined with the net change of CO<sub>2</sub> and economic profit, whose calculation procedures are provided in Sections 2.3 and 2.4. To maintain the MeOH production rate, the amount of CH<sub>4</sub> in the feed was fixed at 500 kmol/h. At this amount of CH<sub>4</sub>, if the amount of H<sub>2</sub>O+CO<sub>2</sub> in the feed was lower than 400 kmol/h, a bad result at both objective functions was observed; thus, the lower bound of 400 kmol/h was specified for the amount of H<sub>2</sub>O+CO<sub>2</sub>.

**Table 3. Correlation used in the calculation of TPC [18]**

	Item	Assumptions & correlations
Operating & maintenance	Operating labor (OL)	60,000 \$/labor/year, 4 labor/shift, 3 shift/day [Republic of Korea]
	Supervisory & clerical labor (S&C)	OL×0.2
	Maintenance & repairs (M&R)	FCI×0.06
	Operating supplies	M&R×0.15
	Laboratory charges	OL×0.15
Others	Depreciation	(TCI−0.05×TCI)/20 (5% salvage value, 20 year)
	Local taxes & insurance	FCI×0.02
	Plant overhead costs	(OL+S&C+M&R)×0.6
	Administration	(OL+S&C+M&R)×0.2

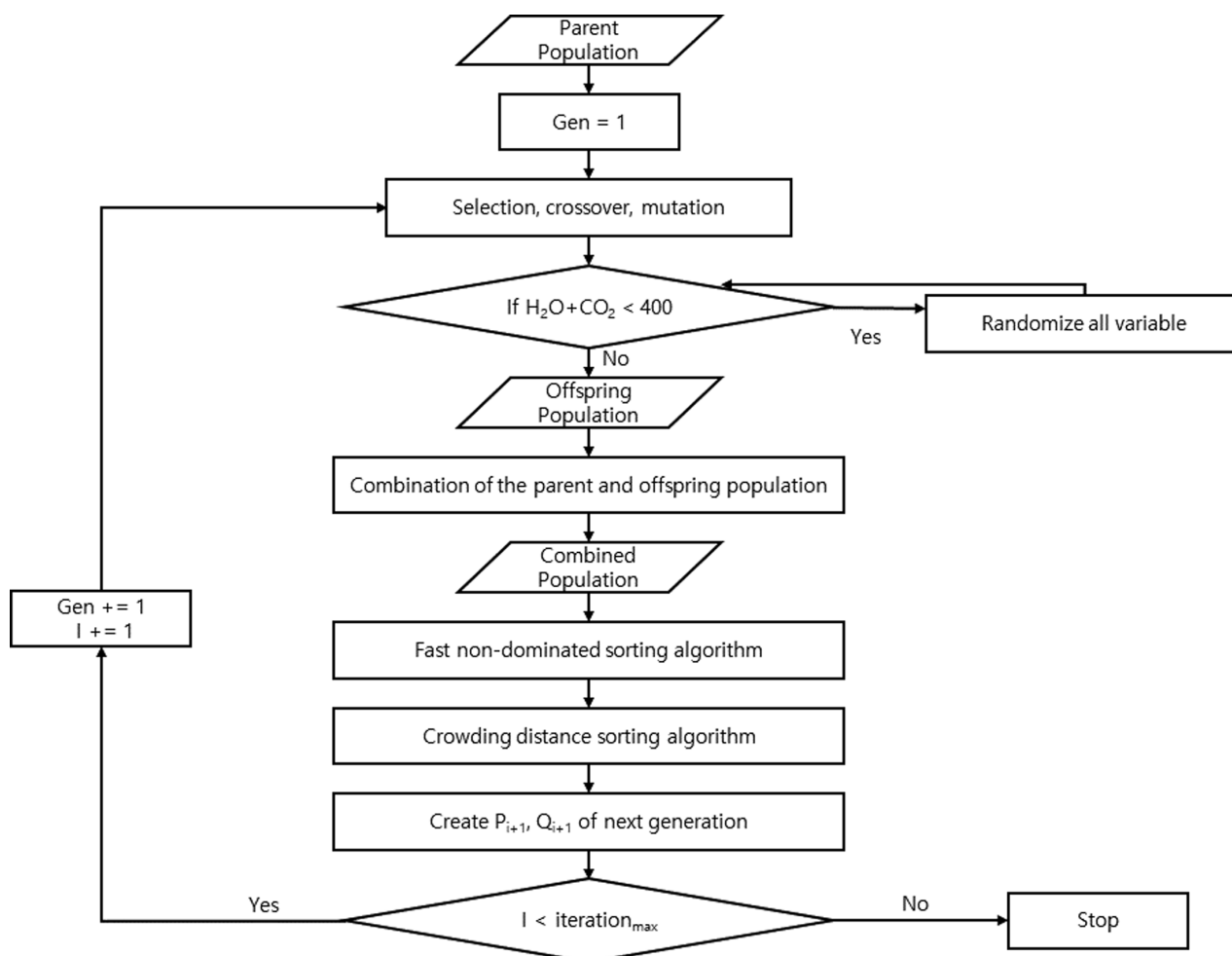


Fig. 2. Flow diagram of multi-objective optimization (NSGA II).

Process simulation was performed using HYSYS (Aspen Technology), and multi-objective optimization was performed using Python. The connection between HYSYS and Python was made using win32 dispatch [26], and the multi-objective optimization (NSGA II) was run using PYMOO [27] in a Python environment.

## RESULTS AND DISCUSSION

### 1. Case Study: Effects of the Purge Ratio

Under the base conditions (feed CO<sub>2</sub>=250 kmol/h, feed H<sub>2</sub>O=500 kmol/h, reformer pressure=500 kPa, reformer temperature=800 °C, MeOH synthesis reactor wall temperature=200 °C), the purge ratio was varied, and the results are shown in Fig. 3. As the purge ratio decreased to 0.1, the profit increased owing to the increase in the MeOH production rate, and CO<sub>2</sub> emission was reduced (CO<sub>2</sub> reduction was increased), indicating that a small purge ratio is preferred for both profit and CO<sub>2</sub> reduction under the base condition; however, there were no negative values for the net change of CO<sub>2</sub> (always CO<sub>2</sub> emissions) for all the purge ratios. When the purge ratio was between 0 and 0.1, the profit and net change of CO<sub>2</sub> fluctuated, probably owing to the convergence issue with the overall mass balance. Therefore, the purge ratio was fixed at 0.1.

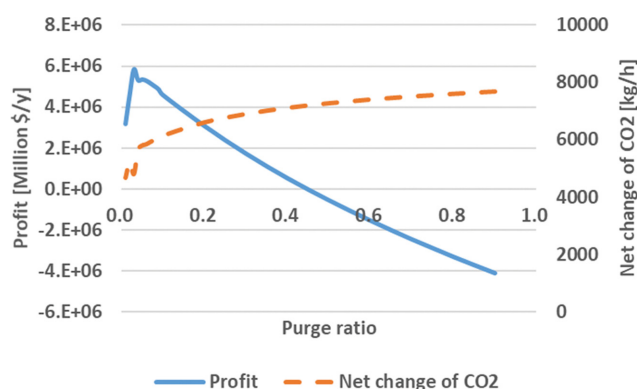
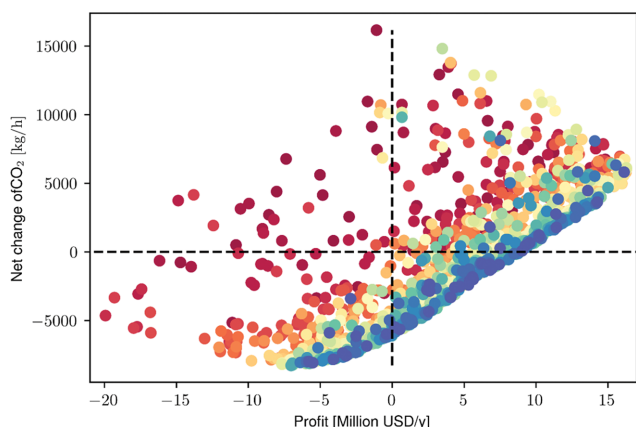


Fig. 3. Profit and net change of CO<sub>2</sub> as a function of purge ratio under the base condition.

### 2. Multi-objective Optimization

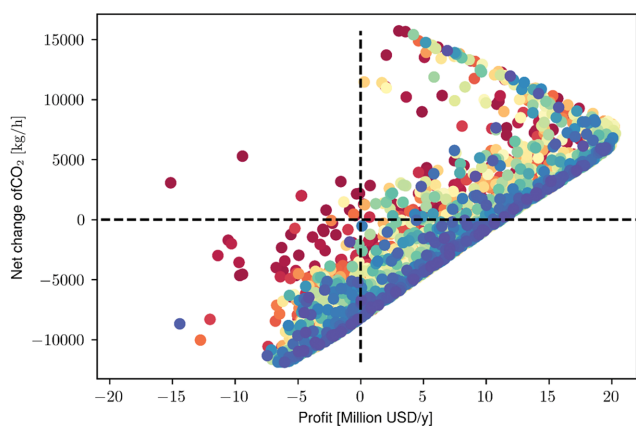
The amount of H<sub>2</sub>O and CO<sub>2</sub> in the feed, reformer operating temperature and pressure, and MeOH synthesis reactor utility temperature were considered as the arguments in the optimization (the amount of CH<sub>4</sub> in the feed was 500 kmol/h). Fig. 4 shows the result of multi-objective optimization (population size: 80, offspring:



**Fig. 4.** Multi-objective optimization results when population size, offspring, generation, and the total number of data are specified at 80, 40, 40, and 1640, respectively. The arguments are the amount of  $\text{H}_2\text{O}$  and  $\text{CO}_2$  in feed, reformer operating temperature and pressure, and MeOH synthesis reactor utility temperature. The first generation is marked with red dots, and the colors change from red to blue as the generation progresses (blue dots represent the last generation).

40, generation: 40, the total number of data: 1640).

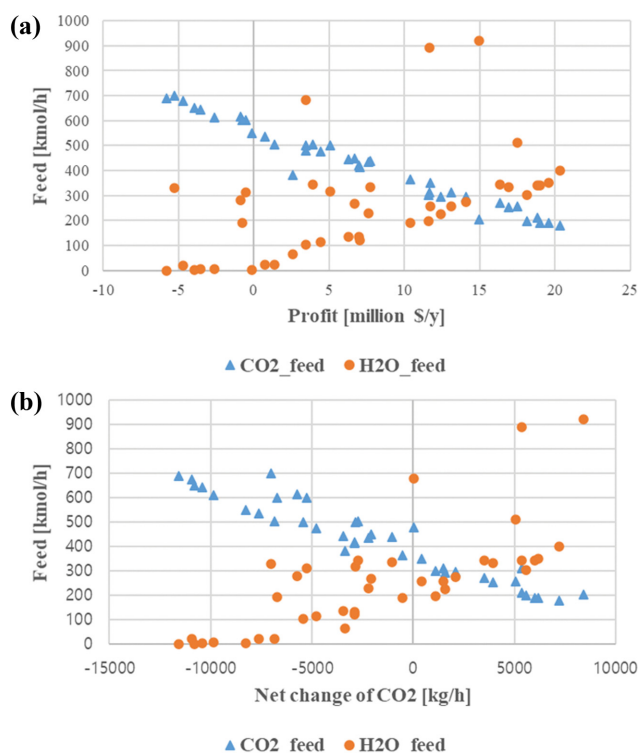
Table S1 in the supplementary shows the last generation data in ascending order of profit. In all data, the reformer temperature and utility temperature of the MeOH synthesis reactor were close to  $900^\circ\text{C}$  and  $200^\circ\text{C}$ , respectively, and the operating pressure of the reformer ranged mostly between 600 and 700 kPa. This means that the temperatures and pressures of the reactors insignificantly influence the profit and net change of  $\text{CO}_2$ . Meanwhile, it can be seen that as  $\text{CO}_2$  decreased and  $\text{H}_2\text{O}$  increased in the feed, both the profit and  $\text{CO}_2$  emissions increased, indicating a trade-off between profit and  $\text{CO}_2$  reduction.



**Fig. 5.** Multi-objective optimization results when population size, offspring, generation, and the total number of data are specified at 80, 40, 100, and 4040, respectively. The arguments are the amount of  $\text{H}_2\text{O}$  and  $\text{CO}_2$  in feed, reformer operating pressure, and MeOH synthesis reactor utility temperature. The first generation is marked with red dots, and the colors change from red to blue as the generation progresses (blue dots represent the last generation).

To identify a more accurate Pareto front, additional multi-objective optimization was performed with the upper limit of the amount of  $\text{CO}_2$  increased to  $700\text{ kmol/h}$ , and the reformer temperature fixed at  $900^\circ\text{C}$ . Fig. 5 shows the result of the multi-objective optimization when the  $\text{CO}_2$  feed,  $\text{H}_2\text{O}$  feed, reformer pressure, and MeOH synthesis reactor utility temperature are specified as the arguments (population size=80, offspring size=40, generation=100, total 4040 data), and Table S2 shows the last 40 generations of data in ascending order for profit. Note that the number of generations was specified to be large enough for the iterations to be converged. As shown in Fig. S1 in the Supplementary Information, the iterations converged when the generation was 50 and, thus, the generation was specified as 100 to guarantee the Pareto front was converged.

Upon reducing the number of arguments and increasing the range of  $\text{CO}_2$  in the feed, the operating pressure of the reformer in the second optimization converged to 1,000–1,100 kPa (Table S2), and a wider Pareto front was determined, as shown in Fig. 5. As observed in the first optimization, the amount of  $\text{H}_2\text{O}$  and  $\text{CO}_2$  in the feed played the most important role in the second optimization, and there was still a trade-off between profit and  $\text{CO}_2$  reduction. Fig. 6 shows the relationship between the amount of  $\text{H}_2\text{O}$  and  $\text{CO}_2$  in the feed with profit and net change of  $\text{CO}_2$ , where it is shown that high profit requires a high  $\text{H}_2\text{O}$  input (higher contribution of steam reforming than that of dry reforming), whereas low  $\text{CO}_2$  emission or  $\text{CO}_2$  reduction is accomplished at a high  $\text{CO}_2$  input (higher contribution of dry reforming than that of steam reforming). This feature is attributable to the competition between steam and dry reforming when steam is added; thus,  $\text{CO}_2$  consumption is decreased. However, the amount of hydrogen pro-



**Fig. 6.** The relationship of the amount of  $\text{CO}_2$  and  $\text{H}_2\text{O}$  in the feed with (a) profit and (b) net change of  $\text{CO}_2$ .



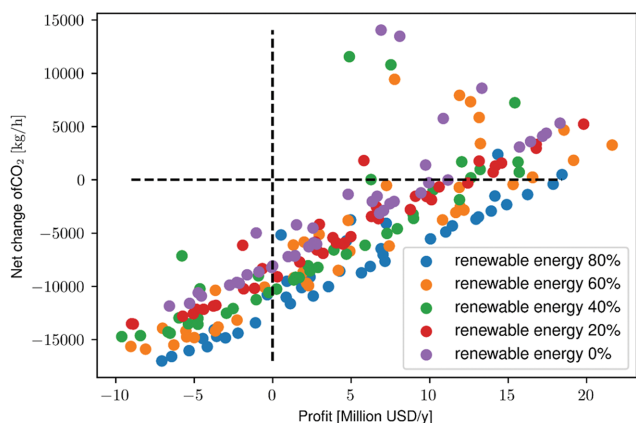


Fig. 7. Pareto front as a function of the use of renewable energy when population size, offspring, generation, and the total number of data are specified at 50, 40, 60, and 2410, respectively.

duced by steam reforming is larger than that by dry reforming (cf. Eqs. (1) and (4)); thus, a large amount of H<sub>2</sub>O increases the MeOH production, increasing the profit of the process.

It is worth noting that the net change of CO<sub>2</sub> was estimated by considering the change in its amount in the stream and energy usage, with the assumption that the CO<sub>2</sub> feed was 100% pure. Therefore, actual CO<sub>2</sub> emission or reduction might be different for the actual plant. In addition, the shape of the Pareto front may vary when other conditions, such as the use of waste heat and the use of steam, are considered. However, despite the deviations from the actual values, an inverse relationship between CO<sub>2</sub> reduction and economic profit is expected in methanol synthesis processes.

Recently, the replacement of fossil fuel energy with renewable energy has been widely considered in many research works. Because the use of renewable energy influences CO<sub>2</sub> emission significantly, sensitivity analysis of the Pareto front was conducted for various fractions of renewable energy usage. The amount of CO<sub>2</sub> generated by electricity usage was adjusted proportionally to the degree of replacement by renewable energy; for example, CO<sub>2</sub> equivalent for 80% of renewable energy was reduced to 0.2 times of 100% use of fossil fuel energy. As shown in Fig. 7, CO<sub>2</sub> reduction was increased as more renewable energy was used. The use of renewable energy also influenced the profit. When the net change of CO<sub>2</sub> was zero, the profit for 80% use of renewable energy was increased approximately 1.75 times higher than that of 0% renewable energy.

## CONCLUSIONS

Multi-object optimization (NSGA II) was applied to the MeOH synthesis process, and the resulting Pareto front showed that there was a trade-off between CO<sub>2</sub> reduction and economic profit. Despite the trade-off, there were conditions in which CO<sub>2</sub> reduction and economic profit were achieved simultaneously. At the maximum CO<sub>2</sub> reduction of 11,588 kg/h, the profit was −5.79 million dollars per year, while the maximum profit of 20 million dollars per year resulted in the maximum CO<sub>2</sub> emission (7,201 kg/h). Among the five variables (CO<sub>2</sub> and H<sub>2</sub>O in the feed, reformer temperature and pressure, and utility temperature of the MeOH synthesis reactor),

the amount of CO<sub>2</sub> and H<sub>2</sub>O in the feed had the most significant influence on the objective elements. A large amount of CO<sub>2</sub> in the feed showed a large contribution of dry reforming, resulting in low CO<sub>2</sub> emission (high CO<sub>2</sub> reduction) at the expense of the economics of the process due to the small amount of hydrogen, that is, low MeOH production rate. Meanwhile, the increase in the amount of H<sub>2</sub>O in the feed increased the economic profit as CO<sub>2</sub> emissions increased.

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## SUPPORTING INFORMATION

Additional information as noted in the text. This information is available via the Internet at <http://www.springer.com/chemistry/journal/11814>.

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## Supporting Information

### Multi-objective optimization of a methanol synthesis process: CO<sub>2</sub> emission vs. economics

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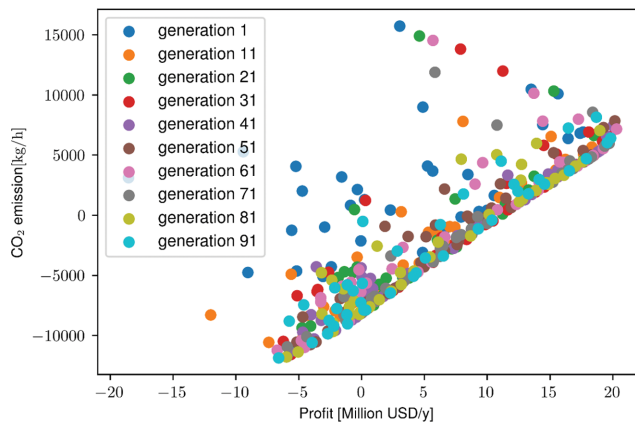
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Table S1. Dataset of the last generation in the first case of the multi-objective optimization (Fig. 4 in manuscript)

Arguments					Objectives	
Reformer temperature [°C]	MeOH synthesis reactor utility temperature [°C]	Reformer pressure [kPa]	CO <sub>2</sub> feed [kmol/h]	H <sub>2</sub> O feed [kmol/h]	Profit [M\$/y]	CO <sub>2</sub> emission [kg/h]
896.4	213.8	933.6	498.8	0.6	−5.8	−7,966.5
896.4	187.8	830	498.8	0.2	−5.5	−8,060.1
859.9	199.2	729.9	451.9	56.6	−4.4	−5,880.6
896.4	192.4	654	498.9	0.2	−4.1	−7,807.9
896.8	201.4	670.9	489.6	11	−3.5	−7,357.1
898.6	205.2	595.2	499.7	2.5	−3.2	−7,552.4
898.7	190.1	594.8	349.9	50.5	−2.9	−3,399.2
899.2	202	613.2	446.1	22.7	−2.5	−6,119.1
896.4	201.3	644.1	497.6	45.8	−1.8	−6,842.4
898.6	203.9	683.2	485.9	83.7	−0.4	−5,967.6
896.5	220	623.1	499.8	116.2	0.2	−5,481.8
898.4	194.9	616.6	486.5	102.2	0.5	−5,625.2
896.9	191.4	1,064.3	495.8	367.4	2.4	−2,754.3
896.4	198.9	640.6	498.1	202.4	2.6	−4,340.9
899	205.9	602.3	394.6	143.8	2.6	−2,341.4
898.6	198.5	595.7	468.1	211.5	2.6	−2,855.1
898.2	208.8	625.5	480.3	241.7	4.1	−3,294.1
898.6	202.4	786.5	491.9	342.2	4.3	−2,574.4
898.6	198.6	610.1	499.4	341.4	4.7	−2,517
899.2	207.9	634	435.3	236	5.3	−2,386.3
897.7	205.3	608.5	488.4	353.6	5.4	−2,081.7
898.6	203.6	607.8	491.1	384.5	5.6	−1,806.4
898.7	191.5	629.2	415.7	241	5.6	−1,985.2
898.5	209.1	637.5	485.2	465.8	6.2	−8,48.9
882.2	190.1	1,092.7	297.2	395.5	6.8	1,829.1
898.6	204.4	656.2	439	335	6.8	−1,312.6
893.9	191.5	701.6	413.6	339.7	6.8	−886
900	202	624.4	449.7	361.7	6.9	−1,212.6
899.7	202	625.1	435.8	361.6	7.4	−911.3
898.9	207.9	623.4	317.3	227.2	7.5	276.9
897.9	204.8	608.3	389.8	354.1	9.0	99.9
898.4	202	658.8	399	426.2	9.3	481.8
899.8	207	696	355.4	346.9	9.6	669.2
898.6	191.3	622.5	337.5	342.4	10.2	1,113.9
896.8	202.2	683.6	385	479.2	10.2	1,246.8
898.1	208.5	716.8	266.7	346.2	11.4	2,767.2
899.7	203.6	640.7	359.6	466.3	11.4	1,784
894.5	197.6	655.8	216.3	384.5	13.6	4,482.8
896.4	203.2	654.4	289.3	505	14.2	3,642
899.8	203.2	637	229.9	602	16.1	5,827.3

**Table S2. Dataset of the last generation in the second multi-objective optimization (Fig. 5 in manuscript)**

Arguments				Objectives	
MeOH synthesis reactor utility temperature [°C]	Reformer pressure [kPa]	CO <sub>2</sub> feed [kmol/h]	H <sub>2</sub> O feed [kmol/h]	Profit [M\$/y]	CO <sub>2</sub> emission [kg/h]
201.6	1,022.1	592.6	3.3	−1.6	−9,325.2
192.2	1,010.9	256.6	274.6	15.2	3,189.7
204.5	1,100.9	525.2	3.4	0.8	−7,360.7
201.3	1,080.8	378.4	187.4	9.9	−922.2
202.7	1,012.5	480.1	2.0	0.0	−6,723.8
196.2	1,057.2	317.0	329.4	14.0	2,225.4
193.1	1,013.0	455.0	141.2	5.6	−3,893.9
197.6	1,065.1	556.0	3.8	−0.2	−8,311.7
197.6	1,049.6	84.0	718.0	11.9	11,971.2
201.9	968.0	688.7	35.9	−4.9	−10,975.1
201.2	1,053.3	359.0	754.0	9.1	3,607.1
192.5	968.7	697.2	364.3	−4.1	−6,484.0
195.8	1,054.1	429.7	106.0	6.1	−3,564.3
209.4	1,032.6	609.3	8.1	−2.1	−9,569.9
198.1	1,007.3	635.6	2.9	−3.3	−10,377.7
200.2	1,029.9	316.7	314.0	14.0	2,010.6
200.1	1,054.0	484.7	108.3	4.2	−4,969.0
202.3	1,037.4	542.5	670.4	−0.9	−1,851.3
204.1	1,010.7	237.0	608.0	17.7	6,135.9
195.4	1,027.1	318.6	218.1	12.2	879.1
204.6	1,054.0	330.9	314.9	13.2	1,723.3
209.0	1,051.2	385.3	213.0	9.7	−856.8
192.9	1,054.1	352.5	234.9	11.4	230.6
197.6	1,025.6	677.1	127.1	−4.4	−9,383.1
203.9	986.4	394.9	141.2	7.1	−2,396.2
200.7	1,024.0	577.4	19.0	−0.8	−8,711.9
199.7	1,021.4	372.8	246.3	10.7	−299.2
206.4	1,018.3	699.5	259.2	−4.5	−7,757.6
199.6	1,059.2	512.5	2.6	0.8	−7,274.9
192.1	1,057.0	633.5	9.2	−3.6	−10,215.5
200.4	972.6	353.4	137.5	6.7	−1,539.0
197.8	1,023.0	416.1	136.1	7.1	−2,885.7
199.5	1,024.1	605.8	0.6	−2.1	−9,699.7
196.3	1,012.0	250.3	344.3	17.2	4,097.7
201.5	1,024.3	380.6	185.5	9.4	−1,223.8
204.7	1,054.6	663.2	4.2	−4.5	−10,906.3
201.9	1,030.7	43.0	876.0	6.9	14,072.2
209.6	1,032.6	612.9	8.4	−2.3	−9,640.7
206.3	1,053.1	508.4	74.9	2.8	−6,029.1
198.3	1,052.5	524.3	32.1	1.4	−7,122.7



**Fig. S1.** Multi-objective optimization results for each generation; all the data are provided in Fig. 5.